

# **The Business Cycle Component of US Asset Returns**

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Rimini Centre for Economic Analysis | July 7, 2009

# Outline

Data: cyclical properties of US asset prices and returns

Theory: numerical example [“Bansal-Yaron plus”]

# Cyclical properties of US asset prices and returns

Cross correlations for financial indicators and economic growth

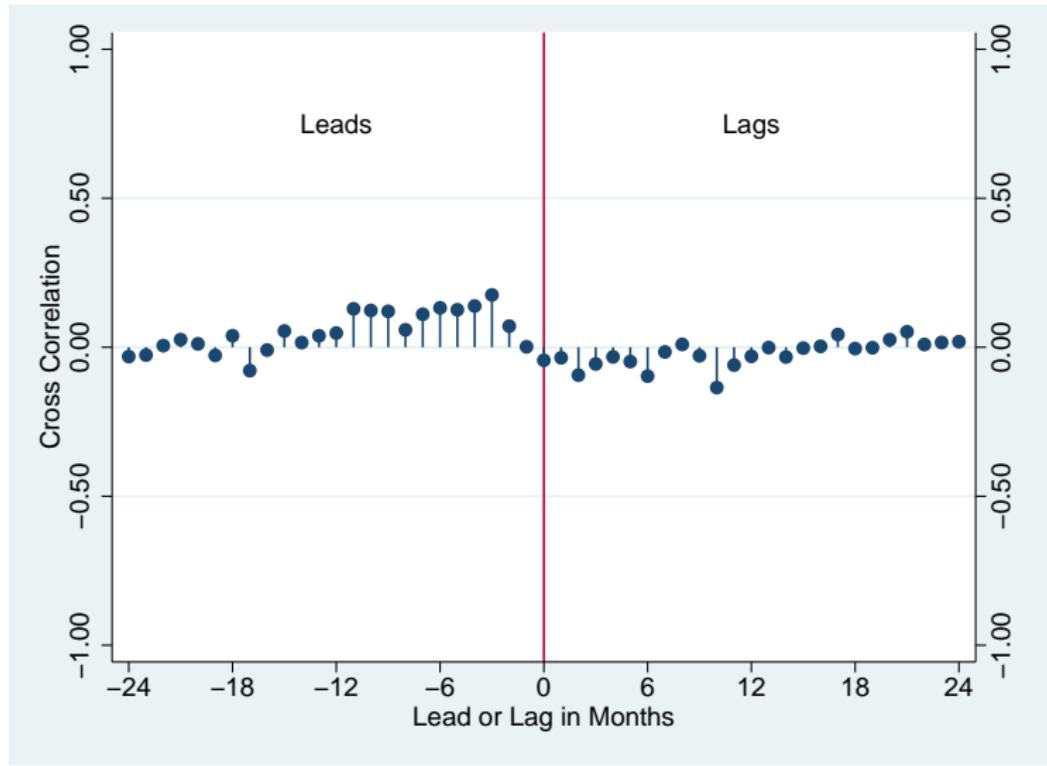
- ▶ Returns: logs of gross returns
- ▶ Excess returns: differences in logs of gross returns

Economic growth

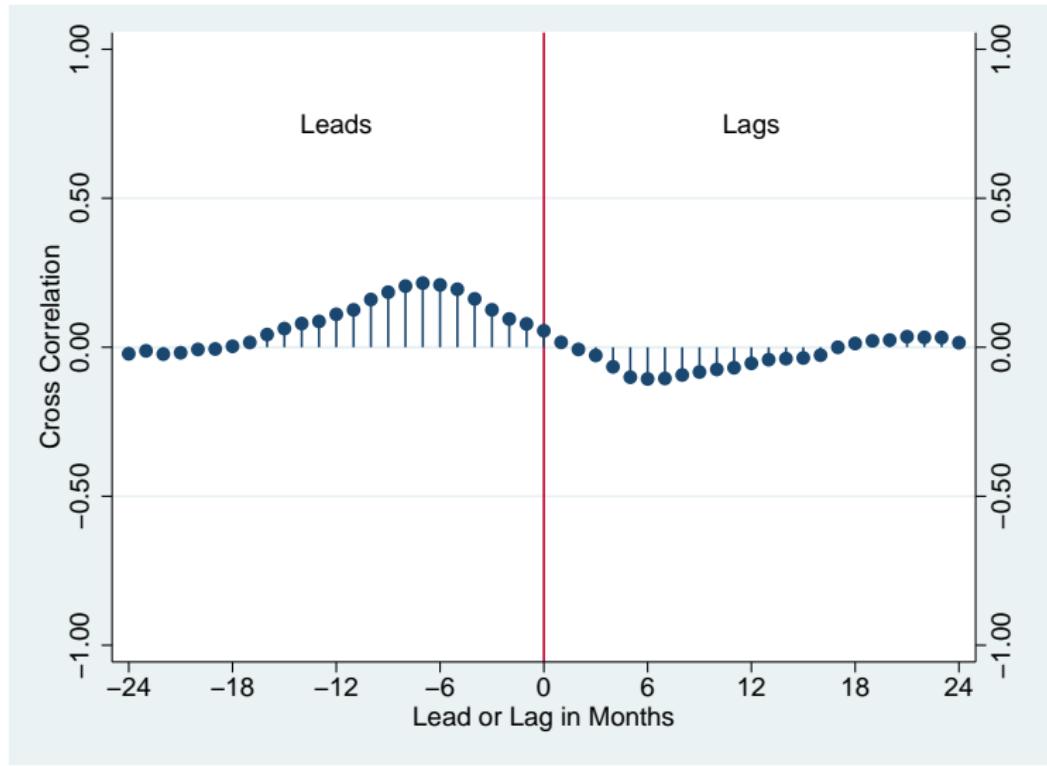
- ▶ Monthly:  $\log x_t - \log x_{t-1}$
- ▶ Or year-on-year:  $\log x_{t+6} - \log x_{t-6}$
- ▶ Computed from: [industrial production](#), consumption, employment

US data, monthly, 1960 to present

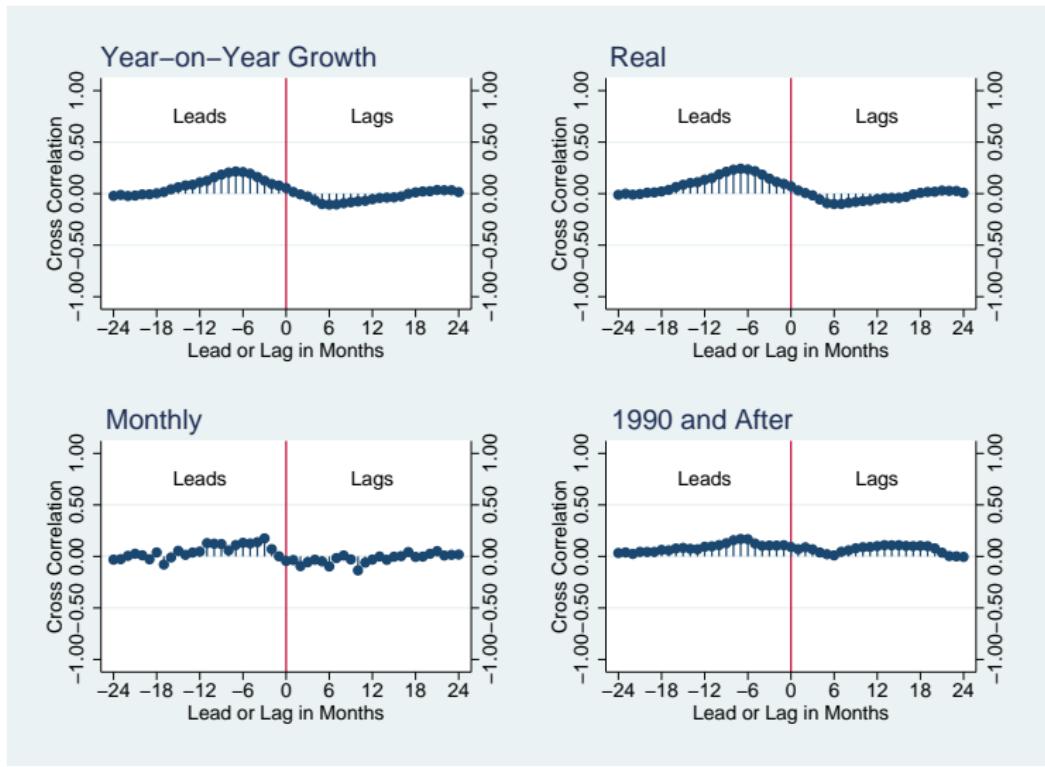
# Equity returns (monthly growth)



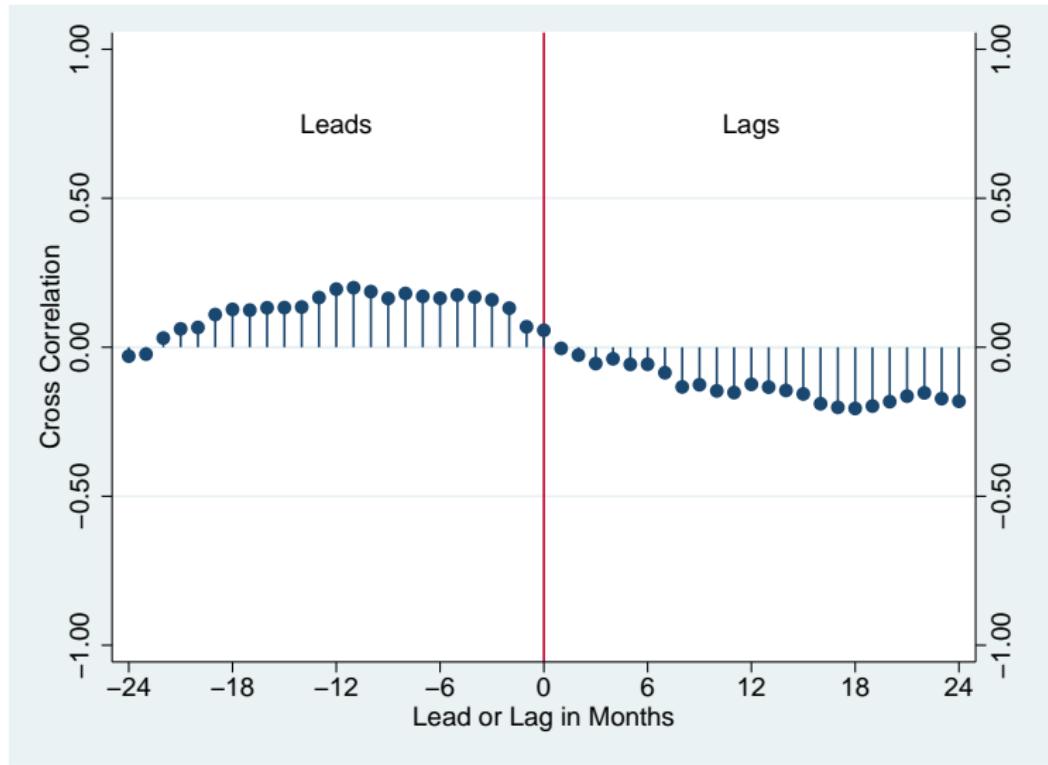
# Equity returns (yo<sub>y</sub> growth)



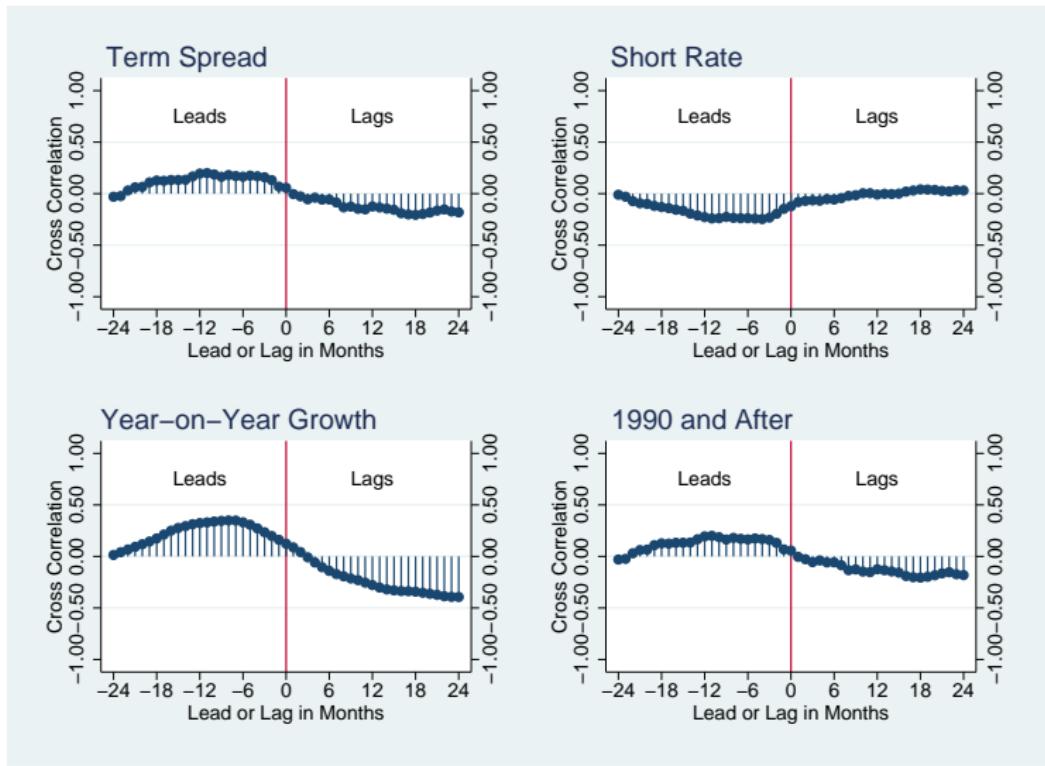
# Equity returns (variations)



# Term spread (monthly growth)

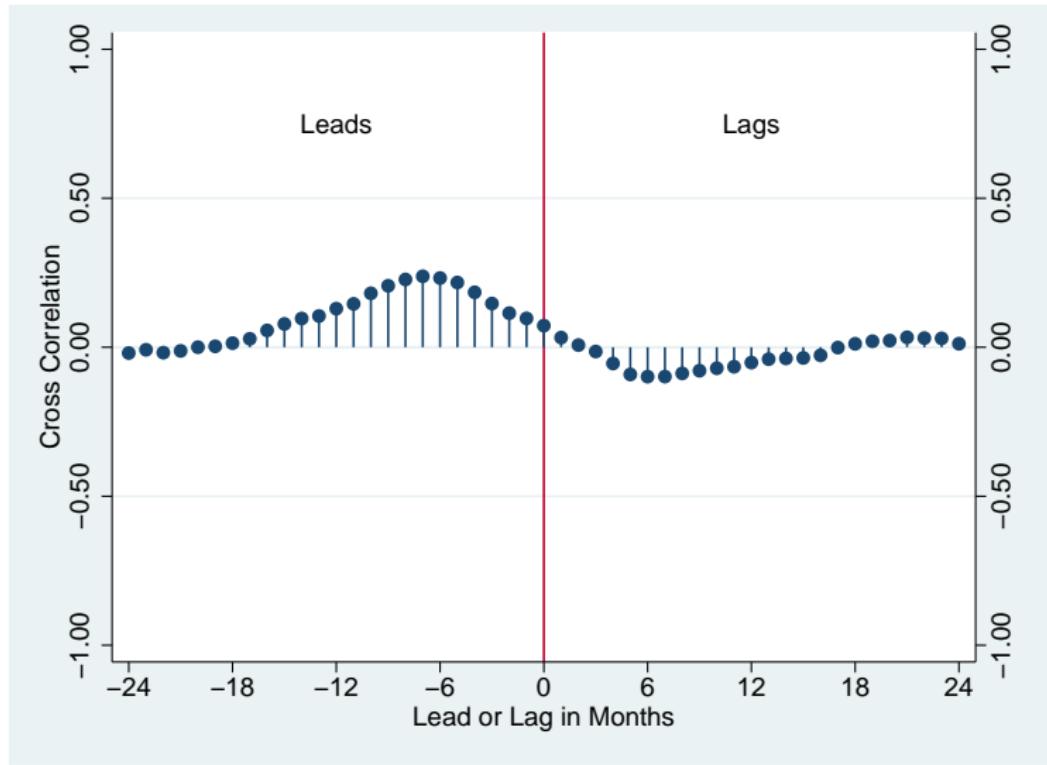


# Term spread (variations)

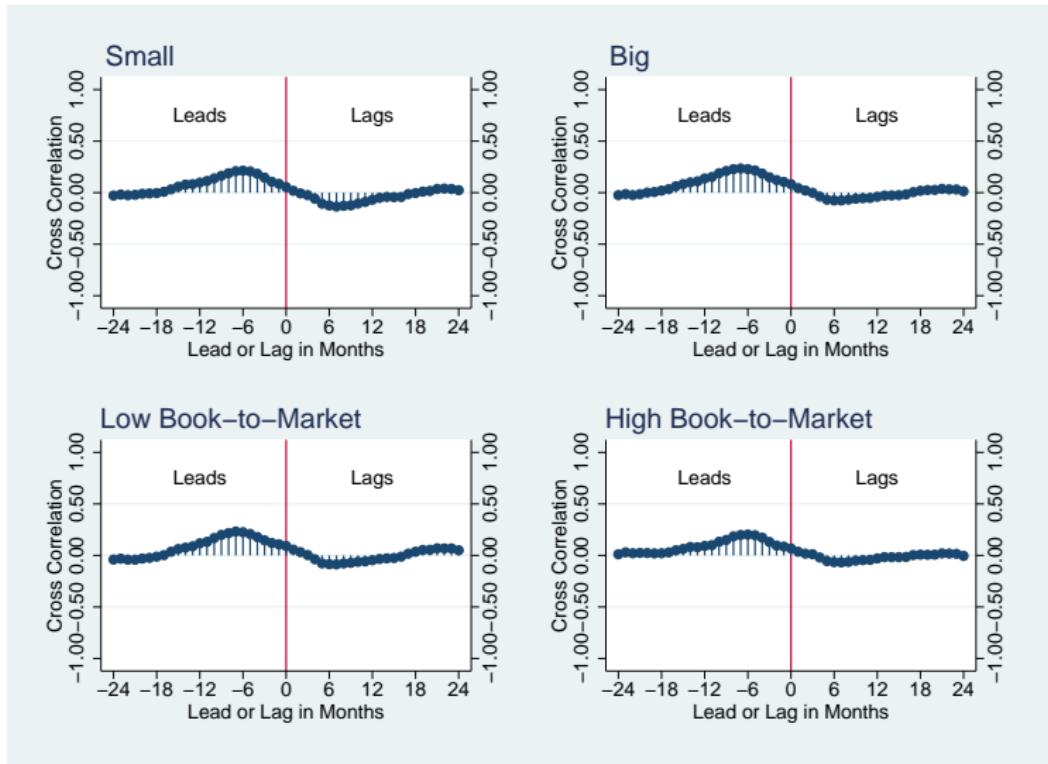


Think about this for a minute...

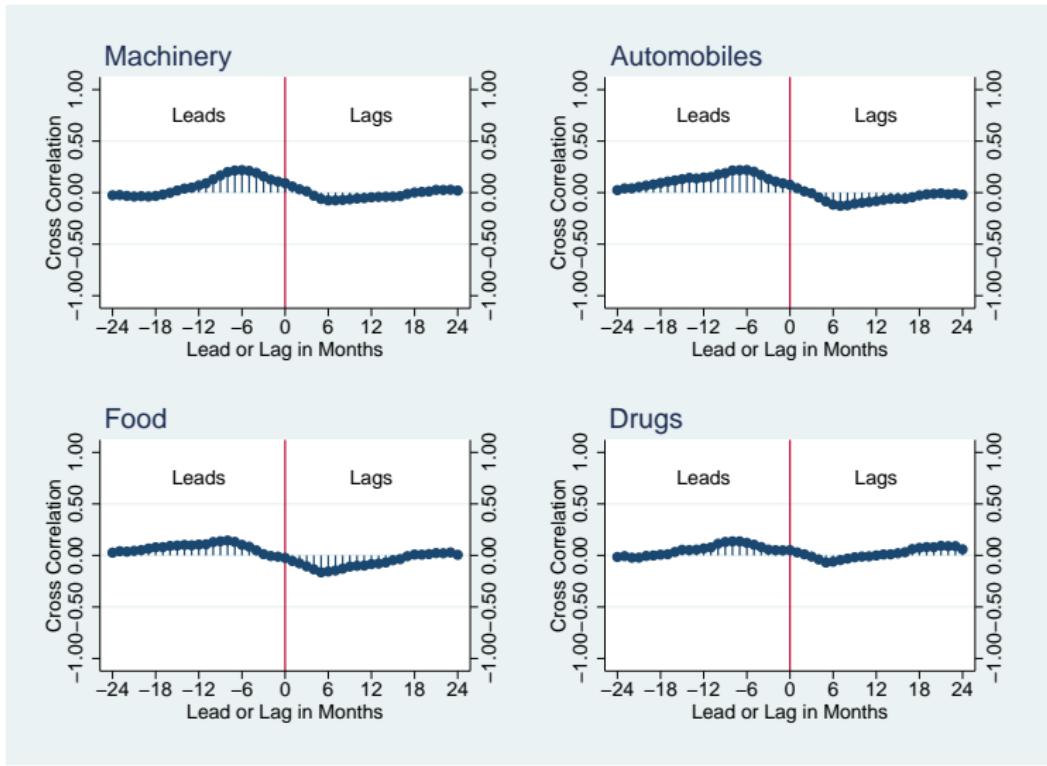
# Excess returns: equity (yoY)



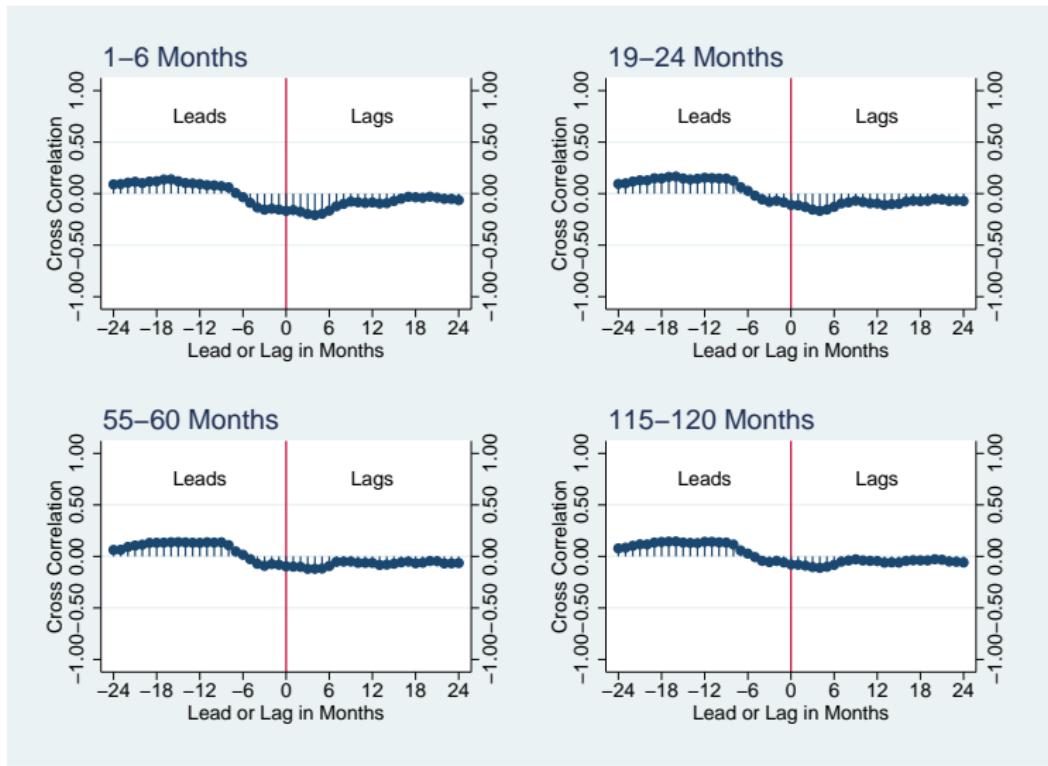
# Excess returns: Fama-French portfolios (yo<sup>y</sup>)



# Excess returns: industries (yo-y)



# Excess returns: bonds (yoY)



# Theoretical economy

Take a breath

What do we need?

- ▶ Variation in risk and/or price of risk
- ▶ ... tied to economic growth

Bansal-Yaron plus

- ▶ Representative agent exchange economy
- ▶ Recursive preferences (Kreps-Porteus/Epstein-Zin/Weil)
- ▶ Loglinear process for consumption growth
- ▶ Stochastic volatility
- ▶ **Interaction between growth and volatility**

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# Kreps-Porteus preferences

## Equations

$$\begin{aligned} U_t &= [(1 - \beta)c_t^\rho + \beta\mu_t(U_{t+1})^\rho]^{1/\rho} \\ \mu_t(U_{t+1}) &= (E_t U_{t+1}^\alpha)^{1/\alpha} \\ \alpha, \rho &\leq 1 \end{aligned}$$

## Interpretation

$$\begin{aligned} IES &= 1/(1 - \rho) \\ CRRA &= 1 - \alpha \\ \alpha &= \rho \Rightarrow \text{additive preferences} \end{aligned}$$

# Consumption growth

Consumption growth follows from

$$\begin{aligned}\log g_t &= g + e^\top x_t \\ x_{t+1} &= Ax_t + a(v_t - v) + v_t^{1/2} Bw_{t+1} \\ v_{t+1} &= (1 - \varphi_v)v + \varphi_v v_t + bw_{t+1}\end{aligned}$$

Note

- ▶  $A$  generates predictable component
- ▶  $v_t$  is stochastic
- ▶  $a$  generates interaction

# Kreps-Porteus pricing kernel

Marginal rate of substitution

$$m_{t+1} = \beta \left( \frac{c_{t+1}}{c_t} \right)^{\rho-1} \left( \frac{U_{t+1}}{\mu_t(U_{t+1})} \right)^{\alpha-\rho}$$

If  $\alpha = \rho$

- ▶ Second term disappears
- ▶ No roles for volatility or predictable consumption growth

# Expectations and certainty equivalents

Example: let  $\log x \sim N(u_t, v_t)$

Expectations and certainty equivalents for lognormals

$$\begin{aligned} E(x) &= \exp(u_t + v_t/2) \\ E(x^\alpha) &= \exp(\alpha u_t + \alpha^2 v_t/2) \\ \mu(x) &= [E(x^\alpha)]^{1/\alpha} = \exp(u_t + \alpha v_t/2). \end{aligned}$$

Effect of risk is multiplicative — additive in logs

# Role of recursive preferences I

Suppose consumption growth is

$$\log x_t = \log x + \sum_{j=0}^{\infty} \chi_j w_{t-j}$$

Pricing kernel

$$\begin{aligned}\log m_{t+1} &= \text{constant} + [(\rho - 1)\chi_0 + (\alpha - \rho)(\chi_0 + X_1)]w_{t+1} \\ &\quad + (\rho - 1) \sum_{j=0}^{\infty} \chi_{j+1} w_{t-j} \\ X_1 &= \sum_{j=1}^{\infty} \beta^j \chi_j \quad (\text{predictable component})\end{aligned}$$

# Role of recursive preferences II

Suppose

$$\log U_{t+1} = u_t + v_t^{1/2} w_{t+1}$$

Pricing kernel gets new terms

$$\begin{aligned}\log m_{t+1} &= \log \beta + (\rho - 1) \log(c_{t+1}/c_t) \\ &\quad + [(\rho - \alpha)/2] \alpha v_t + (\alpha - \rho) v_t^{1/2} w_{t+1}\end{aligned}$$

# Theoretical excess returns

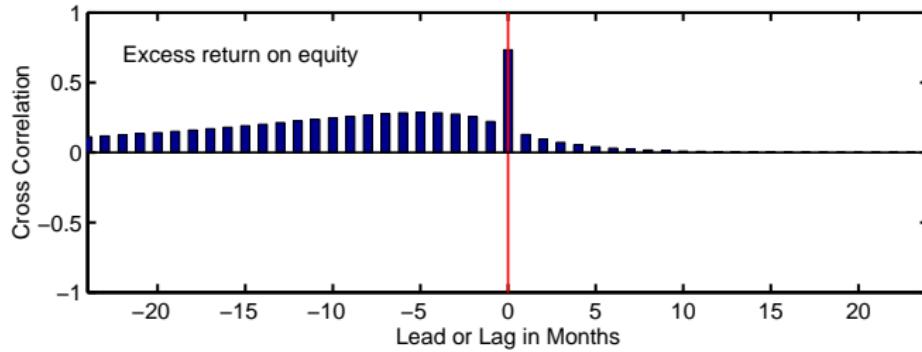
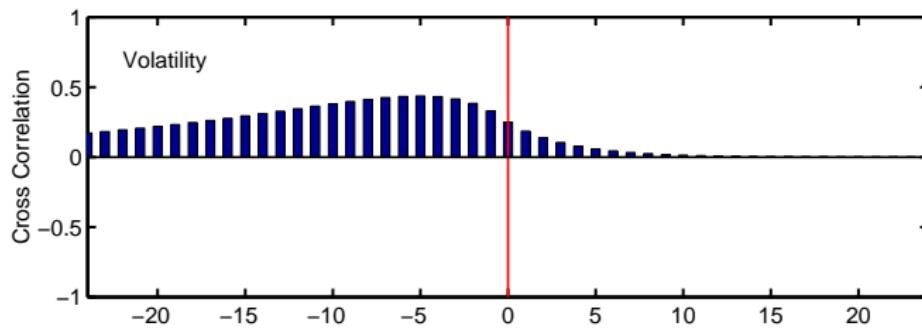
## Transparent loglinear solution

- ▶ We love this, but won't bore you with the details

## Excess returns depend on

- ▶ Volatility ( $v_t$ )
- ▶ Innovations in consumption growth and volatility ( $w_{t+1}$ )
- ▶ **Not:** expected future consumption growth ( $x_t$ )!

# Excess returns: numerical example



# Summary and extensions

## Summary

- ▶ Data: excess returns correlated with future growth
- ▶ Model: ditto via stochastic volatility

## Fixups and extensions

- ▶ Model dividends explicitly
- ▶ Production economies: volatility acts like shock to discount factor, affects consumption and labor supply

# Related work (some of it)

Evidence on financial indicators of business cycles

- ▶ Ang-Piazzesi-Wei, Estrella-Hardouvelis, King-Watson, Rouwenhorst, Stock-Watson

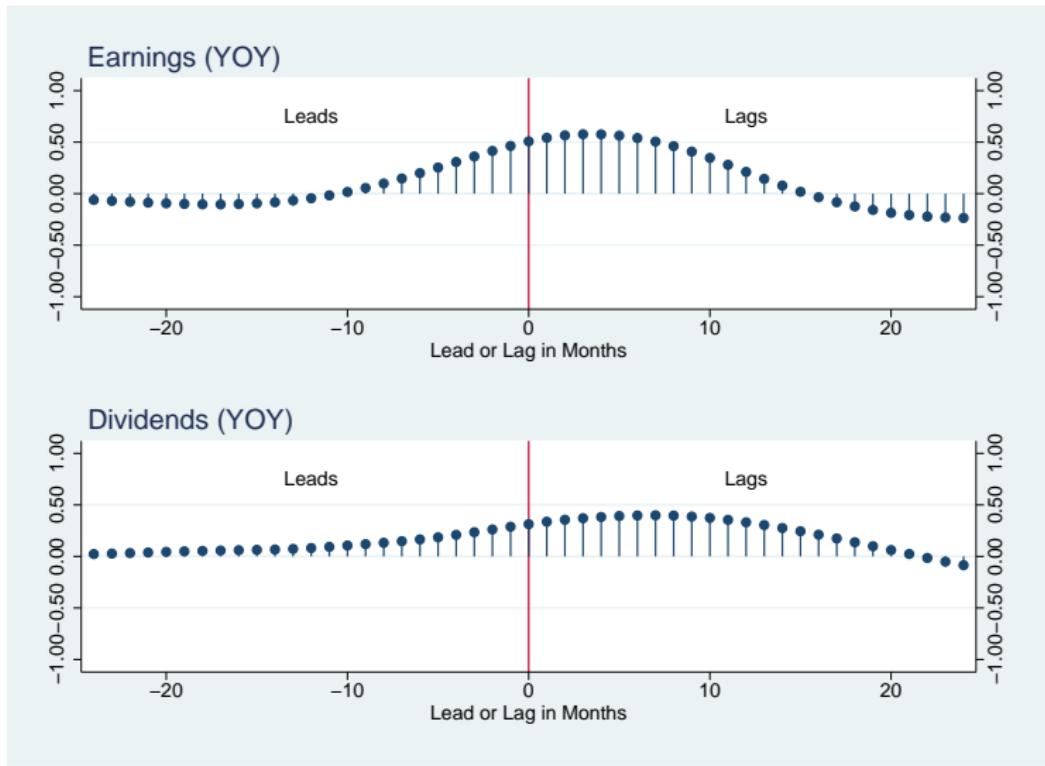
Kreps-Porteus pricing kernel

- ▶ Hansen-Heaton-Li, Weil

Stochastic volatility and returns

- ▶ Atkeson-Kehoe, Gallmeyer-Hollifield-Zin, Naik, Primiceri-Schaumburg-Tambalotti

# Earnings and dividends (yoY)



# Growth: several flavors (yoyn)

