Measuring Investment Returns

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Stern School of Business
First Principles

- Invest in projects that yield a return greater than the minimum acceptable hurdle rate.
  - The hurdle rate should be higher for riskier projects and reflect the financing mix used - owners’ funds (equity) or borrowed money (debt)
  - Returns on projects should be measured based on cash flows generated and the timing of these cash flows; they should also consider both positive and negative side effects of these projects.

- Choose a financing mix that minimizes the hurdle rate and matches the assets being financed.

- If there are not enough investments that earn the hurdle rate, return the cash to stockholders.
  - The form of returns - dividends and stock buybacks - will depend upon the stockholders’ characteristics.

Objective: Maximize the Value of the Firm
Measures of return: earnings versus cash flows

- Principles Governing Accounting Earnings Measurement
  - Accrual Accounting: Show revenues when products and services are sold or provided, not when they are paid for. Show expenses associated with these revenues rather than cash expenses.
  - Operating versus Capital Expenditures: Only expenses associated with creating revenues in the current period should be treated as operating expenses. Expenses that create benefits over several periods are written off over multiple periods (as depreciation or amortization).

- To get from accounting earnings to cash flows:
  - you have to add back non-cash expenses (like depreciation)
  - you have to subtract out cash outflows which are not expensed (such as capital expenditures)
  - you have to make accrual revenues and expenses into cash revenues and expenses (by considering changes in working capital).
Measuring Returns Right: The Basic Principles

- Use cash flows rather than earnings. You cannot spend earnings.
- Use “incremental” cash flows relating to the investment decision, i.e., cashflows that occur as a consequence of the decision, rather than total cash flows.
- Use “time weighted” returns, i.e., value cash flows that occur earlier more than cash flows that occur later.

Earnings versus Cash Flows: A Disney Theme Park

- The theme parks to be built near Bangkok, modeled on Euro Disney in Paris, will include a “Magic Kingdom” to be constructed, beginning immediately, and becoming operational at the beginning of the second year, and a second theme park modeled on Epcot Center at Orlando to be constructed in the second and third year and becoming operational at the beginning of the fifth year.
- The earnings and cash flows are estimated in nominal U.S. Dollars.
Key Assumptions on Start Up and Construction

- Disney has already spent $500 million researching the location and getting the needed licenses for the park.
- The cost of constructing Magic Kingdom will be $3 billion, with $2 billion invested up front, and $1 billion in year 1.
- The cost of constructing Epcot will be $1.5 billion, with $1 billion being spent in year 2 and $0.5 billion in year 3.
# Key Revenue Assumptions

**Revenue estimates for the parks and resort properties (in millions)**

<table>
<thead>
<tr>
<th>Year</th>
<th>Magic Kingdom</th>
<th>Epcot</th>
<th>Resort Hotels</th>
<th>Total Revenues</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$0</td>
<td>$0</td>
<td>$0</td>
<td>$0</td>
</tr>
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<td>$1,000</td>
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<td>$0</td>
<td>$300</td>
<td>$2,000</td>
</tr>
<tr>
<td>5</td>
<td>$2,000</td>
<td>$500</td>
<td>$375</td>
<td>$2,875</td>
</tr>
<tr>
<td>6</td>
<td>$2,200</td>
<td>$550</td>
<td>$688</td>
<td>$3,438</td>
</tr>
<tr>
<td>7</td>
<td>$2,420</td>
<td>$605</td>
<td>$756</td>
<td>$3,781</td>
</tr>
<tr>
<td>8</td>
<td>$2,662</td>
<td>$666</td>
<td>$832</td>
<td>$4,159</td>
</tr>
<tr>
<td>9</td>
<td>$2,928</td>
<td>$732</td>
<td>$915</td>
<td>$4,575</td>
</tr>
<tr>
<td>10 on</td>
<td>Grows at the inflation rate forever: 3%</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
The operating expenses are assumed to be 60% of the revenues at the parks, and 75% of revenues at the resort properties.

Disney will also allocate the following portion of its general and administrative expenses to the theme parks. It is worth noting that a recent analysis of these expenses found that only one-third of these expenses are variable (and a function of total revenue) and that two-thirds are fixed. (in millions)

<table>
<thead>
<tr>
<th>Year</th>
<th>G&amp; A Costs</th>
<th>Year</th>
<th>G&amp; A Costs</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$0</td>
<td>6</td>
<td>$293</td>
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<td>2</td>
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<td>$354</td>
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<tr>
<td>4</td>
<td>$242</td>
<td>9</td>
<td>$390</td>
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<tr>
<td>5</td>
<td>$266</td>
<td>10 on</td>
<td>Grow at inflation rate of 3%</td>
</tr>
</tbody>
</table>
# Depreciation and Capital Maintenance

<table>
<thead>
<tr>
<th>Year</th>
<th>Depreciation</th>
<th>Capital Expenditure</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$0</td>
<td>$0</td>
</tr>
<tr>
<td>2</td>
<td>$375</td>
<td>$150</td>
</tr>
<tr>
<td>3</td>
<td>$378</td>
<td>$206</td>
</tr>
<tr>
<td>4</td>
<td>$369</td>
<td>$250</td>
</tr>
<tr>
<td>5</td>
<td>$319</td>
<td>$359</td>
</tr>
<tr>
<td>6</td>
<td>$302</td>
<td>$344</td>
</tr>
<tr>
<td>7</td>
<td>$305</td>
<td>$303</td>
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<td>9</td>
<td>$305</td>
<td>$343</td>
</tr>
<tr>
<td>10</td>
<td>$315</td>
<td>$315</td>
</tr>
</tbody>
</table>

After Offsetting: Depreciation = Capital Maintenance
Other Assumptions

- Disney will have to maintain net working capital (primarily consisting of inventory at the theme parks and the resort properties, netted against accounts payable) of 5% of revenues, with the investments in working capital being made at the beginning of each year.

- The income from the investment will be taxed at a marginal tax rate of 36%.
## View 1: The Earnings View of the Project

<table>
<thead>
<tr>
<th></th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Revenues</td>
<td>$1,200</td>
<td>$1,650</td>
<td>$2,000</td>
<td>$4,575</td>
<td>$4,713</td>
</tr>
<tr>
<td>Operating Expenses (Non-Depr)</td>
<td>$750</td>
<td>$1,028</td>
<td>$1,245</td>
<td>$2,882</td>
<td>$2,969</td>
</tr>
<tr>
<td>Depreciation &amp; Amortization</td>
<td>$375</td>
<td>$378</td>
<td>$369</td>
<td>$305</td>
<td>$315</td>
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<tr>
<td>Allocated G&amp;A Costs</td>
<td>$200</td>
<td>$220</td>
<td>$242</td>
<td>$390</td>
<td>$401</td>
</tr>
<tr>
<td>Operating Income</td>
<td>$(125)</td>
<td>$25</td>
<td>$144</td>
<td>$998</td>
<td>$1,028</td>
</tr>
<tr>
<td>Taxes</td>
<td>$(45)</td>
<td>$9</td>
<td>$52</td>
<td>$359</td>
<td>$370</td>
</tr>
<tr>
<td>Operating Income after Taxes</td>
<td>$(80)</td>
<td>$16</td>
<td>$92</td>
<td>$639</td>
<td>$658</td>
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</tbody>
</table>
### The Full Picture: Earnings on Project

<table>
<thead>
<tr>
<th></th>
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<th>4</th>
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<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Revenues</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Magic Kingdom</td>
<td>$1,000</td>
<td>$1,400</td>
<td>$1,700</td>
<td>$2,000</td>
<td>$2,200</td>
<td>$2,420</td>
<td>$2,662</td>
<td>$2,928</td>
<td>$2,928</td>
<td>$3,016</td>
<td></td>
</tr>
<tr>
<td>Second Theme Park</td>
<td>$500</td>
<td>$550</td>
<td>$605</td>
<td>$666</td>
<td>$666</td>
<td>$732</td>
<td>$754</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Resort &amp; Properties</td>
<td>$200</td>
<td>$250</td>
<td>$300</td>
<td>$375</td>
<td>$688</td>
<td>$756</td>
<td>$832</td>
<td>$915</td>
<td>$943</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td>$1,200</td>
<td>$1,650</td>
<td>$2,000</td>
<td>$2,875</td>
<td>$3,438</td>
<td>$3,781</td>
<td>$4,159</td>
<td>$4,575</td>
<td>$4,713</td>
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</tr>
<tr>
<td><strong>Operating Expenses</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Magic Kingdom</td>
<td>$600</td>
<td>$840</td>
<td>$1,020</td>
<td>$1,200</td>
<td>$1,320</td>
<td>$1,452</td>
<td>$1,597</td>
<td>$1,757</td>
<td>$1,810</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Second Theme Park</td>
<td>-$</td>
<td>-$</td>
<td>-$</td>
<td>$300</td>
<td>$330</td>
<td>$363</td>
<td>$399</td>
<td>$439</td>
<td>$452</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Resort &amp; Property</td>
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<td>$188</td>
<td>$225</td>
<td>$281</td>
<td>$516</td>
<td>$567</td>
<td>$624</td>
<td>$686</td>
<td>$707</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td>$750</td>
<td>$1,028</td>
<td>$1,245</td>
<td>$1,781</td>
<td>$2,166</td>
<td>$2,382</td>
<td>$2,620</td>
<td>$2,882</td>
<td>$2,969</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Other Expenses</strong></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td>$302</td>
<td>$305</td>
<td>$305</td>
<td>$305</td>
<td>$315</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Allocated G&amp;A Costs</td>
<td>$200</td>
<td>$220</td>
<td>$242</td>
<td>$266</td>
<td>$293</td>
<td>$322</td>
<td>$354</td>
<td>$390</td>
<td>$401</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Operating Income</strong></td>
<td>$(125)</td>
<td>$25</td>
<td>$144</td>
<td>$509</td>
<td>$677</td>
<td>$772</td>
<td>$880</td>
<td>$998</td>
<td>$1,028</td>
<td></td>
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<tr>
<td>Taxes</td>
<td>$(45 )</td>
<td>$9</td>
<td>$52</td>
<td>$183</td>
<td>$244</td>
<td>$278</td>
<td>$317</td>
<td>$359</td>
<td>$370</td>
<td></td>
<td></td>
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<tr>
<td><strong>Operating Income after Taxes</strong></td>
<td>$(80)</td>
<td>$16</td>
<td>$92</td>
<td>$326</td>
<td>$433</td>
<td>$494</td>
<td>$563</td>
<td>$639</td>
<td>$658</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
### And the Accounting View of Return

<table>
<thead>
<tr>
<th>Year</th>
<th>EBIT(1-t)</th>
<th>Beg BV</th>
<th>Deprecn</th>
<th>Cap Ex</th>
<th>End BV</th>
<th>Avge Bv</th>
<th>ROC</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$0</td>
<td>$2,500</td>
<td>$0</td>
<td>$2,500</td>
<td>$2,500</td>
<td>$2,500</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>$0</td>
<td>$2,500</td>
<td>$0</td>
<td>$1,000</td>
<td>$3,500</td>
<td>$3,000</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>($80)</td>
<td>$3,500</td>
<td>$375</td>
<td>$1,150</td>
<td>$4,275</td>
<td>$3,888</td>
<td>-2.06%</td>
</tr>
<tr>
<td>3</td>
<td>$16</td>
<td>$4,275</td>
<td>$378</td>
<td>$706</td>
<td>$4,604</td>
<td>$4,439</td>
<td>0.36%</td>
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<tr>
<td>4</td>
<td>$92</td>
<td>$4,604</td>
<td>$369</td>
<td>$250</td>
<td>$4,484</td>
<td>$4,544</td>
<td>2.02%</td>
</tr>
<tr>
<td>5</td>
<td>$326</td>
<td>$4,484</td>
<td>$319</td>
<td>$359</td>
<td>$4,525</td>
<td>$4,505</td>
<td>7.23%</td>
</tr>
<tr>
<td>6</td>
<td>$433</td>
<td>$4,525</td>
<td>$302</td>
<td>$344</td>
<td>$4,567</td>
<td>$4,546</td>
<td>9.53%</td>
</tr>
<tr>
<td>7</td>
<td>$494</td>
<td>$4,567</td>
<td>$305</td>
<td>$303</td>
<td>$4,564</td>
<td>$4,566</td>
<td>10.82%</td>
</tr>
<tr>
<td>8</td>
<td>$563</td>
<td>$4,564</td>
<td>$305</td>
<td>$312</td>
<td>$4,572</td>
<td>$4,568</td>
<td>12.33%</td>
</tr>
<tr>
<td>9</td>
<td>$639</td>
<td>$4,572</td>
<td>$305</td>
<td>$343</td>
<td>$4,609</td>
<td>$4,590</td>
<td>13.91%</td>
</tr>
<tr>
<td>10</td>
<td>$658</td>
<td>$4,609</td>
<td>$315</td>
<td>$315</td>
<td>$4,609</td>
<td>$4,609</td>
<td>14.27%</td>
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<tr>
<td>Average</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>7.60%</td>
</tr>
</tbody>
</table>
Would lead use to conclude that...

- Do not invest in this park. The return on capital of 7.60% is lower than the cost of capital for theme parks of 12.32%; This would suggest that the project should not be taken.
- Given that we have computed the average over an arbitrary period of 10 years, while the theme park itself would have a life greater than 10 years, would you feel comfortable with this conclusion?
  - Yes
  - No
Just as a comparison of project return on capital to the cost of capital yields a measure of whether the project is acceptable, a comparison can be made at the firm level, to judge whether the existing projects of the firm are adding or destroying value.

Disney, in 1996, had earnings before interest and taxes of $5,559 million, had a book value of equity of $11,368 million and a book value of debt of $7,663 million. With a tax rate of 36%, we get

\[ \text{Return on Capital} = \frac{5559 \times (1-.36)}{11,368+7,663} = 18.69\% \]

\[ \text{Cost of Capital for Disney} = 12.22\% \]

\[ \text{Excess Return} = 18.69\% - 12.22\% = 6.47\% \]

This can be converted into a dollar figure by multiplying by the capital invested, in which case it is called economic value added

\[ \text{EVA} = (0.1869-0.1222) \times (11,368+7,663) = $1,232 \text{ million} \]
To get from income to cash flow, we

- added back all non-cash charges such as depreciation
- subtracted out the capital expenditures
- subtracted out the change in non-cash working capital
The Depreciation Tax Benefit

- While depreciation reduces taxable income and taxes, it does not reduce the cash flows.
- The benefit of depreciation is therefore the tax benefit. In general, the tax benefit from depreciation can be written as:
  \[
  \text{Tax Benefit} = \text{Depreciation} \times \text{Tax Rate}
  \]
- For example, in year 2, the tax benefit from depreciation to Disney from this project can be written as:
  \[
  \text{Tax Benefit in year 2} = 375 \text{ million} \times .36 = 135 \text{ million}
  \]
- **Proposition 1**: The tax benefit from depreciation and other non-cash charges is greater, the higher your tax rate.
- **Proposition 2**: Non-cash charges that are not tax deductible (such as amortization of goodwill) and thus provide no tax benefits have no effect on cash flows.
Depreciation Methods

Broadly categorizing, depreciation methods can be classified as straight line or accelerated methods. In straight line depreciation, the capital expense is spread evenly over time. In accelerated depreciation, the capital expense is depreciated more in earlier years and less in later years. Assume that you made a large investment this year, and that you are choosing between straight line and accelerated depreciation methods. Which will result in higher net income this year?

- Straight Line Depreciation
- Accelerated Depreciation

Which will result in higher cash flows this year?

- Straight Line Depreciation
- Accelerated Depreciation
The Capital Expenditures Effect

- Capital expenditures are not treated as accounting expenses but they do cause cash outflows.
- Capital expenditures can generally be categorized into two groups
  - New (or Growth) capital expenditures are capital expenditures designed to create new assets and future growth
  - Maintenance capital expenditures refer to capital expenditures designed to keep existing assets.
- Both initial and maintenance capital expenditures reduce cash flows
- The need for maintenance capital expenditures will increase with the life of the project. In other words, a 25-year project will require more maintenance capital expenditures than a 2-year asset.
To cap ex or not to cap ex

- Assume that you run your own software business, and that you have an expense this year of $100 million from producing and distribution promotional CDs in software magazines. Your accountant tells you that you can expense this item or capitalize and depreciate. Which will have a more positive effect on income?
  - Expense it
  - Capitalize and Depreciate it

Which will have a more positive effect on cash flows?
  - Expense it
  - Capitalize and Depreciate it
The Working Capital Effect

- Intuitively, money invested in inventory or in accounts receivable cannot be used elsewhere. It, thus, represents a drain on cash flows.
- To the degree that some of these investments can be financed using suppliers credit (accounts payable) the cash flow drain is reduced.
- Investments in working capital are thus cash outflows
  - Any increase in working capital reduces cash flows in that year
  - Any decrease in working capital increases cash flows in that year
- To provide closure, working capital investments need to be salvaged at the end of the project life.

Proposition 1: The failure to consider working capital in a capital budgeting project will overstate cash flows on that project and make it look more attractive than it really is.

Proposition 2: Other things held equal, a reduction in working capital requirements will increase the cash flows on all projects for a firm.
The incremental cash flows on the project

<table>
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<tr>
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<th>1</th>
<th>2</th>
<th>3</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cash Flow on Project</td>
<td>$ (2,500)</td>
<td>$ (1,000)</td>
<td>$ (915)</td>
<td>$ (335)</td>
<td>$ 580</td>
<td>$ 651</td>
</tr>
<tr>
<td>- Sunk Costs</td>
<td>$ 500</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>+ Non-incremental Allocated Costs</td>
<td>$ -</td>
<td>$ -</td>
<td>$ 85</td>
<td>$ 94</td>
<td>$ 166</td>
<td>$ 171</td>
</tr>
<tr>
<td>Incremental Cash Flow on Project</td>
<td>$ (2,000)</td>
<td>$ (1,000)</td>
<td>$ (830)</td>
<td>$ (241)</td>
<td>$ 746</td>
<td>$ 822</td>
</tr>
</tbody>
</table>

To get from cash flow to incremental cash flows, we

- subtract out sunk costs
- subtract the non-incremental allocated costs (in after-tax terms)
Sunk Costs

- Any expenditure that has *already been incurred, and cannot be* recovered (even if a project is rejected) is called a sunk cost.
- When analyzing a project, sunk costs *should not be considered* since they are incremental.
- By this definition, market testing expenses and R&D expenses are both likely to be sunk costs before the projects that are based upon them are analyzed. If sunk costs are not considered in project analysis, how can a firm ensure that these costs are covered?
Allocated Costs

- Firms allocate costs to individual projects from a centralized pool (such as general and administrative expenses) based upon some characteristic of the project (sales is a common choice).
- For large firms, these allocated costs can result in the rejection of projects.
- To the degree that these costs are not incremental (and would exist anyway), this makes the firm worse off.
- Thus, it is only the incremental component of allocated costs that should show up in project analysis.
- How, looking at these pooled expenses, do we know how much of the costs are fixed and how much are variable?
The Incremental Cash Flows

<table>
<thead>
<tr>
<th></th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Operating Income after Taxes</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>+ Depreciation &amp; Amortization</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>- Capital Expenditures</td>
<td>$2,000</td>
<td>$1,000</td>
<td>$1,150</td>
<td>$706</td>
<td>$250</td>
<td>$359</td>
<td>$344</td>
<td>$303</td>
<td>$312</td>
<td>$343</td>
<td>$315</td>
</tr>
<tr>
<td>- Change in Working Capital</td>
<td>$60</td>
<td>$23</td>
<td>$18</td>
<td>$44</td>
<td>$28</td>
<td>$17</td>
<td>$19</td>
<td>$21</td>
<td>$7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>+ Non-incremental Allocated Expense</td>
<td>$85</td>
<td>$94</td>
<td>$103</td>
<td>$114</td>
<td>$125</td>
<td>$137</td>
<td>$151</td>
<td>$166</td>
<td>$171</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cashflow to Firm</td>
<td>$(2,000)</td>
<td>$(1,000)</td>
<td>$(830)</td>
<td>$(241)</td>
<td>$297</td>
<td>$355</td>
<td>$488</td>
<td>$617</td>
<td>$688</td>
<td>$746</td>
<td>$822</td>
</tr>
</tbody>
</table>
To Time-Weighted Cash Flows

- Incremental cash flows in the earlier years are worth more than incremental cash flows in later years.

- In fact, cash flows across time cannot be added up. They have to be brought to the same point in time before aggregation.

- This process of moving cash flows through time is
  - discounting, when future cash flows are brought to the present
  - compounding, when present cash flows are taken to the future

- The discounting and compounding is done at a discount rate that will reflect
  - Expected inflation: Higher Inflation -> Higher Discount Rates
  - Expected real rate: Higher real rate -> Higher Discount rate
  - Expected uncertainty: Higher uncertainty -> Higher Discount Rate
## Present Value Mechanics

<table>
<thead>
<tr>
<th>Cash Flow Type</th>
<th>Discounting Formula</th>
<th>Compounding Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Simple CF</td>
<td>( CF_n / (1+r)^n )</td>
<td>( CF_0 (1+r)^n )</td>
</tr>
</tbody>
</table>
| 2. Annuity             | \[
A \left\{ \frac{1 - \frac{1}{(1+r)^n}}{r} \right\}
\]  | \[
A \left\{ \frac{(1+r)^n - 1}{r} \right\}
\]  |
| 3. Growing Annuity     | \[
A(1+g) \left\{ \frac{1 - \frac{(1+g)^n}{(1+r)^n}}{r - g} \right\}
\]  | \[   \] |
| 4. Perpetuity          | \( A/r \)                   |                             |
| 5. Growing Perpetuity  | \( A(1+g)/(r-g) \)          |                             |
Discounted cash flow measures of return

- **Net Present Value (NPV):** The net present value is the sum of the present values of all cash flows from the project (including initial investment).
  \[ NPV = \text{Sum of the present values of all cash flows on the project, including the initial investment, with the cash flows being discounted at the appropriate hurdle rate (cost of capital, if cash flow is cash flow to the firm, and cost of equity, if cash flow is to equity investors)} \]
  - Decision Rule: Accept if NPV > 0

- **Internal Rate of Return (IRR):** The internal rate of return is the discount rate that sets the net present value equal to zero. It is the percentage rate of return, based upon incremental time-weighted cash flows.
  - Decision Rule: Accept if IRR > hurdle rate
In a project with a finite and short life, you would need to compute a salvage value, which is the expected proceeds from selling all of the investment in the project at the end of the project life. It is usually set equal to book value of fixed assets and working capital.

In a project with an infinite or very long life, we compute cash flows for a reasonable period, and then compute a terminal value for this project, which is the present value of all cash flows that occur after the estimation period ends.

Assuming the project lasts forever, and that cash flows after year 9 grow 3% (the inflation rate) forever, the present value at the end of year 9 of cash flows after that can be written as:
- Terminal Value = \( \frac{\text{CF in year 10}}{\text{Cost of Capital} - \text{Growth Rate}} \)
  = \( \frac{822}{(.1232-.03)} \) = $8,821 million
Which yields a NPV of..

<table>
<thead>
<tr>
<th>Year</th>
<th>Incremental CF</th>
<th>Terminal Value</th>
<th>PV at 12.32%</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$(2,000)$</td>
<td>$(2,000)$</td>
<td>$(2,000)$</td>
</tr>
<tr>
<td>1</td>
<td>$(1,000)$</td>
<td>$(890)$</td>
<td>$(890)$</td>
</tr>
<tr>
<td>2</td>
<td>$(830)$</td>
<td>$(658)$</td>
<td>$(658)$</td>
</tr>
<tr>
<td>3</td>
<td>$(241)$</td>
<td>$(170)$</td>
<td>$(170)$</td>
</tr>
<tr>
<td>4</td>
<td>$297$</td>
<td>$187$</td>
<td>$187$</td>
</tr>
<tr>
<td>5</td>
<td>$355$</td>
<td>$198$</td>
<td>$198$</td>
</tr>
<tr>
<td>6</td>
<td>$488$</td>
<td>$243$</td>
<td>$243$</td>
</tr>
<tr>
<td>7</td>
<td>$617$</td>
<td>$273$</td>
<td>$273$</td>
</tr>
<tr>
<td>8</td>
<td>$688$</td>
<td>$272$</td>
<td>$272$</td>
</tr>
<tr>
<td>9</td>
<td>$746$</td>
<td>$8,821$</td>
<td>$3,363$</td>
</tr>
</tbody>
</table>

Net Present Value of Project = $818
Which makes the argument that..

- **The project should be accepted.** The positive net present value suggests that the project will add value to the firm, and earn a return in excess of the cost of capital.
- By taking the project, Disney will increase its value as a firm by $818 million.
The IRR of this project

NPV Profile for Theme Park

Discount Rate

NPV

($3,000) ($2,000) ($1,000) $0 $1,000 $2,000 $3,000 $4,000 $5,000 $6,000 $7,000 $8,000

0% 2% 4% 6% 8% 10% 12% 14% 16% 18% 20% 22% 24% 26% 28% 30% 32% 34% 36% 38% 40% 42% 44% 46%
The IRR suggests..

- **The project is a good one.** Using time-weighted, incremental cash flows, this project provides a return of 15.32%. This is greater than the cost of capital of 12.32%.

- The IRR and the NPV will yield **similar results** most of the time, though there are differences between the two approaches that may cause project rankings to vary depending upon the approach used.
Case 1: IRR versus NPV

- Consider a project with the following cash flows:

<table>
<thead>
<tr>
<th>Year</th>
<th>Cash Flow</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>-1000</td>
</tr>
<tr>
<td>1</td>
<td>800</td>
</tr>
<tr>
<td>2</td>
<td>1000</td>
</tr>
<tr>
<td>3</td>
<td>1300</td>
</tr>
<tr>
<td>4</td>
<td>-2200</td>
</tr>
</tbody>
</table>
Project’s NPV Profile
What do we do now?

- This project has two internal rates of return. The first is 6.60%, whereas the second is 36.55%.
- Why are there two internal rates of return on this project?

- If your cost of capital is 12.32%, would you accept or reject this project?
  - I would reject the project
  - I would accept this project

Explain.
## Case 2: NPV versus IRR

### Project A

<table>
<thead>
<tr>
<th>Cash Flow</th>
<th>$350,000</th>
<th>$450,000</th>
<th>$600,000</th>
<th>$750,000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Investment</td>
<td>$1,000,000</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

NPV = $467,937  
IRR = 33.66%

### Project B

<table>
<thead>
<tr>
<th>Cash Flow</th>
<th>$3,000,000</th>
<th>$3,500,000</th>
<th>$4,500,000</th>
<th>$5,500,000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Investment</td>
<td>$10,000,000</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

NPV = $1,358,664  
IRR = 20.88%
Which one would you pick?

Assume that you can pick only one of these two projects. Your choice will clearly vary depending upon whether you look at NPV or IRR. You have enough money currently on hand to take either. Which one would you pick?

- Project A. It gives me the bigger bang for the buck and more margin for error.
- Project B. It creates more dollar value in my business.

If you pick A, what would your biggest concern be?

If you pick B, what would your biggest concern be?
Capital Rationing, Uncertainty and Choosing a Rule

- If a business has limited access to capital, has a stream of surplus value projects and faces more uncertainty in its project cash flows, it is much more likely to use IRR as its decision rule.

  Small, high-growth companies and private businesses are much more likely to use IRR.

- If a business has substantial funds on hand, access to capital, limited surplus value projects, and more certainty on its project cash flows, it is much more likely to use NPV as its decision rule.

  As firms go public and grow, they are much more likely to gain from using NPV.
An Alternative to IRR with Capital Rationing

- The problem with the NPV rule, when there is capital rationing, is that it is a dollar value. It measures success in absolute terms.
- The NPV can be converted into a relative measure by dividing by the initial investment. This is called the profitability index.
  - Profitability Index (PI) = NPV/Initial Investment
- In the example described, the PI of the two projects would have been:
  - PI of Project A = $467,937/1,000,000 = 46.79%
  - PI of Project B = $1,358,664/10,000,000 = 13.59%
Project A would have scored higher.
Case 3: NPV versus IRR

**Project A**

<table>
<thead>
<tr>
<th>Cash Flow</th>
<th>$5,000,000</th>
<th>$4,000,000</th>
<th>$3,200,000</th>
<th>$3,000,000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Investment</td>
<td>$10,000,000</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

NPV = $1,191,712
IRR = 21.41%

**Project B**

<table>
<thead>
<tr>
<th>Cash Flow</th>
<th>$3,000,000</th>
<th>$3,500,000</th>
<th>$4,500,000</th>
<th>$5,500,000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Investment</td>
<td>$10,000,000</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

NPV = $1,358,664
IRR = 20.88%
Why the difference?

These projects are of the same scale. Both the NPV and IRR use time-weighted cash flows. Yet, the rankings are different. Why?

Which one would you pick?
- Project A. It gives me the bigger bang for the buck and more margin for error.
- Project B. It creates more dollar value in my business.
NPV, IRR and the Reinvestment Rate Assumption

- The NPV rule assumes that intermediate cash flows on the project get reinvested at the hurdle rate (which is based upon what projects of comparable risk should earn).
- The IRR rule assumes that intermediate cash flows on the project get reinvested at the IRR. Implicit is the assumption that the firm has an infinite stream of projects yielding similar IRRs.
- Conclusion: When the IRR is high (the project is creating significant surplus value) and the project life is long, the IRR will overstate the true return on the project.
Solution to Reinvestment Rate Problem

Cash Flow

<table>
<thead>
<tr>
<th>Year</th>
<th>Cash Flow</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$300</td>
</tr>
<tr>
<td>1</td>
<td>$400</td>
</tr>
<tr>
<td>2</td>
<td>$500</td>
</tr>
<tr>
<td>3</td>
<td>$600</td>
</tr>
</tbody>
</table>

Investment <$1000>

<table>
<thead>
<tr>
<th>Year</th>
<th>Investment</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$300(1.15)</td>
</tr>
<tr>
<td>1</td>
<td>$400(1.15^2)</td>
</tr>
<tr>
<td>2</td>
<td>$500(1.15^3)</td>
</tr>
<tr>
<td>3</td>
<td>$600</td>
</tr>
</tbody>
</table>

Terminal Value = $2160

Internal Rate of Return = 24.89%
Modified Internal Rate of Return = 21.23%
Why NPV and IRR may differ..

- A project can have only one NPV, whereas it can have more than one IRR.
- The NPV is a dollar surplus value, whereas the IRR is a percentage measure of return. The NPV is therefore likely to be larger for “large scale” projects, while the IRR is higher for “small-scale” projects.
- The NPV assumes that intermediate cash flows get reinvested at the “hurdle rate”, which is based upon what you can make on investments of comparable risk, while the IRR assumes that intermediate cash flows get reinvested at the “IRR”.
Case: NPV and Project Life

Project A

- $1000

NPV of Project A = $ 442

$400 $400 $400 $400 $400

Project B

- $1500

NPV of Project B = $ 478

NPV of Project A = $ 442

Hurdle Rate for Both Projects = 12%
Choosing Between Mutually Exclusive Projects

- The net present values of mutually exclusive projects with different lives cannot be compared, since there is a bias towards longer-life projects.
- To do the comparison, we have to
  - replicate the projects till they have the same life (or)
  - convert the net present values into annuities
Solution 1: Project Replication

Project A: Replicated

\[\begin{array}{cccccccccc}
\$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 \\
-\$1000 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 & \$400 \\
\end{array}\]

NPV of Project A replicated = $693

Project B

\[\begin{array}{cccccccccc}
\$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 \\
-\$1500 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 & \$350 \\
\end{array}\]

NPV of Project B = $478
Solution 2: Equivalent Annuities

- Equivalent Annuity for 5-year project
  \[ = 442 \times PV(A,12\%,5 \text{ years}) \]
  \[ = 122.62 \]

- Equivalent Annuity for 10-year project
  \[ = 478 \times PV(A,12\%,10 \text{ years}) \]
  \[ = 84.60 \]
What would you choose as your investment tool?

- Given the advantages/disadvantages outlined for each of the different decision rules, which one would you choose to adopt?
  - Return on Investment (ROE, ROA)
  - Payback or Discounted Payback
  - Net Present Value
  - Internal Rate of Return
  - Profitability Index
## What firms actually use ..

<table>
<thead>
<tr>
<th>Decision Rule</th>
<th>% of Firms using as primary decision rule in</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1976</td>
</tr>
<tr>
<td>IRR</td>
<td>53.6%</td>
</tr>
<tr>
<td>Accounting Return</td>
<td>25.0%</td>
</tr>
<tr>
<td>NPV</td>
<td>9.8%</td>
</tr>
<tr>
<td>Payback Period</td>
<td>8.9%</td>
</tr>
<tr>
<td>Profitability Index</td>
<td>2.7%</td>
</tr>
</tbody>
</table>
The cash flows on the Bangkok Disney park will be in Thai Baht. This will expose Disney to exchange rate risk. In addition, there are political and economic risks to consider in an investment in Thailand. The discount rate of 12.32% that we used is a cost of capital for U.S. theme parks. Would you use a higher rate for this project?

- Yes
- No
Should there be a risk premium for foreign projects?

- The exchange rate risk may be diversifiable risk (and hence should not command a premium) if
  - the company has projects in a large number of countries (or)
  - the investors in the company are globally diversified.
  
  For Disney, this risk should not affect the cost of capital used.

- The same diversification argument can also be applied against political risk, which would mean that it too should not affect the discount rate. It may, however, affect the cash flows, by reducing the expected life or cash flows on the project.

  For Disney, this risk too is assumed to not affect the cost of capital.
Domestic versus international expansion

- The analysis was done in dollars. Would the conclusions have been any different if we had done the analysis in Thai Baht?
  - Yes
  - No
The “Consistency Rule” for Cash Flows

- The cash flows on a project and the discount rate used should be defined in the same terms.
  - If cash flows are in dollars (baht), the discount rate has to be a dollar (baht) discount rate
  - If the cash flows are nominal (real), the discount rate has to be nominal (real).

- If consistency is maintained, the project conclusions should be identical, no matter what cash flows are used.
The inflation rates were assumed to be 15% in Thailand and 3% in the United States. The Baht/dollar rate at the time of the analysis was 35 BT/dollar.

The expected exchange rate was derived assuming purchasing power parity.

\[
\text{Expected Exchange Rate}_t = \text{Exchange Rate today} \times \left( \frac{1.15}{1.03} \right)^t
\]

The expected growth rate after year 9 is still expected to be the inflation rate, but it is the 15% Thai inflation rate.

The cost of capital in Baht was derived from the cost of capital in dollars and the differences in inflation rates:

\[
\text{Baht Cost of Capital} = \text{\$ Cost of Capital} \times \left( \frac{1.15}{1.03} \right) = 12.32\% \left( \frac{1.15}{1.03} \right) = 25.41\%
\]
Disney Theme Park: The Baht NPV

<table>
<thead>
<tr>
<th>Year</th>
<th>$ Cash Flows</th>
<th>Exchange Rate</th>
<th>BT Cash Flows</th>
<th>Terminal Value</th>
<th>Total FCFF</th>
<th>PV of FCFF</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>($2,000.00)</td>
<td>35.00</td>
<td>($70,000 Bt)</td>
<td>($70,000 Bt)</td>
<td>($70,000 Bt)</td>
<td>(70,000 Bt)</td>
</tr>
<tr>
<td>1</td>
<td>($890.31)</td>
<td>39.08</td>
<td>($39,078 Bt)</td>
<td>($39,078 Bt)</td>
<td>($39,078 Bt)</td>
<td>(31,161 Bt)</td>
</tr>
<tr>
<td>2</td>
<td>($657.64)</td>
<td>43.63</td>
<td>($36,199 Bt)</td>
<td>($36,199 Bt)</td>
<td>($36,199 Bt)</td>
<td>(23,017 Bt)</td>
</tr>
<tr>
<td>3</td>
<td>($170.35)</td>
<td>48.71</td>
<td>($11,759 Bt)</td>
<td>($11,759 Bt)</td>
<td>($11,759 Bt)</td>
<td>(5,962 Bt)</td>
</tr>
<tr>
<td>4</td>
<td>186.63</td>
<td>54.39</td>
<td>16,155 Bt</td>
<td></td>
<td>16,155 Bt</td>
<td>6,532 Bt</td>
</tr>
<tr>
<td>5</td>
<td>198.49</td>
<td>60.73</td>
<td>21,548 Bt</td>
<td></td>
<td>21,548 Bt</td>
<td>6,947 Bt</td>
</tr>
<tr>
<td>6</td>
<td>243.21</td>
<td>67.80</td>
<td>33,109 Bt</td>
<td></td>
<td>33,109 Bt</td>
<td>8,512 Bt</td>
</tr>
<tr>
<td>7</td>
<td>273.49</td>
<td>75.70</td>
<td>46,692 Bt</td>
<td></td>
<td>46,692 Bt</td>
<td>9,572 Bt</td>
</tr>
<tr>
<td>8</td>
<td>271.69</td>
<td>84.52</td>
<td>58,169 Bt</td>
<td></td>
<td>58,169 Bt</td>
<td>9,509 Bt</td>
</tr>
<tr>
<td>9</td>
<td>746.27</td>
<td>94.37</td>
<td>70,423 Bt</td>
<td>832,421 Bt</td>
<td>902,843 Bt</td>
<td>117,694 Bt</td>
</tr>
<tr>
<td>NPV</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>28,626 Bt</td>
<td></td>
</tr>
</tbody>
</table>

NPV = 28,626 Bt/35 Bt = $ 818 Million

NPV is equal to NPV in dollar terms
Dealing with Inflation

- In our analysis, we used nominal dollars and Bt. Would the NPV have been different if we had used real cash flows instead of nominal cash flows?
  - It would be much lower, since real cash flows are lower than nominal cash flows
  - It would be much higher
  - It should be unaffected
Disney Theme Park

- The nominal cash flows in Bt are deflated first at the inflation rate:
  - Real Cash Flows\(_t\) = Nominal Cash Flow\(_t\)/(1+\text{Inflation Rate})^t

- The real cost of capital is obtained by deflating the nominal discount rate at the inflation rate.
  - Real Cost of Capital = \((1+\text{Nominal Cost of Capital})/(1+\text{Inflation Rate}) - 1\)
  - For the theme park, this would be:
    Real Cost of Capital = \(1.25411/1.15 - 1 = 9.05\%\)
# Disney Theme Park: Real NPV

<table>
<thead>
<tr>
<th>Year</th>
<th>Nominal CF (Bt)</th>
<th>Real CF</th>
<th>PV at</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>(70,000 Bt)</td>
<td>(70,000 Bt)</td>
<td>(70,000 Bt)</td>
</tr>
<tr>
<td>1</td>
<td>(39,078 Bt)</td>
<td>(33,981 Bt)</td>
<td>(31,161 Bt)</td>
</tr>
<tr>
<td>2</td>
<td>(36,199 Bt)</td>
<td>(27,371 Bt)</td>
<td>(23,017 Bt)</td>
</tr>
<tr>
<td>3</td>
<td>(11,759 Bt)</td>
<td>(7,731 Bt)</td>
<td>(5,962 Bt)</td>
</tr>
<tr>
<td>4</td>
<td>16,155 Bt</td>
<td>9,237 Bt</td>
<td>6,532 Bt</td>
</tr>
<tr>
<td>5</td>
<td>21,548 Bt</td>
<td>10,713 Bt</td>
<td>6,947 Bt</td>
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<tr>
<td>6</td>
<td>33,109 Bt</td>
<td>14,314 Bt</td>
<td>8,512 Bt</td>
</tr>
<tr>
<td>7</td>
<td>46,692 Bt</td>
<td>17,553 Bt</td>
<td>9,572 Bt</td>
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<td>58,169 Bt</td>
<td>19,015 Bt</td>
<td>9,509 Bt</td>
</tr>
<tr>
<td>9</td>
<td>902,843 Bt</td>
<td>256,644 Bt</td>
<td>117,694 Bt</td>
</tr>
</tbody>
</table>

**NPV of Project = 28,626 Bt**
The investment analysis can be done entirely in equity terms, as well. The returns, cashflows and hurdle rates will all be defined from the perspective of equity investors.

If using accounting returns,
  - Return will be Return on Equity (ROE) = Net Income/BV of Equity
  - ROE has to be greater than cost of equity

If using discounted cashflow models,
  - Cashflows will be cashflows after debt payments to equity investors
  - Hurdle rate will be cost of equity
A Brief Example: A Paper Plant for Aracruz - Investment Assumptions

The plant is expected to have a capacity of 750,000 tons and will have the following characteristics:

- It will require an initial investment of 250 Million BR. At the end of the fifth year, an additional investment of 50 Million BR will be needed to update the plant.
- Aracruz plans to borrow 100 Million BR, at a real interest rate of 5.5%, using a 10-year term loan (where the loan will be paid off in equal annual increments).
- The plant will have a life of 10 years. During that period, the plant (and the additional investment in year 5) will be depreciated using double declining balance depreciation, with a life of 10 years.
Operating Assumptions

- The plant will be partly in commission in a couple of months, but will have a capacity of only 650,000 tons in the first year, 700,000 tons in the second year before getting to its full capacity of 750,000 tons in the third year.
- The capacity utilization rate will be 90% for the first 3 years, and rise to 95% after that.
- The price per ton of linerboard is currently $400, and is expected to keep pace with inflation for the life of the plant.
- The variable cost of production, primarily labor and material, is expected to be 55% of total revenues; there is a fixed cost of 50 Million BR, which will grow at the inflation rate.
- The working capital requirements are estimated to be 15% of total revenues, and the investments have to be made at the beginning of each year.
Assumptions about Salvage

- At the end of the tenth year, the plant is expected to be salvaged at book value.
- At the end of the tenth year, it is anticipated that the entire working capital will be salvaged.
The Hurdle Rate

- The analysis is done in real, equity terms. Thus, the hurdle rate has to be a real cost of equity
- The real cost of equity for Aracruz, based upon
  - the beta estimate of 0.71,
  - the real riskless rate of 5% (using the real growth rate in Brazil as proxy)
  - and the risk premium for Brazil of 7.5% (based upon country rating spread over U.S premium of 5.5%)

  \[
  \text{Real Cost of Equity} = 5\% + 0.71 \times (7.5\%) = 10.33\%
  \]
### A ROE Analysis

<table>
<thead>
<tr>
<th>Year</th>
<th>Net Income</th>
<th>Depreciation</th>
<th>Cap Exp</th>
<th>Ending BV: Assets</th>
<th>Debt</th>
<th>BV: Equity</th>
<th>Avge BV</th>
<th>ROE</th>
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</thead>
<tbody>
<tr>
<td>0</td>
<td>0 BR</td>
<td>0 BR</td>
<td>250,000 BR</td>
<td>250,000 BR</td>
<td>100,000 BR</td>
<td>150,000 BR</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>(1,289 BR)</td>
<td>50,000 BR</td>
<td>0 BR</td>
<td>200,000 BR</td>
<td>92,233 BR</td>
<td>107,767 BR</td>
<td>128,883 BR</td>
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<td>2</td>
<td>7,371 BR</td>
<td>40,000 BR</td>
<td>0 BR</td>
<td>160,000 BR</td>
<td>84,039 BR</td>
<td>75,961 BR</td>
<td>91,864 BR</td>
<td>8.02%</td>
</tr>
<tr>
<td>3</td>
<td>15,122 BR</td>
<td>32,000 BR</td>
<td>0 BR</td>
<td>128,000 BR</td>
<td>75,395 BR</td>
<td>52,605 BR</td>
<td>64,283 BR</td>
<td>23.52%</td>
</tr>
<tr>
<td>4</td>
<td>21,526 BR</td>
<td>25,600 BR</td>
<td>0 BR</td>
<td>102,400 BR</td>
<td>66,275 BR</td>
<td>36,125 BR</td>
<td>44,365 BR</td>
<td>48.52%</td>
</tr>
<tr>
<td>5</td>
<td>24,234 BR</td>
<td>20,480 BR</td>
<td>50,000 BR</td>
<td>131,920 BR</td>
<td>56,653 BR</td>
<td>75,267 BR</td>
<td>55,696 BR</td>
<td>43.51%</td>
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<td>6</td>
<td>21,864 BR</td>
<td>26,384 BR</td>
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<td>105,536 BR</td>
<td>46,502 BR</td>
<td>59,034 BR</td>
<td>67,151 BR</td>
<td>32.56%</td>
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<tr>
<td>7</td>
<td>24,684 BR</td>
<td>21,107 BR</td>
<td>0 BR</td>
<td>84,429 BR</td>
<td>35,793 BR</td>
<td>48,636 BR</td>
<td>53,835 BR</td>
<td>45.85%</td>
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<td>8</td>
<td>27,036 BR</td>
<td>16,886 BR</td>
<td>0 BR</td>
<td>67,543 BR</td>
<td>24,495 BR</td>
<td>43,048 BR</td>
<td>45,842 BR</td>
<td>58.98%</td>
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<td>9</td>
<td>29,020 BR</td>
<td>13,509 BR</td>
<td>0 BR</td>
<td>54,034 BR</td>
<td>12,575 BR</td>
<td>41,459 BR</td>
<td>42,254 BR</td>
<td>68.68%</td>
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<tr>
<td>10</td>
<td>30,715 BR</td>
<td>10,807 BR</td>
<td>0 BR</td>
<td>43,228 BR</td>
<td>(0 BR)</td>
<td>43,228 BR</td>
<td>42,343 BR</td>
<td>72.54%</td>
</tr>
</tbody>
</table>

Real ROE of 40.12% is greater than
Real Cost of Equity of 10.33%
As with the earlier analysis, where we used return on capital and cost of capital to measure the overall quality of projects at Disney, we can compute return on equity and cost of equity at Aracruz to pass judgment on whether Aracruz is creating value to its equity investors.

In 1996, Aracruz had net income of 47 million BR on book value of equity of 2,115 million BR, yielding a return on equity of:

\[
ROE = \frac{47}{2115} = 2.22\% \text{ (Real because book value is inflation adjusted)}
\]

Cost of Equity = 10.33%

Excess Return = 2.22\% - 10.33\% = -8.11\%

This can be converted into a dollar value by multiplying by the book value of equity, to yield an equity economic value added:

\[
\text{Equity EVA} = (2.22\% - 10.33\%) \times (2,115 \text{ Million}) = -171 \text{ Million BR}
\]
An Incremental CF Analysis

<table>
<thead>
<tr>
<th>Year</th>
<th>FCFE</th>
<th>PV of FCFE (at 10.33%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>(185,100 BR)</td>
<td>(185,100 BR)</td>
</tr>
<tr>
<td>1</td>
<td>38,244 BR</td>
<td>34,663 BR</td>
</tr>
<tr>
<td>2</td>
<td>36,477 BR</td>
<td>29,966 BR</td>
</tr>
<tr>
<td>3</td>
<td>36,227 BR</td>
<td>26,974 BR</td>
</tr>
<tr>
<td>4</td>
<td>38,006 BR</td>
<td>25,649 BR</td>
</tr>
<tr>
<td>5</td>
<td>(14,907 BR)</td>
<td>(9,119 BR)</td>
</tr>
<tr>
<td>6</td>
<td>38,097 BR</td>
<td>21,122 BR</td>
</tr>
<tr>
<td>7</td>
<td>35,082 BR</td>
<td>17,629 BR</td>
</tr>
<tr>
<td>8</td>
<td>32,624 BR</td>
<td>14,859 BR</td>
</tr>
<tr>
<td>9</td>
<td>30,609 BR</td>
<td>12,636 BR</td>
</tr>
<tr>
<td>10</td>
<td>114,925 BR</td>
<td>43,001 BR</td>
</tr>
<tr>
<td>NPV</td>
<td></td>
<td>32,280 BR</td>
</tr>
</tbody>
</table>
The Role of Sensitivity Analysis

- Our conclusions on a project are clearly conditioned on a large number of assumptions about revenues, costs and other variables over very long time periods.
- To the degree that these assumptions are wrong, our conclusions can also be wrong.
- One way to gain confidence in the conclusions is to check to see how sensitive the decision measure (NPV, IRR..) is to changes in key assumptions.
Viability of Paper Plant: Sensitivity to Price per Ton

Aracruz: NPV versus Price per Ton

Price per Ton

NPV

300 325 350 375 400 425 450 475 500

-60,000 -40,000 -20,000 0 20,000 40,000 60,000 80,000 100,000 120,000
What does sensitivity analysis tell us?

Assume that the manager at Aracruz who has to decide on whether to take this plant is very conservative. She looks at the sensitivity analysis and decides not to take the project because the NPV would turn negative if the price drops below $360 per ton. (Though the expected price per ton is $400, there is a significant probability of the price dropping below $360.) Is this the right thing to do?

- Yes
- No

Explain.
Most projects considered by any business create side costs and benefits for that business.

The side costs include the costs created by the use of resources that the business already owns (opportunity costs) and lost revenues for other projects that the firm may have.

The benefits that may not be captured in the traditional capital budgeting analysis include project synergies (where cash flow benefits may accrue to other projects) and options embedded in projects (including the options to delay, expand or abandon a project).

The returns on a project should incorporate these costs and benefits.
Opportunity Cost

- An opportunity cost arises when a project uses a resource that may already have been paid for by the firm.
- When a resource that is already owned by a firm is being considered for use in a project, this resource has to be priced on its next best alternative use, which may be
  - a sale of the asset, in which case the opportunity cost is the expected proceeds from the sale, net of any capital gains taxes
  - renting or leasing the asset out, in which case the opportunity cost is the expected present value of the after-tax rental or lease revenues.
  - use elsewhere in the business, in which case the opportunity cost is the cost of replacing it.
Case 1: Opportunity Costs

Assume that Disney owns land in Bangkok already. This land is undeveloped and was acquired several years ago for $5 million for a hotel that was never built. It is anticipated, if this theme park is built, that this land will be used to build the offices for Disney Bangkok. The land currently can be sold for $40 million, though that would create a capital gain (which will be taxed at 20%). In assessing the theme park, which of the following would you do:

- Ignore the cost of the land, since Disney owns its already
- Use the book value of the land, which is $5 million
- Use the market value of the land, which is $40 million
- Other:
Case 2: Excess Capacity

- In the Aracruz example, assume that the firm will use its existing distribution system to service the production out of the new paper plant. The new plant manager argues that there is no cost associated with using this system, since it has been paid for already and cannot be sold or leased to a competitor (and thus has no competing current use). Do you agree?
  - Yes
  - No
Estimating the Cost of Excess Capacity

- Existing Capacity = 100,000 units
- Current Usage = 50,000 (50% of Capacity); 50% Excess Capacity;
- New Product will use 30% of Capacity; Sales growth at 5% a year; CM per unit = $5/unit
- Book Value = $1,000,000 Cost of a building new capacity = $1,500,000 Cost of Capital = 12%
- Current product sales growing at 10% a year. CM per unit = $4/unit

- Basic Framework
  - If I do not take this product, when will I run out of capacity?
  - If I take this project, when will I run out of capacity
  - When I run out of capacity, what will I do?
    - cut back on production: cost is PV of after-tax cash flows from lost sales
    - buy new capacity: cost is difference in PV between earlier & later investment
## Opportunity Cost of Excess Capacity

<table>
<thead>
<tr>
<th>Year</th>
<th>Old</th>
<th>New</th>
<th>Old + New</th>
<th>Lost ATCF</th>
<th>PV(ATCF)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>50.00%</td>
<td>30.00%</td>
<td>80.00%</td>
<td>$0</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>55.00%</td>
<td>31.50%</td>
<td>86.50%</td>
<td>$0</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>60.50%</td>
<td>33.08%</td>
<td>93.58%</td>
<td>$0</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>66.55%</td>
<td>34.73%</td>
<td>101.28%</td>
<td>$5,115</td>
<td>$3,251</td>
</tr>
<tr>
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<td>73.21%</td>
<td>36.47%</td>
<td>109.67%</td>
<td>$38,681</td>
<td>$21,949</td>
</tr>
<tr>
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<td>80.53%</td>
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<td>118.81%</td>
<td>$75,256</td>
<td>$38,127</td>
</tr>
<tr>
<td>7</td>
<td>88.58%</td>
<td>40.20%</td>
<td>128.78%</td>
<td>$115,124</td>
<td>$52,076</td>
</tr>
<tr>
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<td>97.44%</td>
<td>42.21%</td>
<td>139.65%</td>
<td>$158,595</td>
<td>$64,054</td>
</tr>
<tr>
<td>9</td>
<td>107.18%</td>
<td>44.32%</td>
<td>151.50%</td>
<td>$206,000</td>
<td>$74,286</td>
</tr>
<tr>
<td>10</td>
<td>117.90%</td>
<td>46.54%</td>
<td>164.44%</td>
<td>$257,760</td>
<td>$82,992</td>
</tr>
</tbody>
</table>

PV(LOST SALES) = $336,734

- PV (Building Capacity In Year 3 Instead Of Year 8) = $1,500,000/1.12³ - $1,500,000/1.12⁸ = $461,846
- Opportunity Cost of Excess Capacity = $336,734
Costs for Other Projects

- Projects often create side-costs for other projects. The key question that has to be asked then is: Is this an incremental cost, as a result of the project, or would it have occurred anyway?
- If it is an incremental cost, it should be considered in project analysis. If it would have occurred anyway, it should be ignored.
Product and Project Cannibalization: A Real Cost?

Assume that in the Disney theme park example, 20% of the revenues at the Bangkok Disney park are expected to come from people who would have gone to Disneyland in Anaheim, California. In doing the analysis of the park, would you

- Look at only incremental revenues (i.e. 80% of the total revenue)
- Look at total revenues at the park
- Choose an intermediate number

Would your answer be different if you were analyzing whether to introduce a new show on the Disney cable channel on Saturday mornings that is expected to attract 20% of its viewers from ABC (which is also owned by Disney)?

- Yes
- No
A project may provide benefits for other projects within the firm. If this is the case, these benefits have to be valued and shown in the initial project analysis.

Consider, for instance, a typical Disney animated movie. Assume that it costs $50 million to produce and promote. This movie, in addition to theatrical revenues, also produces revenues from

- the sale of merchandise (stuffed toys, plastic figures, clothes ..)
- increased attendance at the theme parks
- stage shows (see “Beauty and the Beast” and the “Lion King”)
- television series based upon the movie
One of the limitations of traditional investment analysis is that it is static and does not do a good job of capturing the options embedded in investment.

- The first of these options is the option to delay taking a project, when a firm has exclusive rights to it, until a later date.
- The second of these options is taking one project may allow us to take advantage of other opportunities (projects) in the future.
- The last option that is embedded in projects is the option to abandon a project, if the cash flows do not measure up.

These options all add value to projects and may make a “bad” project (from traditional analysis) into a good one.
The Option to Delay

- When a firm has exclusive rights to a project or product for a specific period, it can delay taking this project or product until a later date.
- A traditional investment analysis just answers the question of whether the project is a “good” one if taken today.
- Thus, the fact that a project does not pass muster today (because its NPV is negative, or its IRR is less than its hurdle rate) does not mean that the rights to this project are not valuable.
Valuing the Option to Delay a Project

Present Value of Expected Cash Flows on Product

PV of Cash Flows from Project

Initial Investment in Project

Project has negative NPV in this section

Project's NPV turns positive in this section

Present Value of Expected Cash Flows on Product
Insights for Investment Analyses

- Having the exclusive rights to a product or project is valuable, even if the product or project is not viable today.
- The value of these rights increases with the volatility of the underlying business.
- The cost of acquiring these rights (by buying them or spending money on development - R&D, for instance) has to be weighed off against these benefits.
The Option to Expand/Take Other Projects

- Taking a project today may allow a firm to consider and take other valuable projects in the future.
- Thus, even though a project may have a negative NPV, it may be a project worth taking if the option it provides the firm (to take other projects in the future) provides a more-than-compensating value.
- These are the options that firms often call “strategic options” and use as a rationale for taking on “negative NPV” or even “negative return” projects.
The Option to Expand

PV of Cash Flows from Expansion

Additional Investment to Expand

Present Value of Expected Cash Flows on Expansion

Firm will not expand in this section

Expansion becomes attractive in this section
An Example of an Expansion Option

- Disney is considering investing $100 million to create a Spanish version of the Disney channel to serve the growing Mexican market.

- A financial analysis of the cash flows from this investment suggests that the present value of the cash flows from this investment to Disney will be only $80 million. Thus, by itself, the new channel has a negative NPV of $20 million.

- If the market in Mexico turns out to be more lucrative than currently anticipated, Disney could expand its reach to all of Latin America with an additional investment of $150 million any time over the next 10 years. While the current expectation is that the cash flows from having a Disney channel in Latin America is only $100 million, there is considerable uncertainty about both the potential for such an channel and the shape of the market itself, leading to significant variance in this estimate.
Valuing the Expansion Option

- Value of the Underlying Asset (S) = PV of Cash Flows from Expansion to Latin America, if done now = $100 Million
- Strike Price (K) = Cost of Expansion into Latin American = $150 Million
- We estimate the variance in the estimate of the project value by using the annualized variance in firm value of publicly traded entertainment firms in the Latin American markets, which is approximately 10%.
  - Variance in Underlying Asset’s Value = 0.10
- Time to expiration = Period for which expansion option applies = 10 years
  
  \[
  \text{Call Value} = 100 \times (0.7915) - 150 \times \exp(-0.065)(10) \times (0.3400) = $52.5 \text{ Million}
  \]
Considering the Project with Expansion Option

- NPV of Disney Channel in Mexico = $80 Million - $100 Million = - $20 Million
- Value of Option to Expand = $52.5 Million
- NPV of Project with option to expand
  = - $20 million + $52.5 million
  = $32.5 million
- Take the project
A firm may sometimes have the option to abandon a project, if the cash flows do not measure up to expectations. If abandoning the project allows the firm to save itself from further losses, this option can make a project more valuable.
Valuing the Option to Abandon

- Disney is considering taking a 25-year project which
  - requires an initial investment of $250 million in an real estate partnership to develop time share properties with a South Florida real estate developer,
  - has a present value of expected cash flows is $254 million.

- While the net present value of $4 million is small, assume that Disney has the option to abandon this project anytime by selling its share back to the developer in the next 5 years for $150 million.

- A simulation of the cash flows on this time share investment yields a variance in the present value of the cash flows from being in the partnership is 0.09.
Project with Option to Abandon

- Value of the Underlying Asset \( (S) \) = PV of Cash Flows from Project = $254 million
- Strike Price \( (K) \) = Salvage Value from Abandonment = $150 million
- Variance in Underlying Asset’s Value = 0.09
- Time to expiration = Life of the Project = 5 years
- Dividend Yield = \( 1 / \text{Life of the Project} \) = \( 1 / 25 \) = 0.04 (We are assuming that the project’s present value will drop by roughly \( 1/n \) each year into the project)
- Assume that the five-year riskless rate is 7%. The value of the put option can be estimated as follows:
Should Disney take this project?

- Call Value = $110.12 million
- Put Value = $7.86 million

The value of this abandonment option has to be added on to the net present value of the project of $4 million, yielding a total net present value with the abandonment option of $11.86 million.
Invest in projects that **yield a return** greater than the minimum acceptable hurdle rate.

- The hurdle rate should be higher for riskier projects and reflect the financing mix used - owners’ funds (equity) or borrowed money (debt).
- **Returns on projects should be measured based on cash flows generated and the timing of these cash flows; they should also consider both positive and negative side effects of these projects.**

Choose a financing mix that minimizes the hurdle rate and matches the assets being financed.

If there are not enough investments that earn the hurdle rate, return the cash to stockholders.

- The form of returns - dividends and stock buybacks - will depend upon the stockholders’ characteristics.