Leasing and Secondary Markets:  
Theory and Evidence from Commercial Aircraft*

Alessandro Gavazza§

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Abstract

I construct a dynamic model of transactions in used capital to understand the role of leasing when trading is subject to frictions. Firms trade assets to adjust their productive capacity in response to shocks to profitability. Transaction costs hinder the efficiency of the allocation of capital, and lessors act as trading intermediaries who reduce trading frictions. The model predicts that leased assets trade more frequently and produce more output than owned assets, for two reasons. First, high-volatility firms are more likely to lease than low-volatility firms, since they expect to adjust their capacity more frequently. Second, ownership’s larger transaction costs widen owners’ inaction bands relative to lessees’.

Using data on commercial aircraft, I find that leased aircraft have holding durations 38-percent shorter and fly 6.5-percent more hours than owned aircraft. Additional tests indicate that most of these differential patterns in trading and utilization arise because owners have wider inaction bands than lessees, and carriers’ self-selection into leasing plays a minor role.

1 Introduction

In this paper, I study the link between the efficiency of secondary markets for firms’ inputs and the efficiency of production of final output, with a focus on the market for commercial aircraft and the airline industry. In particular, I study how a contract that has recently become popular in the aircraft market—the operating lease—increases the efficiency of aircraft transactions and, thus, capacity utilization in the airline industry.

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§Leonard N. Stern School of Business, New York University. 44 West 4th Street, New York, NY 10012. Telephone: (212) 998-0959. Fax: (212) 995-4218. Email: agavazza@stern.nyu.edu.
Several markets for used capital equipment are active. For example, more than two thirds of all machine tools sold in the United States in 1960 were used (Waterson, 1964), and more than half of the trucks traded in the United States in 1977 sold in secondary markets (Bond, 1983). Figure 1 plots the number of transactions in the primary and the secondary markets for commercial aircraft. Since the mid-1980s, trades in the secondary market for aircraft have grown steadily, and the number of transactions on used markets today is about three times the number of purchases of new aircraft.

A large share of these transactions is due to leasing. About one third of the aircraft currently operated by major carriers are under an operating lease, a rental contract between a lessor and an airline for use of the aircraft for a period of four to eight years (for more details on aircraft leasing, see Section 3 and Gavazza, 2010). Figure 2 plots the annual share of new commercial aircraft purchased by operating lessors, showing that lessors are active buyers on the primary market, and that their acquisitions have increased in recent years. Moreover, lessors also account for a large share of secondary-markets transactions, as they frequently buy used aircraft and lease them out several times during their useful lifetime.

In this paper, I construct a model of aircraft transactions to understand the role of lessors when trading is subject to frictions—i.e., transaction costs and search costs for potential buyers. The model combines five factors: 1) Carriers have heterogeneous stochastic productivity; 2) carriers have heterogeneous volatility; 3) aircraft can be bought or leased; 4) carriers incur costs to sell aircraft; and 5) lessors incur per-period costs of monitoring their assets.

In this world, secondary markets play a fundamental allocative role since carriers trade aircraft to
adjust their productive capacity. When either cost or demand shocks adversely affect profitability, carriers shrink and sell aircraft. Conversely, when shocks positively affect profitability, carriers expand and acquire aircraft.

If there is no leasing, trading frictions prevent capital goods from being efficiently allocated. Efficiency requires that only the most productive carriers operate aircraft. However, transaction costs create a wedge between the price the buyer pays and the price the seller receives. This wedge is a barrier to trade and implies that some carriers operating aircraft are less productive than some carriers not operating aircraft.

If carriers can buy or lease aircraft, they trade off ownership’s lower per-period rental rates and leasing’s lower transaction costs. This trade-off generates two differences between leased and owned aircraft in equilibrium: 1) Leased aircraft trade more frequently, due to two effects. The first is selection: High-volatility carriers lease and low-volatility carriers own aircraft. Since high-volatility carriers expect to adjust their capacity more frequently, they value leasing’s benefits more than low-volatility carriers do. The second is that, due to larger transaction costs, owners have wider inaction bands than lessees do. 2) Leased aircraft have higher utilization due to the same two effects. First, when acquiring aircraft, high-volatility carriers (i.e., lessees) are more productive than low-volatility carriers (i.e., owners). Second, owners’ wide inaction bands generate a long left tail in their productivity distribution. Instead, leasing’s lower trading frictions truncate the left tail of lessees’ productivity distribution.

I use data on commercial aircraft to provide evidence on the model’s qualitative implications.
I find that leased aircraft have: 1) holding durations 38-percent shorter than owned aircraft; and 2) flying hours 6.5-percent higher than owned aircraft. The empirical analysis shows that leased aircraft are parked inactive less frequently than owned aircraft, and that, conditional on being in use, leased aircraft have a higher capacity utilization than owned aircraft. Moreover, I find evidence in favor of both effects highlighted by the model, but their empirical relevance is lopsided: Most of the differential patterns in trading and utilization arise because owners have wider inaction bands than lessees, and carriers’ self-selection into leasing plays a minor role. Finally, I calibrate the model and show that it is quantitatively consistent with the data. The calibration highlights that small differences in carriers’ volatilities can lead to the observed larger differences in trading and utilization between leased and owned aircraft, confirming that carriers’ selection does not play a dominant role.

I argue that the growth of trade in the secondary markets for aircraft since the mid-1980s is consistent with the model. The Airline Deregulation Act of 1978 reduced entry costs, thereby increasing the competitiveness of airline markets.\footnote{The airline industry was governed by the Civil Aeronautics Board (CAB) from 1938 to 1984. Under the Airline Deregulation Act of 1978, the industry was deregulated in stages. In January 1, 1982, all controls on entry and exit were removed, while airfares were deregulated in January 1, 1983. The actual changes were implemented rather more rapidly. Finally, on January 1, 1985, the governance of the airline industry was transferred from the Civil Aeronautics Board to the Department of Transportation.} This increase in competitiveness amplified the volatility of firm-level output, implying that carriers needed to adjust their fleets more frequently. The volume of trade on secondary markets increased due to higher inter-firm reallocation of inputs. Therefore, the entry of lessors in the mid-1980s coincided with a period of trade expansion in secondary markets, when the need for market intermediaries to coordinate sellers and buyers became stronger.\footnote{Steven F. Udvar-Hazy, Chairman and CEO of ILFC, one of the largest aircraft lessors, declares: “The inevitability of change creates a constant flow of upswings and downturns in air transportation. But one thing does not change – the continuous need for rapid, economical deployment of high performance aircraft. ILFC understood this reality as early as 1973 when we pioneered the world’s first aircraft operating lease.” Available at \url{http://www.ilfc.com/ceo.htm}.} Variations of the operating lease have evolved, but the key point is that, when carriers want to shed excess capacity, the lessor takes over the job of finding a new operator. The logic is that specialists can do this job more efficiently, while carriers focus on operating the aircraft and servicing the passengers.

This paper identifies lessors as intermediaries who reduce frictions in secondary markets. Thus, I highlight a role for leasing in capital equipment that has been ignored in the literature. The mechanisms identified in this paper are not unique to aircraft markets, and may help clarify the role of leasing for a wide range of capital equipment. Frictions in secondary markets for capital goods are a key factor in determining an industry’s aggregate productivity growth or an industry’s speed.
of adjustment after a shock or a policy intervention. This paper is one of the few that empirically quantify the gains from institutions that enhance the efficiency of trading in these markets.

2 Related Literature

This paper is related to several strands of the literature. First, a series of papers studies the reallocation of capital across firms. These papers document the importance of gross capital flows in determining capital accumulation (Ramey and Shapiro, 1998); study the cyclical properties of reallocations (Eisfeldt and Rampini, 2006); or investigate some frictions in the capital reallocation process (Pulvino, 1998; Ramey and Shapiro, 2001; Eisfeldt and Rampini, 2006). However, none of these papers studies the role of leasing in alleviating frictions.

Second, a strand of the literature examines the corporate decisions to lease. Several papers focus on the tax advantages of leasing, following Miller and Upton (1976). However, as I discuss in detail in Section 6.1.4, taxes cannot explain all the empirical patterns documented in Section 5. Thus, the current paper contributes to a growing literature that shows that the economics of leasing go beyond tax-minimization strategies. In particular, following Smith and Wakeman (1985), a few authors have focused on some financial contracting aspects of leasing (see Krishnan and Moyer, 1994; Sharpe and Nguyen, 1995; Eisfeldt and Rampini, 2009; Gavazza, 2010). Particularly related to the current paper are Sharpe and Nguyen (1995) and Eisfeldt and Rampini (2009), both of which focus on firms’ decision to lease, showing that more-financially-constrained firms lease more of their capital than less-constrained firms do. Instead, I focus on leasing’s effects on trading and allocation of assets.

Third, the literature on consumer durable goods has investigated the role of secondary markets in allocating new and used goods (Rust, 1985; Anderson and Ginsburgh, 1994; Hendel and Lizzeri, 1999a). In these papers, the gains from trade arise from the depreciation of the durables, while in the current paper, the gains from trade arise from the stochastic evolution of firms’ efficiency (as in House and Leahy, 2004, which, however, does not consider the role of leasing). In this strand of the literature, Waldman (1997) and Hendel and Lizzeri (1999b, 2002) analyze manufacturers’ incentives to lease and show that leasing may allow manufacturers to gain market power in the used market. Hendel and Lizzeri (2002) and Johnson and Waldman (2003, 2010) show that manufacturers’ leasing ameliorates the consequences of information asymmetries about the quality of used goods. Gilligan (2004), using data on business jets, finds empirical evidence consistent with the theoretical results of Hendel and Lizzeri (2002) and Johnson and Waldman (2003). Further, Bulow (1982) shows that a
durable-goods monopolist prefers to lease in order to solve the Coasian time-inconsistency problem. Thus, the current paper differs from this strand of the literature by focusing on a novel role of leasing that, I argue, captures the main features of commercial aircraft markets.

Fourth, a series of papers has analyzed the passenger-airline industry. Most of the literature has analyzed carriers’ product market decisions (entry, scheduling of flights, pricing of tickets, etc.), and only a few papers have focused on aircraft transactions. Pulvino (1998) finds that airlines under financial pressure sell aircraft at a 14-percent discount. He further shows that distressed airlines experience higher rates of asset sales than non-distressed airlines do, which is consistent with the results of my model. Goolsbee (1998) studies how carriers’ financial performance, the business cycle, factor prices, and the cost of capital affect carriers’ decision to sell/retire a specific aircraft type, the Boeing 707. However, none of these papers considers the role of aircraft leasing.

3 Background: Aircraft Markets and Aircraft Leasing

3.1 Trading Frictions

The secondary market for aircraft is a single, worldwide market that is more active than the market for other capital equipment. Nonetheless, several facts suggest that trading frictions are important (see, also, Gavazza, 2010, forthcoming).

First, aircraft are traded in decentralized markets. Thus, no centralized exchange provides immediacy of trade and pre-trade price transparency. To initiate a transaction, sellers must contact multiple potential buyers. Comparing two similar aircraft for sale is costly since aircraft sales involve the inspection of the aircraft. In addition, a sale involves legal costs, which increase if there are legal disputes over the title or if the local aviation authority has deregistered the aircraft. Thus, aircraft are seldom sold at auctions. Pulvino (1998) reports that, in one of the first auctions, only nine of the 35 aircraft offered for sale were sold. Some subsequent auctions ended without even a single sale. Hence, aircraft markets share many features with other over-the-counter markets for financial assets (mortgage-backed securities, corporate bonds, bank loans, derivatives, etc.) and for real assets (real estate), in which trading involves material and opportunity costs (Duffie, Gärleanu and Pedersen, 2005). Therefore, most major carriers have staff devoted to the acquisition and disposition of aircraft, which indicates that trade is not frictionless.

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3 This is one characteristic that Rauch (1999) uses to measure asset-specificity. The idea is that if an asset is sold on an organized exchange, then the market for this asset is thick and, hence, the asset is less specific to the transaction.
Second, compared to financial markets and other equipment markets, the number of transactions is small. For example, in the 12 months between May 2002 and April 2003, of the total stock of 12,409 commercial aircraft used for passenger transportation and older than two years, only 720 (5.8 percent) traded. Moreover, aircraft are differentiated products. Each type of aircraft requires human-capital investments in specific skills—for pilots, crew and mechanics—that increase the degree of physical differentiation. Product differentiation also implies that aircraft are imperfect substitutes for one another, as different types are designed to serve different markets and ranges. For example, a Boeing 747 is suited to markets in which both demand and distance are large. For a given type, the number of annual transactions can be small: Only 21 used Boeing 747s traded in the 12-month period ending April 2003.

In thin markets, the search costs to find high-value buyers are large (Ramey and Shapiro, 2001). Industry experts and market participants consider these frictions a fundamental characteristic of aircraft markets. For example, according to Lehman Brothers (1998): “The ratings agencies require an 18-month source of liquidity because this is the length of time they feel it will take to market and resell the aircraft in order to maximize value.” Hence, transaction prices are sensitive to parties’ individual shocks. For example, Pulvino (1998) finds that sellers with bad financial status sell aircraft at a 14-percent discount relative to the average market price.

3.2 Lessors as Intermediaries

In response to trading frictions, almost all over-the-counter markets have intermediaries. In aircraft markets, operating lessors play the role of marketmakers/dealers, and a fringe of smaller companies operate as independent brokers. Habib and Johnsen (1999) describe the origin and nature of the leasing business as follows: “[Lessors] appear to have invested substantial resources through the 1980s and early 1990s to establish general knowledge of secondary market redeployment opportunities for used aircraft. They also appear to have invested, ex ante, to establish specific knowledge of redeployment opportunities for particular used aircraft.” In its 2003 Annual Report, ILFC—the founder of the aircraft-leasing business—describes its business as follows: “International Lease Finance Corporation is primarily engaged in the acquisition of new commercial jet aircraft and the leasing of those aircraft to airlines throughout the world. In addition to its leasing activity, the Company regularly sells aircraft from its leased aircraft fleet to third party lessors and airlines.” Similarly, AWAS, another operating lessor, states: “At AWAS we pride ourselves in our ability to optimise return on investment through the effective management and remarketing of our assets.”
3.3 The Trade-off between Leasing and Owning

If carriers are leasing an aircraft and no longer need it, the lessor takes over the job of finding a new operator. Leasing companies advertise this advantage to attract carriers. For example, GECAS cites the following benefits of an operating lease: “Fleet flexibility to introduce new routes or aircraft types” and “Flexibility to increase or reduce capacity quickly.” Similarly, AWAS mentions that “AWAS’ customers gain operating flexibility.”

Leasing companies have technical, legal and marketing teams that accumulate extensive knowledge of the market, keep track of carriers’ capacity needs, and also monitor the use of their aircraft. However, these “monitoring” costs, as in Eisfeldt and Rampini (2009) and Rampini and Viswanathan (2010), imply that per-period rates are higher on leased than on owned aircraft. Indeed, Gavazza (2010), using data on aircraft prices and aircraft lease rates, documents that lease rates are, on average, 20-percent higher than implicit rental rates.

Hence, carriers face a trade-off between leasing’s higher per-period costs and ownership’s higher transaction costs. For example, Barrington (1998) notes: “The airlines that use operating leases consider that the flexibility such leases provide makes up for the fact that the cash costs of the leases can be greater than the cost of acquiring the same aircraft through ownership.” Similarly, Morrell (2001) lists “no aircraft trading experience needed” as one of the advantages of leasing for the carriers, and “a higher cost than, say, debt finance for purchase” as one of the disadvantages.

3.4 Why Lessors own Aircraft

Having documented the role of lessors as trading intermediaries, the natural question to ask is why lessors do not trade aircraft as brokers/dealers. The answer combines two issues: 1) why aircraft owners are the intermediaries—i.e., what are the efficiency gains if intermediation is performed by the same firms that own aircraft? and 2) why carriers would rather not own aircraft—i.e., what are the efficiency gains if companies that are not carriers own aircraft?

First, in the event of default on a lease prior to bankruptcy, a lessor can seize the aircraft more easily than a secured lender can in both U.S. and non-U.S. bankruptcies (Krishnan and Moyer, 1994; Habib and Johnsen, 1999). In U.S.-based Chapter 7 bankruptcies and in most non-U.S. bankruptcies, a lessor can repossess the asset more rapidly than a debt holder can (Littlejohns and McGairl, 1998). In U.S.-based Chapter 11 bankruptcies, Section 1110 treats lessors and all other secured lenders

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4The model focuses on monitoring costs, but the exact reason why leasing per-period costs are higher is not critical.
equally in allowing foreclosure on an aircraft. However, the bankruptcy code establishes that other claims of secured creditors are more diluted than comparable claims of lessors. For example, in an interesting case, Continental Airlines sought to have over $100 million of its lease obligations treated as debt during its reorganization under Chapter 11 bankruptcy in 1991 (Krishnan and Moyer, 1994). The lessors did not agree, and the court ruled in their favor. Thus, since defaults and bankruptcies are frequent in the airline industry, leasing enhances the efficiency of redeployment by exploiting its stronger ability to repossess assets. Moreover, Eisfeldt and Rampini (2009) argue that leasing is particularly attractive to financially constrained operators. Such operators are often young, have volatile capacity needs, and are more likely to default on their leases. Hence, lessors frequently get aircraft returned, which leads them to further specialize in redeployment.

Second, Shleifer and Vishny (1992) note that “[t]he institution of airline leasing seems to be designed partly to avoid fire sales of assets.” Because the airline industry is highly cyclical, both airline profits and aircraft values carry large financial risk, and they are almost perfectly correlated. Leasing allows carriers to transfer some of the aircraft-ownership risk to operating lessors. The price discounts estimated by Pulvino (1998) show that even the idiosyncratic risk of aircraft ownership can be substantial. Lessors are better suited to assuming this risk through their knowledge of secondary markets, their scale economies, and their diversification of aircraft types and lessees operating in different geographic regions. Moreover, the largest lessors (GECAS and ILFC) belong to financial conglomerates, which allows them to diversify the aggregate risk of aircraft ownership and to have a lower cost of funds, thanks to a higher credit rating.

4 Model

In this section, I introduce a model that illustrates the effects of leasing on aircraft trading and utilization. The theoretical framework will guide the empirical analysis of Section 5. I discuss only the results of the model in the text, relegating the analytic details to Appendix B.

4.1 Setup

Time is continuous and the horizon infinite. All firms are risk-neutral and discount the future at rate \( r > 0 \).

Aircraft - There is a mass \( X < 1 \) of homogeneous capital goods, which I refer to as aircraft. For simplicity, aircraft do not depreciate. Aircraft can be bought or leased. The (endogenous) mass
\( X_L \in [0, X] \) of aircraft is leased, and the mass \( X - X_L \) is owned.

**Firms** - There are two types of firms, carriers and lessors. Carriers operate aircraft to produce flights, and lessors supply leased aircraft to carriers.

There is a unit mass of carriers, and I refer to the carriers collectively as the *industry*. Carriers are infinitesimal—i.e., each carrier can operate, at most, one aircraft. Carriers' instantaneous output \( y \) (and revenues, since the price of output is normalized to one) is given by \( y(z, s) = zs \), where the parameter \( z \) is a carrier’s “long-term” productivity, and the parameter \( s \) is a “short-term” shock. The parameter \( z \) is distributed in the population according to the cumulative distribution function \( F(z) \) and follows an independent stochastic process: A mass \( \omega \) of carriers receives a new draw from \( F(z) \) at rate \( \alpha_h \), whereas the complementary mass \( 1 - \omega \) receives a new draw at rate \( \alpha_\ell < \alpha_h \). The heterogeneous parameter \( \alpha \in \{\alpha_\ell, \alpha_h\} \) is constant over time for each carrier and, thus, measures the volatility of long-term productivity.

The shock \( s \) follows a Markov process on the finite state space \( \{0, 1\} \), with transition intensity \( \mu \) from state one to state zero, and transition intensity \( \lambda \) from state zero to state one. The rates \( \lambda \) and \( \mu \) satisfy \( \lambda > \alpha_h > \alpha_\ell > \mu \), so that the parameter \( s \) is an infrequent, short-term profitability shock. For simplicity, I assume that carriers’ long-run productivity \( z \) does not change while \( s = 0 \).

Lessors acquire aircraft at the market price \( p \) and rent them at a per-period lease rate \( l \). Lessors have to spend \( mp \) on each unit of capital in monitoring costs (Eisfeldt and Rampini, 2009; Rampini and Viswanathan, 2010). Hence, their instantaneous profits are proportional to \( l - (r + m)p \) : On each leased unit, the lessor’s revenues are equal to the lease rate \( l \); its costs \( (r + m)p \) are equal to the opportunity cost \( rp \) of owning an aircraft of price \( p \) when the interest rate is \( r \), and the monitoring costs \( mp \). Lessors are competitive and, thus, in equilibrium earn zero profits—i.e., \( l = (r + m)p \).

**Trade and Transaction costs** - In each period, after carriers know their current parameters \( z \) and \( s \), they can trade aircraft. On owned aircraft, the buyer pays the endogenous price \( p \), but the seller receives \( p (1 - \tau) \), \( \tau \in [0, 1] \). Hence, \( \tau p \) are the transaction costs. On leased aircraft, the lessee pays the endogenous per-period lease rate \( l \) to the lessor, and there are no transaction costs when trading. (No transaction costs on leased aircraft are just a normalization. All that matters is that transaction costs on leased aircraft are lower than on owned aircraft.)

### 4.2 Benchmark: No Frictions (\( \tau = 0 \) and \( m = 0 \))

Secondary markets play an important allocative role since carriers trade aircraft to adjust their productive capacity: When shocks adversely affect their efficiency \( zs \), carriers shed aircraft that
reallocate to carriers who enter the industry. When there are no frictions, Proposition 1 shows that carriers trade aircraft such that, in equilibrium, only the most efficient carriers operate them.

**Proposition 1** When there are no frictions (i.e., $\tau = 0$ and $m = 0$), all carriers are indifferent between leasing or owning aircraft. Moreover, there exists a threshold value $\hat{z}$ such that only carriers $z \geq \hat{z}$ and $s = 1$ operate an aircraft; $\hat{z}$ satisfies

$$X = \frac{\lambda}{\mu + \lambda} (1 - F(\hat{z})).$$

The equilibrium lease rate $l$ is equal to $\hat{z}$, and the equilibrium price $p$ is equal to $\frac{\hat{z}}{\hat{r}}$.

The equilibrium displays two features that do not survive once trading and monitoring costs are present. First, the set of carriers is partitioned. No carrier with temporary shock operates an aircraft, and only the most productive carriers with no temporary shock operate an aircraft. Hence, the equilibrium allocation maximizes the total industry output. Second, the equilibrium allocation, the equilibrium price, and the equilibrium lease rate are independent of the volatility parameters $\alpha_h$ and $\alpha_\ell$, even though assets’ holding periods are obviously shorter for high-volatility carriers.

Proposition 1 also implies that the allocation of leased and owned aircraft is identical. Thus:

**Corollary 2** When there are no frictions, leased aircraft and owned aircraft have the same holding duration, and fly the same number of hours.

In Section 5, I show that the data reject these implications.

4.3 The Effects of Frictions

In the presence of frictions, carriers face a trade-off between leased and owned aircraft, and this modifies the previous benchmark. Lower transaction costs on leased aircraft make leasing attractive for carriers. However, monitoring costs imply that the lease rate $l$ is higher than $r_p$, the implicit rental rate on ownership if there were no transaction costs. If transaction costs are sufficiently high, leasing dominates ownership for all carriers. If transaction costs are sufficiently small, owning dominates leasing for all carriers. The interesting case (and the empirically relevant one) is if transaction costs are of intermediate value.

Intuitively, the lower transaction costs of leasing are more attractive to high-volatility carriers since they expect to adjust their capacity more frequently. Therefore, leased and owned aircraft can coexist, with high-volatility carriers leasing and low-volatility carriers owning. An analytic
characterization of how the volatility of carriers’ productivity affects their choice between leasing and owning cannot be provided because their choice depends on the equilibrium allocation and price, which cannot be solved for in closed form. Thus, I compute numerical solutions to illustrate carriers’ choice between leased and owned aircraft. Appendix B.8 reports all equilibrium conditions.

Figure 3 shows that, in accordance with the intuition, the fraction of aircraft for lease increases monotonically as carriers’ volatilities increase. If $\alpha_\ell$ and $\alpha_h$ are low, expected transaction costs are low, and owning dominates leasing for all carriers. Similarly, if $\alpha_\ell$ and $\alpha_h$ are high, then leasing dominates owning for all carriers. When volatilities are of intermediate values, then high-volatility carriers choose to lease and low-volatility carriers choose to own aircraft.

The comparative statics depicted in Figure 3 can be useful to understand the entry of lessors in the mid-1980s. Figure 2 documents that the aircraft-leasing business started just a few years after the 1980 Airline Deregulation Act removed controls on entry and exit and deregulated fares. Habib and Johnsen (1999) note: “Anticipating the effect of deregulation, [lessors] appear to have invested substantial resources throughout the 1980s and early 1990s to establish general knowledge of secondary market redeployment opportunities for used aircraft.” The Deregulation Act increased competition in airline markets, thereby spurring the entry and exit of carriers, and increasing the volatility of output/profits (the higher the competition a firm faces, the flatter the marginal revenue curve is. Hence, for a given shock to marginal cost, each firm’s output change is bigger in more-competitive markets). Thus, Figure 3 suggests that a more-competitive airline industry increases the demand for intermediaries that specialize in the reallocation of aircraft, and this may help explain
why the leasing business started when the Deregulation Act was passed.

When leased and owned aircraft coexists, carriers’ capacity adjustment differs depending on whether they lease or own aircraft:

**Proposition 3** Let transaction costs satisfy \( \tau > \frac{r}{\lambda+\tau} \). In an equilibrium in which low-volatility carriers own and high-volatility carriers lease aircraft,

(i) There exists \( z^*, z^{**} \) and \( z^{***} \) such that low-volatility carriers: acquire an owned aircraft if they have productivity \( z \geq z^* \) and \( s = 1 \); sell an owned aircraft if they have productivity below the threshold \( z^{**} \) and a temporary shock \( (s = 0) \); sell an owned aircraft if they have productivity \( z \) below the threshold \( z^{***} \) and no temporary shock \( (s = 1) \). Moreover, \( z^* > z^{**} > z^{***} \).

(ii) (Leased aircraft) High-volatility carriers: acquire a leased aircraft if they have productivity \( z \geq l \) and no temporary shock \( (s = 1) \); return a leased aircraft if they have either a temporary shock \( (s = 0) \), or have productivity \( z \) below the threshold \( l \).

Transaction costs generate an option value of waiting for owners. Since efficiency \( z \) is stochastic, the option value means that owners have wider inaction bands than lessees. If transaction costs are sufficiently high —i.e., \( \tau > \frac{r}{\lambda+\tau} \)—some owners choose to keep their aircraft even when their revenues are temporarily zero. Thus, the first testable implication follows:

**Corollary 4** In an equilibrium in which low-volatility carriers own and high-volatility carriers lease aircraft, the distribution function of holding durations of owned aircraft first-order stochastically dominates the distribution function of holding durations of leased aircraft.

The result of the Corollary is the combination of two effects. The first is that high-volatility carriers choose leasing. The second is that the level of productivity that triggers owners to reduce capacity is lower than lessees’—i.e., leased aircraft have higher utilizations than owned aircraft before trading. Hence, owned aircraft trade less frequently. The same two effects also shape the equilibrium cross-sectional distributions of utilizations of leased and owned aircraft. Thus, the second set of testable implications follows:

**Corollary 5** In an equilibrium in which low-volatility carriers own and high-volatility carriers lease aircraft, the distribution function of flying hours of leased aircraft first-order stochastically dominates the distribution function of flying hours of owned aircraft. Hence:
(i) (Extensive margin) Leased aircraft are parked inactive less frequently than owned aircraft.

(ii) (Intensive margin) Conditional on not being parked, leased aircraft fly more than owned aircraft.

The two effects act as follows. First, in equilibrium, lessee carriers have a higher entry threshold than owners—i.e., in terms of Proposition 3, $z^* \leq l$. Second, owners’ wide inaction bands generate a long left tail in their productivity distribution. Instead, leasing’s lower trading frictions truncate the left tail of lessees’ productivity distribution. As a result, Corollary 5 shows that, on average, lessees are more efficient than owners, and, thus, leased aircraft fly more. This difference in efficiency affects both the extensive margin (whether aircraft fly or not) and the intensive margin (conditional on flying, aircraft flying hours). Furthermore, the difference in the lower tails of the productivity distributions implies that the dispersions of the productivity distributions of owners and lessees differ.

4.4 Discussion

The model focuses on the trade-off between the lower one-time trading costs of leased aircraft and the lower per-period costs of owned aircraft, thereby setting aside at least two important aspects of carriers’ fleet decisions: replacements of aircraft and carriers’ fleet-size choice.

The model assumes that all aircraft are identical and do not depreciate. As a result, carriers trade aircraft because their productivity changes over time. Aircraft depreciation introduces another motive for trade: When the quality of the capital depreciates over time, carriers sell old aircraft to acquire new, more-productive ones. In a previous version of this paper, I consider an extension to the current model with two vintages. Under the assumption that the quality of an aircraft and the productivity of a carrier are complements in the production function, more-efficient carriers choose higher-quality aircraft, and they choose to lease in order to replace aircraft at a lower cost when they depreciate. However, the quantitative importance of these effects is negligible.

Furthermore, the model assumes that each carrier operates, at most, one aircraft. This assumption delivers a tractable model with clear empirical predictions. A more realistic setup would have a carrier with average productivity $z$ and i.i.d. shocks $\epsilon_j$ and $s_j$ on each route $j$ it flies, so that a carrier’s total output is $\sum_j (z + \epsilon_j) s_j$. Unfortunately, this setup cannot be solved analytically, but intuitively it would deliver the additional predictions (confirmed by the data) that more-efficient carriers operate more aircraft and lease a lower fraction of their fleets, as they can reallocate their aircraft internally without paying transaction costs. However, this version of the model would still deliver the main predictions that leased aircraft trade more frequently and fly more than owned
aircraft, even within a single carrier.

5 Empirical Evidence: Commercial Aircraft

I use data from commercial aircraft to test the main implications of the model. The analysis follows Corollaries 4 and 5: Section 5.2 investigates the differences in trading patterns between leased and owned aircraft, and Section 5.3 analyzes the differences in capacity utilization. Finally, Section 5.4 investigates whether the model is quantitatively consistent with the data, calibrating it to match moments of the data.

5.1 Data

The empirical analysis uses a database of commercial aircraft compiled by a producer of computer-based information systems. The database is organized into different files that classify aircraft and carriers according to different characteristics. I use two files:

1. Current Aircraft Datafile. This file has detailed cross-sectional data on all aircraft active in April 2003. This dataset (henceforth, cross-sectional data) reports detailed characteristics of aircraft, such as the type (Boeing 737), the model (Boeing 737-200), the engine, the age, cumulative flying hours, etc.; information related to the period with the current operator, such as the operational role of the aircraft (passenger transportation, freighter, etc.), the date on which the current operator acquired the aircraft, total flying hours, annual flying hours (for the 12-month period between May 2002 and April 2003); and whether the aircraft is leased or owned by its current operator. If the aircraft is leased, the dataset reports whether the lease is an operating or a capital lease.

2. Time-series Utilization Datafile. This file (henceforth, time-series data) reports the flying hours and landings of each aircraft for each month from January 1990 to April 2003.

The data have one limitation: They report whether an aircraft is leased with an operating or a capital lease only in the Current Aircraft Datafile. Hence, most of the empirical analysis relies on cross-sectional data. Nevertheless, the cross-sectional data report several details of each aircraft, including the two outcome variables that are the focus of the model: holding durations and flying
hours.\textsuperscript{5} This richness of the data implies that, in the empirical analysis, I can control for several features of the asset that are often unobserved in other studies that rely on cross-sectional data.

I apply the following restrictions to the sample. First, I restrict the analysis to wide-body aircraft operated for passenger transportation.\textsuperscript{6} I do so because carriers employ wide-body aircraft on long-haul point-to-point flights only, and narrow-body aircraft on shorter flights where carriers’ network choice (hub-and-spoke versus point-to-point) affects capacity utilization. Second, in the analysis on capacity utilization, I further restrict the sample to aircraft operated by the same carrier in the period May 2002-April 2003. This restriction is necessary because, in order to eliminate the impact of differential seasonality for different carriers, I use annual hours flown to measure capacity utilization.

Table 1 presents summary statistics, and uncovers patterns consistent with the model. Leased aircraft have shorter holding durations and higher capacity utilization than owned aircraft. To appreciate the magnitudes of the differences, the left panel of Figure 4 plots the empirical distribution of the ongoing cross-sectional holding durations as of April 2003 (measured in months), and the right panel plots the empirical distribution of capacity utilization (hours flown in the period May 2002-April 2003). The dashed line represents owned aircraft, while the solid line represents leased aircraft. A standard Kolmogorov-Smirnov test of the equality of distributions rejects the null hypothesis of equal distributions at the one-percent level (the asymptotic $p$-values are equal to $5.8 \times 10^{-37}$ and $1.5 \times 10^{-10}$, respectively). Moreover, I also test for first-order stochastic dominance, applying the non-parametric procedures proposed by Davidson and Duclos (2000) and Barrett and Donald (2003). Both tests fail to reject the null hypothesis of first-order stochastic dominance, at least at the one-

\textsuperscript{5}The model assumes that revenues and output are identical, while, in practice, they are different. Nonetheless, the data indicate that they are closely related. For example, at the aggregate level, capacity utilization is highly procyclical, and aircraft are parked inactive in the desert more frequently in recessions than in booms. Similarly, at the carrier level, the data reveal that Southwest has higher capacity utilization than other U.S. carriers, and that capacity utilization is substantially lower before a carrier enters into bankruptcy. Moreover, the inclusion of carrier fixed-effects in the empirical analysis implies that the difference between leased and owned aircraft is identified from variations within carriers. Thus, it is less likely that the other component of revenues—i.e., load factors and prices—vary between leased and owned aircraft within a single carrier.

\textsuperscript{6}The database classifies a number of aircraft as “for lease,” meaning that they are currently with the lessor. These aircraft are not included in my analysis for two reasons: 1) I do not know whether these aircraft are available to be operating leased or capital leased; and 2) lessors own freighters and convertible aircraft, too, and the data do not allow me to clearly distinguish between passenger aircraft and freighters when the aircraft are with the lessor. In Subsection 6, I perform several robustness checks that take into account the potential mismeasurement due to this data-coding issue.
Table 1: Summary Statistics

<table>
<thead>
<tr>
<th></th>
<th>Total</th>
<th>Leased</th>
<th>Owned</th>
<th>( p )-value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Panel A</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Holding Duration (Months)</strong></td>
<td>97.66</td>
<td>61.77</td>
<td>108.31</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>(76.34)</td>
<td>(58.19)</td>
<td>(77.84)</td>
<td></td>
</tr>
<tr>
<td><strong>Age (Years)</strong></td>
<td>10.80</td>
<td>9.71</td>
<td>11.12</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>(7.37)</td>
<td>(6.85)</td>
<td>(7.50)</td>
<td></td>
</tr>
<tr>
<td># Obs</td>
<td>3091</td>
<td>707</td>
<td>2384</td>
<td></td>
</tr>
<tr>
<td><strong>Panel B</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Hours Flown</strong></td>
<td>3349</td>
<td>3710</td>
<td>3257</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>(1377)</td>
<td>(1294)</td>
<td>(1382)</td>
<td></td>
</tr>
<tr>
<td><strong>Parked (%)</strong></td>
<td>.055</td>
<td>.024</td>
<td>.063</td>
<td>.0002</td>
</tr>
<tr>
<td></td>
<td>(.229)</td>
<td>(.153)</td>
<td>(.245)</td>
<td></td>
</tr>
<tr>
<td><strong>Age (Years)</strong></td>
<td>11.01</td>
<td>9.87</td>
<td>11.30</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>(6.75)</td>
<td>(6.75)</td>
<td>(7.29)</td>
<td></td>
</tr>
<tr>
<td>#Obs</td>
<td>2846</td>
<td>578</td>
<td>2268</td>
<td></td>
</tr>
</tbody>
</table>

Notes: This table provides summary statistics of the variables. Panel A presents summary statistics for all aircraft in the sample. This full sample is used in the analysis of holding durations. Panel B presents summary statistics for all aircraft that have been operated by the same carrier during the period May 2002 to April 2003. This restricted sample is used in the analysis of capacity utilization. **Holding Duration** is the number of months since the carrier acquired the aircraft. **Age** is the number of years since the delivery of the aircraft. **Hours Flown** is the number of hours the aircraft flew during the period May 2002 to April 2003. **Parked** is a binary variable equal to one if the aircraft has **Hours Flown** equal to zero, and zero otherwise. The **\( p \)-value** refers to the difference of means between the sample of leased aircraft and the sample of owned aircraft. Standard deviations in parenthesis.

5.2 Leasing and Aircraft Trading

The previous tests of equality of distributions of holding durations ignore observable aircraft characteristics that could explain the differences between leased and owned aircraft. For example, Table 1 shows that leased aircraft are, on average, younger. Hence, I remove the effect of observable characteristics by regressing holding durations on a set of covariates: aircraft age, aircraft model fixed-effects, engine maker fixed-effects, and fixed-effects for each maker of the auxiliary power unit. Then, I construct residual holding durations as the regression’s residuals. The left panel of Figure 5 presents the empirical distributions of these residuals. The dashed line represents owned aircraft and the solid line represents leased aircraft. Again, the cumulative distribution function of the residual holding durations of owned aircraft first-order stochastically dominates the cumulative distribution function of the residual holding durations of leased aircraft. The average residual duration of owned

---

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---

7 As holding durations and utilizations may be correlated within carriers, I have also compared the distributions of the median holding duration and median utilization for each carrier. In this case, too, I accept the null hypothesis of first-order stochastic dominance.
Fig. 4: Empirical cumulative distribution functions of holding durations (left panel) and capacity utilizations (right panel). The dashed line represents owned aircraft, and the solid line represents leased aircraft.

aircraft is about 34 months longer than the average residual duration of leased aircraft.

In order to test for first-order stochastic dominance, I could compare the distributions of residual durations using the same tests used in the case of raw holding durations. However, residual durations are not directly observed but, rather, estimated. Hence, I need to take into account the sampling variability when constructing the distributions of the test statistics. Thus, I follow Abadie (2001) and use a bootstrap procedure to compute the \( p \)-values of the test statistics. The Kolmogorov-Smirnov test of equality of the distributions rejects the null hypothesis of equal distributions (the bootstrapped \( p \)-value is equal to 0). Moreover, the Davidson and Duclos (2000) and Barrett and Donald (2003) tests of first-order stochastic dominance fail to reject the null hypothesis that the distribution of residual durations of leased aircraft first-order stochastically dominates the distribution of residuals of owned aircraft, at least at the one-percent level (the bootstrapped \( p \)-values are equal to .988 and 1, respectively). In practice, sampling variability is not a concern because of the large sample size. Appendix A presents the details of the procedures and of the results.

The right panel of Figure 5 plots similar residual durations obtained from a regression that also includes carrier fixed-effects as explanatory variables, in addition to the set of covariates previously listed. These fixed-effects controls for all unobserved carriers’ characteristics, thus controlling for carriers’ selection into leasing. The average residual durations of owned aircraft is now about 21 months longer than the average residual durations of leased aircraft, or 38 percent. Moreover, the bootstrapped Kolmogorov-Smirnov test of equality of the distributions rejects the null hypothesis of equal distributions (the bootstrapped \( p \)-value is equal to 0). The Davidson and Duclos (2000) and
Barrett and Donald (2003) tests for first-order stochastic dominance fail to reject the null hypothesis that the distribution of residual durations of leased aircraft first-order stochastically dominates the distribution of residuals of owned aircraft, at least at the ten-percent level (the bootstrapped $p$-values are equal to .917 and .994, respectively. Further details of the tests are in Appendix A).

The divergence between the left and right panels of Figure 5, and between the estimated differences of 34 months versus 21 months when carriers fixed-effects are excluded or included in the regression, respectively, provides evidence for both forces highlighted by the model. Since the difference between leased and owned aircraft decreases when the regression controls for carrier fixed-effects, high-volatility carriers lease a higher fraction of their fleet, consistent with selection. Since the difference between leased and owned aircraft persists when the regression controls for carrier fixed-effects, leasing affects trading independent of carriers’ selection. Moreover, the magnitude of the divergence (34 months versus 21 months) suggests that carriers’ selection is quantitatively less important than the effect of leasing.

An additional way to investigate differences in trading frictions is to compare the probability of trading leased and owned aircraft as a function of their utilization in the year prior to trade. Proposition 3 implies that leased aircraft should have a higher utilization than owned aircraft before trading. To test this implication, I employ the Time-series Utilization Datafile to obtain aircraft’s hours flown in the period May 2001-April 2002. I then merge these hours flown with the aircraft
characteristics from the *Current Aircraft Datafile*. With these merged data, I employ a linear probability model in which the dependent variable is equal to one if the aircraft traded in the period May 2002-April 2003, and zero otherwise. The independent variables are the aircraft characteristics employed in previous regressions—i.e., the age of the aircraft, aircraft model fixed-effects, and fixed-effects for each maker of the auxiliary power unit—plus the hours flown in the period May 2001-April 2002, and a dummy variable equal to one if the aircraft is leased, and zero otherwise.

Table 2 presents the results of four specifications. Specifications (1) and (2) do not include carrier fixed-effects, while specifications (3) and (4) do. In specifications (2) and (4), I interact the hours flown in the period May 2001-April 2002 with an indicator variable equal to one if the aircraft is leased, and zero otherwise. Thus, specifications (2) and (4) allow the previous year’s utilization to differentially affect the probability of trading leased and owned aircraft.

The coefficients reported in column (1) indicate that leased aircraft are 13-percent more likely to trade, confirming the prediction of Proposition 4. The coefficients in column (2) further indicate that the difference in the probability of trading a leased aircraft versus an owned one decreases as utilization increases, and it almost disappears for aircraft that are used the most. To appreciate the differences in trading probabilities, the left panel of Figure 6 displays the fitted probability of trading for an aircraft with average sample characteristics, obtained from specifications (2) in Table 2. Specifications (3) and (4) indicate that the differences between leased and owned aircraft persist if carrier fixed-effects are included. The magnitudes are smaller, though, as the right panel of Figure 6
Table 2: Leasing and Probability of Trading

<table>
<thead>
<tr>
<th>Probability of Trade</th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age</td>
<td>.0021</td>
<td>.0025</td>
<td>.0026</td>
<td>.0028</td>
</tr>
<tr>
<td></td>
<td>(.0011)</td>
<td>(.0011)</td>
<td>(.0011)</td>
<td>(.0011)</td>
</tr>
<tr>
<td>Hours Flown in t-1</td>
<td>-.0258</td>
<td>-.0111</td>
<td>-.0173</td>
<td>-.0098</td>
</tr>
<tr>
<td></td>
<td>(.0043)</td>
<td>(.0037)</td>
<td>(.0047)</td>
<td>(.0044)</td>
</tr>
<tr>
<td>Hours Flown in t-1*Leased</td>
<td>-.0490</td>
<td>-.0249</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>(.0106)</td>
<td>(.0106)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Leased</td>
<td>.1299</td>
<td>.2849</td>
<td>.1150</td>
<td>.1938</td>
</tr>
<tr>
<td></td>
<td>(.0140)</td>
<td>(.0419)</td>
<td>(.0156)</td>
<td>(.0418)</td>
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<tr>
<td>Model Fixed effects</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Carrier Fixed effects</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>R^2</td>
<td>.130</td>
<td>.145</td>
<td>.325</td>
<td>.328</td>
</tr>
<tr>
<td># Obs</td>
<td>3016</td>
<td>3016</td>
<td>3016</td>
<td>3016</td>
</tr>
</tbody>
</table>

Notes: This table presents the estimates of the coefficients of four specifications of a linear probability model. The dependent variable is equal to one if the operator of the aircraft in May 2002 is no longer operating the aircraft in April 2003, and zero otherwise. Hours Flown in t-1 corresponds to the hours flown during the period May 2001-April 2002. All specifications further include a constant, fixed-effects for the maker of the engine and fixed-effects for the maker of the auxiliary power unit. Robust standard errors in parenthesis. Also shows. Thus, specifications (3) and (4) confirm that selection into leasing plays a role. However, this selection does not account for all the differences in trading patterns of leased and owned aircraft, corroborating that carriers shed leased aircraft faster when their profitability declines.

5.3 Leasing and Aircraft Utilization

In this section, I investigate whether leased and owned aircraft have different flying hours, testing Proposition 5. The empirical model controls for all observable aircraft characteristics reported in the cross-sectional data and uses the residuals of flying hours as a measure of carriers’ efficiency.

Specifically, let $X_{ik}$ be the observable characteristics of aircraft $i$ of model $k$—the age of the aircraft, aircraft model fixed-effects, engine maker fixed-effects, and fixed-effects for each maker of the auxiliary power unit—and let $z_{ik}s_{ik}$ be the (unobserved) efficiency of the operator. The observable characteristics of aircraft $ik$ and the efficiency of its operator jointly determine flying hours $y_{ik}$ according to:

$$y_{ik} = z_{ik}s_{ik} \exp(\beta X_{ik}).$$

(1)

Table 1 documents that aircraft are sometimes parked inactive. Hence, I let the binary variable $s_{ik}$ describe the decision to fly the aircraft or to park it. Thus, flying hours are given by

$$y_{ik} = \begin{cases} z_{ik} \exp(\beta X_{ik}) & \text{if } s_{ik} = 1 \\ 0 & \text{if } s_{ik} = 0, \end{cases}$$

21
where the binary variable $s_{ik}$ derives from the vector of $W_{ik}$ of observable characteristics of aircraft $i$ of model $k$ through the following latent process:

$$s_{ik} = \begin{cases} 
1 & \text{if } \gamma W_{ik} + \eta_{ik} \geq 0 \\
0 & \text{if } \gamma W_{ik} + \eta_{ik} < 0.
\end{cases}$$

Thus, I observe:

$$y_{ik} = \begin{cases} 
z_{ik} \exp(\beta X_{ik}) & \text{if } \gamma W_{ik} + \eta_{ik} \geq 0 \\
0 & \text{if } \gamma W_{ik} + \eta_{ik} < 0.
\end{cases}$$

The empirical model described by equations (2) and (3) is a Heckman (1979)-type selection model. Letting $\epsilon_{ik} = \log z_{ik}$, and assuming that $(\epsilon_{ik}, \eta_{ik})$ are normal random variables with mean zero and covariance matrix

$$\Sigma = \begin{pmatrix} 
\sigma^2_\epsilon & \rho \sigma_\epsilon \sigma_\eta \\
\rho \sigma_\epsilon \sigma_\eta & \sigma^2_\eta
\end{pmatrix},$$

I can employ standard results for bivariate normal random variables and estimate the model using either Heckman’s two-step procedure (Heckman, 1979) or maximum likelihood. Since the empirical model depends on $\sigma_\eta$ only through $\frac{\gamma \sigma_\eta}{\sigma_\eta}$, the normalization $\sigma_\eta = 1$ is required.

The estimation of the empirical model given by equations (2) and (3) faces some econometric challenges. The first concerns the separate identification of the extensive margin—whether to fly the aircraft $s_{ik}$—and of the intensive margin—the flying hours $y_{ik}$. Specifically, while the parametric assumption of normality of the error terms guarantees identification, a stronger identification requires that at least one variable included in the vector $W_{ik}$ is excluded from the vector $X_{ik}$. Finding such an exclusion restriction is traditionally challenging. In the case of aircraft, this restriction requires a variable that affects the costs/benefits of parking the aircraft, but it does not affect the intensive margin of utilization. Aircraft are always parked in warm, dry locations in order to prevent damage to the fuselage and engines. Therefore, the distance of a carrier’s headquarters from a warm location plausibly affects the fixed costs/benefits of parking the aircraft, but does not affect the marginal costs/benefit of flying the aircraft one additional hour. Thus, I obtain the average latitude of the country where an operator is based. Since the latitude measures the distance from the equator, it is correlated with the distance from a warm, dry location. However, the latitude does not vary within a country and within a carrier, so I use (the log of) the latitude interacted with the age of each aircraft $ik$ to obtain a variable that should positively affect whether the aircraft flies, but does not affect how many hours it flies.
Table 3: Estimates of the Parameters of Equations (2) and (3)

<table>
<thead>
<tr>
<th></th>
<th>(1) Hours Flown</th>
<th>FLY</th>
<th>(2) Hours Flown</th>
<th>FLY</th>
</tr>
</thead>
<tbody>
<tr>
<td>AGE</td>
<td>-.0170</td>
<td>-.1546</td>
<td>-.0133</td>
<td>-.1827</td>
</tr>
<tr>
<td></td>
<td>(.0044)</td>
<td>(.0384)</td>
<td>(.0046)</td>
<td>(.0413)</td>
</tr>
<tr>
<td>LOG(LATITUDE)*AGE</td>
<td>.0186</td>
<td></td>
<td>.0222</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(.0087)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(\sigma_e)</td>
<td>.5408</td>
<td></td>
<td>.5348</td>
<td></td>
</tr>
<tr>
<td></td>
<td>(.0476)</td>
<td></td>
<td>(.0478)</td>
<td></td>
</tr>
<tr>
<td>(\rho)</td>
<td>-.4512</td>
<td></td>
<td>-.9494</td>
<td></td>
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<tr>
<td></td>
<td>(.5690)</td>
<td></td>
<td>(.3592)</td>
<td></td>
</tr>
<tr>
<td>MODEL FIXED EFFECTS</td>
<td>YES</td>
<td></td>
<td>YES</td>
<td></td>
</tr>
<tr>
<td>CARRIER FIXED EFFECTS</td>
<td>NO</td>
<td></td>
<td>YES</td>
<td></td>
</tr>
<tr>
<td># Obs</td>
<td>2846</td>
<td></td>
<td>2846</td>
<td></td>
</tr>
</tbody>
</table>

Notes: This table reports estimates of the parameters of equations (2) and (3), obtained using Heckman (1979) two-step procedure. LOG(LATITUDE)*AGE is the interaction between the log of the average latitude of the country of the operator of the aircraft, and the AGE of the aircraft. The equations in specifications (1) and (2) further contain constant, engine-maker fixed-effects, and auxiliary-power-unit-maker fixed-effects (not reported). Standard errors in parenthesis are obtained bootstrapping the data using 1,000 replications.

The second econometric challenge is a potential endogeneity concern that arises because a carrier’s efficiency—the unobservable—could be correlated with the vintage of the aircraft—an observable included in the vector \(X_{ik}\). Specifically, if the vintage of the aircraft and a carrier’s efficiency are either complements or substitutes in the output function, carriers self-select and acquire different vintages according to their efficiency, with more- (less-) efficient carriers acquiring younger aircraft if they are complements (substitutes). To solve this potential concern, I use instruments that are correlated with the age of the aircraft, but arguably uncorrelated with a carrier’s efficiency—i.e., the unobservable. The instruments draw upon the idea that a carrier chooses a vintage from the distribution of all vintages available at the time it acquired the aircraft. Hence, if all aircraft of a given model are young, a carrier is most likely to acquire a young aircraft. Thus, the instruments exploit two facts: 1) Carriers acquired different aircraft at different times, and their choice sets varied over time; and 2) choices are correlated with choice sets. In practice, I use the following two instruments for the age of aircraft \(ik\): 1) the average age of all aircraft of model \(k\) in the year in which the operator acquired aircraft \(ik\); and 2) the total number of aircraft of model \(k\) existing in the year in which the operator acquired aircraft \(ik\).

Specification (1) in Table 3 reports the estimates of the parameters. The point-estimate of the coefficient of aircraft age in the intensive margin equation is equal to -.0170, which indicates that the number of hours flown decreases slowly as aircraft age. The point-estimate of the coefficient
of aircraft age in the extensive margin equation is equal to -.1546, which, translated into marginal effects, implies that the probability that an aircraft is parked is 0.3-percent higher for an aircraft one year older. Moreover, the interaction between the log of the latitude of the operator’s country and the age of the aircraft is positive and significant, as expected. Instead, the estimate of the correlation coefficient $\rho$ is negative, but rather imprecise in specification (1).

In the specification reported in (2), I add carrier fixed-effects to the vectors $X_{ik}$ and $W_{ik}$. The point-estimate of the coefficient of aircraft age in the intensive margin equation is now equal to -.0133, just slightly smaller than the coefficient of specification (1): I cannot reject the hypothesis that they are identical. Similarly, the point-estimate of the coefficient of age in the extensive margin equation is now equal to -.1827, which is again similar to—and statistically indistinguishable from—the coefficient of specification (1).

I now use the estimated coefficients reported in Table 3 to obtain measures of carriers’ efficiency. Using equation (1), I calculate carriers’ efficiency as:

$$\hat{z}_{ik}s_{ik} = \frac{y_{ik}}{\exp (\beta X_{ik})}.$$  

Figure 7 shows the empirical distributions of $\hat{z}_{ik}s_{ik}$ corresponding to owned and leased aircraft. The left panel corresponds to the efficiency $\hat{z}_{ik}s_{ik}$ calculated using the parameters of specification (1), and the right panel corresponds to the efficiency $\hat{z}_{ik}s_{ik}$ calculated using the parameters of specification (2)—i.e., including carriers’ fixed-effects in $\beta X_{ik}$. The dashed line represents the efficiency of operators of owned aircraft, while the solid line represents the efficiency of operators of leased aircraft. Simple visual inspection shows that lessees’ productivity is higher than owners’.

Since efficiency is not directly observed, but estimated, I use a bootstrap procedure to compute the $p$-values of the test statistics. Appendix A presents the details of the tests. The Kolmogorov-Smirnov test of the equality of distributions rejects the null hypothesis of equal distributions: The bootstrapped $p$-values are equal to 0 when carrier fixed-effects are not included in the empirical model, and .010 when fixed-effects are included. Moreover, the tests for first-order stochastic dominance proposed by Davidson and Duclos (2000) and Barrett and Donald (2003) fail to reject the null hypothesis that the distribution of lessees’ efficiency first-order stochastically dominates the owners’ distribution. The bootstrapped $p$-values of the Davidson and Duclos test are equal to .958 (without carrier fixed-effects) and .940 (with carrier fixed-effects), and the bootstrapped $p$-values of the Barrett and Donald test are equal to .989 (without carrier fixed-effects) and .973 (with carrier fixed-effects).

I now employ the estimates of carriers’ efficiency to quantify the differences in utilization between
leased and owned aircraft. In particular, I calculate the empirical counterparts of parts (i) and (ii) of Proposition 5 and, thus, decompose the differences between leased and owned aircraft into separate differences in the intensive and extensive margins. Specifically, let $E(s_Lz_L)$ and $E(s_Oz_O)$ be the average efficiency obtained from leased and owned aircraft, respectively. Taking logs, I can express the percentage difference in efficiency between leased and owned aircraft as

$$\log E(s_Lz_L) - \log E(s_Oz_O) = \log \Pr(s_L = 1) E(z_L|s_L = 1) - \log \Pr(s_O = 1) E(z_O|s_O = 1). \quad (4)$$

Rearranging the above equation (4), I obtain:

$$\log E(s_Lz_L) - \log E(s_Oz_O) = \log \Pr(s_L = 1) - \log \Pr(s_O = 1) + \log E(z_L|s_L = 1) - \log E(z_O|s_O = 1).$$

The term $\log \Pr(s_L = 1) - \log \Pr(s_O = 1)$ measures the differences in the extensive margin, and the term $\log E(z_L|s_L = 1) - \log E(z_O|s_O = 1)$ measures the differences in the intensive margin.

Table 4 quantifies and decomposes the difference between leased and owned aircraft. Columns (1) and (2) correspond to specifications (1) and (2), respectively, in Table 3.\(^8\) Table 4 shows that the difference between leased and owned aircraft is equal to 6.5-7.8 percent of output. The intensive margin accounts for approximately 75 percent of the total difference, and the extensive margin accounts for the remaining approximately 25 percent. The divergence between columns (1) and (2)

\(^8\)The term $\log \Pr(s_L = 1) - \log \Pr(s_O = 1)$ is calculated as $(\log E(s_L = 1) - \log E\Phi(\gamma W)) - (\log E(s_O = 1) - \log E\Phi(\gamma W))$ to take into account the differences in observable characteristics between leased and owned aircraft.
Table 4: Differences in Utilization between Leased and Owned Aircraft

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Total</strong></td>
<td>log $E(s_L</td>
<td>z_L) - log E(s_O</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Extensive Margin</strong></td>
<td>log $Pr(s_L = 1) - log Pr(s_O = 1)$</td>
<td>0.0198</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Intensive Margin</strong></td>
<td>log $E(z_L</td>
<td>s_L = 1) - log E(z_O</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes: This table reports the estimated differences in efficiency between leased and owned aircraft. The magnitudes reported in Columns (1) and (2) are calculated using the parameters of specifications (1) and (2), respectively, in Table 3. Standard errors in parenthesis are obtained by bootstrapping the data using 1,000 replications.

of Table 4 provides further evidence for both forces highlighted by the model. Moreover, columns (1) and (2) of Table 4 show that carriers’ selection, captured by carriers’ fixed-effects, accounts for a smaller fraction of the observed difference between leased and owned aircraft in capacity utilization, indicating that the effect of leasing is quantitatively more important than carriers’ selection.

5.4 Calibrating the Model

I now investigate whether the model in Section 4 is quantitatively consistent with the data, calibrating it to match moments of the data.

This calibration faces some challenges. Although the model is highly non-linear, so that all parameters affect all outcomes, the identification of some key parameters is problematic. More precisely, the mass of assets $X$ determines the optimal buying/selling thresholds of owners and lessees (this is easy to see, for example, from the equilibrium of the frictionless benchmark—i.e., Proposition 1). In turn, for any value of the other parameters, these thresholds determine aircraft’s holding durations and utilizations. Unfortunately, the data do not allow me to pin down the value of $X$. Similarly, the data do not provide any direct evidence on the level of monitoring costs. We can only infer that these costs belong to a certain range—i.e., they are not zero and not infinitely large—such that certain carriers choose to lease and others choose to own aircraft. For these reasons, the main goal of this calibration is to investigate whether the model is quantitatively consistent with the data, rather than an estimation of its structural parameters.

With the previous caveats in mind, I proceed by fixing the value of the interest rate to $r = 0.03$. (It is well known that the discount factor/interest rate are difficult parameters to calibrate in the data.) I further assume that $F(z)$ is normal with mean $E(z)$ and standard deviation $St.Dev.(z)$ to be calibrated. Then, I choose the parameters $(X, \omega, \alpha_L, \alpha_H, \mu, \lambda, E(z), St.Dev.(z), \tau, m)$ so that the
Table 5: Moments and Parameters of the Calibration

<table>
<thead>
<tr>
<th>Panel A: Moments</th>
<th>(1)</th>
<th>(2)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>DATA</td>
<td>MODEL</td>
</tr>
<tr>
<td>Average Holding Duration (Months), Owned Aircraft</td>
<td>108.31</td>
<td>100.56</td>
</tr>
<tr>
<td>Average Holding Duration (Months), Leased Aircraft</td>
<td>61.77</td>
<td>55.80</td>
</tr>
<tr>
<td>St. Dev. Holding Duration (Months), Owned Aircraft</td>
<td>77.84</td>
<td>95.16</td>
</tr>
<tr>
<td>St. Dev. Holding Duration (Months), Leased Aircraft</td>
<td>58.19</td>
<td>51.24</td>
</tr>
<tr>
<td>Average Hours Flown, Owned Aircraft</td>
<td>3257</td>
<td>2728</td>
</tr>
<tr>
<td>Average Hours Flown, Leased Aircraft</td>
<td>3710</td>
<td>3329</td>
</tr>
<tr>
<td>St. Dev. Hours Flown, Owned Aircraft</td>
<td>1382</td>
<td>1827</td>
</tr>
<tr>
<td>St. Dev. Hours Flown, Leased Aircraft</td>
<td>1294</td>
<td>1610</td>
</tr>
<tr>
<td>Parked Aircraft (%), Difference Owned-Leased</td>
<td>3.9</td>
<td>3.8</td>
</tr>
<tr>
<td>Leased Aircraft (%)</td>
<td>22.8</td>
<td>23.0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Panel B: Parameters</th>
<th>X</th>
<th>0.4958</th>
<th>λ</th>
<th>0.4531</th>
</tr>
</thead>
<tbody>
<tr>
<td>ω</td>
<td>0.2835</td>
<td>E(z)</td>
<td>767.42</td>
<td></td>
</tr>
<tr>
<td>α_h</td>
<td>0.3358</td>
<td>St.Dev.(z)</td>
<td>2833.7</td>
<td></td>
</tr>
<tr>
<td>α_l</td>
<td>0.2962</td>
<td>τ</td>
<td>0.1583</td>
<td></td>
</tr>
<tr>
<td>μ</td>
<td>0.0277</td>
<td>m</td>
<td>0.0267</td>
<td></td>
</tr>
</tbody>
</table>

Notes—This table contains details of the calibration of model parameters. Column (1) in Panel A reports the moments of the data that the model seeks to match. Column (2) in Panel A reports the corresponding moments computed from the model with the parameters reported in Panel B.

moments computed from the model are as close as possible to the moments in the data reported in Table 5.4. Panel B of Table 5.4 reports the implied parameters, and column (2) of Panel A reports the moments computed from the model at those parameters.

Overall, the model matches the data quite well: On average, the difference between the empirical and the theoretical moments is less than 13 percent. The transaction cost parameter τ is equal to approximately 15 percent—a non-trivial magnitude—and the monitoring cost parameter m is equal to approximately 2.7 percent. The parameters α_l and α_h imply that the productivity of high-volatility carriers varies every 35.7 months (≈ 12/α_h), and the productivity of low-volatility carriers varies every 40.5 months (≈ 12/α_l). The difference is less than five months, small compared to the empirical difference in holding durations between leased and owned aircraft. This confirms that selection does not play a large role in explaining the empirical results of Section 5.2. Similarly, the parameters imply that the equilibrium entry threshold of owners is equal to z* = 1224, and the entry threshold of lessees is equal to l = 1281. Hence, if owners had inaction bands as wide as lessees’ and, thus, selection was the only difference between lessees and owners, then owners’ average hours flown would be E(y|z ≥ z*, s = 1) = 3272, while lessees’ would remain E(y|z ≥ l, s = 1) = 3329. This small difference corroborates that selection is a minor factor driving the empirical results of
As mentioned, the parameters of Table 5.4 rely on several assumptions. Unfortunately, some of these assumptions are not directly testable with the available data. For that reason, I view these parameters as suggestive. Nonetheless, the magnitudes of these parameters do not seem unreasonable. A conclusion that emerges from the calibration is that small differences in carriers’ volatilities can lead to larger differences in trading and utilization between leased and owned aircraft.

6 Alternative Explanations and Robustness Checks

The results of the empirical analysis indicate that the trading and utilization patterns of leased and owned aircraft differ systematically, as Corollaries 4 and 5 predict. I now consider alternative hypotheses and perform some robustness checks. The analysis strengthens the previous findings.

6.1 Selection into Leasing

In the theoretical model, high-volatility carriers lease and low-volatility carriers own aircraft. I now investigate whether different potential motives behind carriers’ decision to lease could provide an alternative explanation of all the empirical results.

6.1.1 Persistence of Productivity

The model assumes that, when a carrier’s productivity changes over time, its new productivity is independent of the previous one. If more-productive carriers receive better productivity draws in the future, then they should have longer expected holding periods. Thus, they may choose to purchase rather than lease because they can spread the transaction costs over a longer holding period. Hence, this alternative hypothesis could explain the difference in holding durations and trading frequencies between leased and owned aircraft.

However, additional patterns in the data speak against this alternative hypotheses. The first argument against this type of selection is that the analysis in Section 5.2—Table 2 and Figures 5-6, in particular—shows that the substance of the results on holding periods is unchanged when carriers’ fixed-effects are included in the estimation. Thus, an alternative hypothesis based on differences across carriers cannot explain the observed differences in holding durations between leased and owned aircraft within carriers. Second, this alternative hypothesis suggests that owners’ productivity may be higher than lessees’. However, the analysis in Section 5.3—Figure 7 and Table 4, in
particular—shows that exactly the opposite is true. Moreover, the results are almost identical with or without carriers’ fixed-effects. Third, this selection based on productivity implies that the upper tails of the productivity distributions should differ, with owners’ distribution first-order stochastically dominating lessees’ distribution. Figure 7 shows that the two distributions move almost parallel after the initial difference at low levels of productivity, and the difference does not reverse at high productivity levels, as this alternative hypothesis requires. More formally, Appendix A shows that, when restricting the analysis to the top 15 percent of carriers’ productivities, a Kolmogorov-Smirnov test of the equality of distributions does not reject the null hypothesis of equal distributions (the bootstrapped $p$-value is equal to .131); and the Davidson and Duclos (2000) and Barrett and Donald (2003) tests of first-order stochastic dominance reject the null hypothesis of first-order stochastic dominance (the bootstrapped $p$-values are equal to .474 and .455, respectively).

6.1.2 Replacement of Aircraft

An alternative hypothesis is that the most-productive carriers select leasing because it allows them to replace their aircraft at lower costs when they depreciate. This explanation acknowledges that trading frictions are lower for leased aircraft, as this paper posits, but claims that replacement is the main motive for trade. Thus, the argument is that the most-productive carriers choose to lease aircraft and trade them more frequently in order to replace them. Moreover, since productive carriers select into leasing, leased aircraft fly more than owned ones.

However, several patterns in the data are inconsistent with this explanation. First, according to this explanation, replacement is the main motive for trade. However, Table 2 and Figure 6 show that the probability of trading an aircraft is a decreasing function of the previous year’s utilization. If replacement were the main motive for trade, the probability of trading an aircraft should be an increasing function of the previous year’s utilization. Furthermore, if carriers selected leasing to replace aircraft, the probabilities of trading a leased and an owned aircraft should diverge as previous utilization increases, as high productivity implies high utilization. Table 2 and Figure 6 show that this is not the case. Second, this type of selection again implies that the difference in the distributions should be concentrated in the upper tail of the distribution. However, we have already highlighted that Figure 7 shows that the cumulative distribution functions of lessees’ and owners’ efficiency move almost parallel after the initial difference at low productivity levels, that the difference does not grow larger as productivity increases, and that formal tests reject the null hypothesis of first-order stochastic dominance in the upper tails of the distributions. Third, Tables
2-4 and Figures 5-7 show that the substance of the results is identical when carriers’ fixed-effects are included in the estimation. Hence, any carrier-specific factor cannot explain the observed differences between leased and owned aircraft.

### 6.1.3 Financing Constraints

Sharpe and Nguyen (1995) suggest that leasing relaxes financing constraints. Eisfeldt and Rampini (2009) explain that, since it is easier for a lessor to regain control of an asset than it is for a secured lender to repossess it, lessors can extend more credit than secured lenders can. However, leasing separates ownership and control of assets, thereby generating agency costs. As a result of this trade-off, more credit-constrained firms lease more of their capital.

The focus of these papers on leasing and financing frictions differs from the focus here. They are interested in firms’ decision to lease, while this paper focuses also on the effects of leasing on aircraft trading and utilization. In aircraft markets, it is certainly true that, in the initial stages, operating lessors were mainly buying surplus second-hand aircraft from carriers and leasing them to other carriers, particularly those with poor access to debt and equity markets. Moreover, Benmelech and Bergman (2011) find that airlines in countries with poor creditor rights are more likely to lease than to own aircraft, consistent with the idea that leasing allows firms to alleviate some of the financial frictions associated with debt financing. Hence, the question arises: Is it likely that financing constraints alone explain all the observed differences between leased and owned aircraft?

In my view, the answer is no, for at least two reasons. First, explanations based on financing frictions do not have joint predictions for assets’ trading and utilization. Instead, the data show that leased aircraft trade more frequently and fly more. Second, all the empirical results are robust to the inclusion of carrier fixed-effects, while financing frictions are constant within a carrier. Thus, financing frictions do not explain the differences between leased and owned aircraft documented in Tables 2-4 and Figures 5-7, which persist once carrier fixed-effects are included in the regressions.

Rather, the ideas that leasing relaxes financing constraints and that leasing facilitates asset reallocation seems complementary. Eisfeldt and Rampini (2009) suggest that leasing is particularly attractive to financially-constrained operators, and these operators often have volatile capacity needs. Hence, lessors frequently get aircraft returned, which leads them to further specialize in redeployment. This specialization explains the patterns in trading and utilization that are the focus of this paper.
6.1.4 The Role of Taxation

Several papers suggest that leasing provides taxation advantages to the contracting parties, and they investigate how taxes affect corporate leasing policies (Miller and Upton, 1976; Graham, Lemmon and Schallheim, 1998). The idea is that leases allow for the transfer of tax shields from firms that cannot fully utilize the associated tax deduction (lessees) to firms that can (lessors).

However, it is unlikely that taxes explain all the empirical results. First, Babcock and Bewsher (1998) note that in an operating lease, “any tax benefits are normally incidental.” Second, it is not clear why there is a substantial mix of leased and non-leased assets. If leasing were so favorable from a taxation perspective, we should probably expect all aircraft to be leased. Third, if leasing gives carriers a tax advantage, then it is not clear why carriers are more likely to shed leased aircraft first. Fourth, Gavazza (2010) shows that there is considerable variation in the fraction of different aircraft types leased, and taxation advantages (if any) will not depend on aircraft type. Fifth, any tax benefit would be specific to a lessee, and would not vary within a carrier. Hence, in the empirical analysis, these advantages would have been picked up by carrier fixed-effects and would not explain the observed variation between leased and owned aircraft within carriers.

6.2 Quality Differentials and Adverse Selection

The literature on durable goods highlights the role of quality differentials and depreciation in explaining patterns of trade. The literature makes different predictions if parties have symmetric versus asymmetric information on the asset’s quality. Hendel and Lizzieri (1999b) shows that, under symmetric information, lower-quality goods should trade more frequently. Since Section 5.2 shows that leased aircraft trade more frequently, we must infer that they are of lower quality. Then, however, it is difficult to explain why leased aircraft fly more than owned ones. Moreover, Pulvino (1998) clearly rejects the hypothesis that, conditional on observable characteristics such as age, lower-quality aircraft trade more than higher-quality ones. Thus, theories of quality differentials under symmetric information cannot explain the observed patterns.

Under asymmetric information, higher-quality durable goods trade more frequently (Hendel and Lizzieri, 1999a), so we must conclude that leased aircraft are of higher quality. This explanation might seem to explain the empirical differences between leased and owned aircraft. In principle, adverse selection can be thought of as a cost captured in a reduced-form way by the transaction costs. However, several institutional features of aircraft markets and a closer look at the data show
that this explanation is unlikely to account for all observed patterns. First, the aviation authorities regulate aircraft maintenance: After a fixed number of hours flown, carriers undertake compulsory maintenance. This reduces quality differences. Moreover, Pulvino (1998) rejects the hypothesis that unobserved quality differentials among aircraft explain trade patterns. Furthermore, maintenance records are readily available, and all parties can observe the entire history of each aircraft. In addition, all transactions involve a thorough material inspection of the aircraft, which mitigates information asymmetries. Second, Hendel and Lizzeri (2002) present a model of leasing under adverse selection. In their framework, leased durable goods trade more frequently because high-valuation individuals select leasing, as they want to replace the durables more frequently. However, as I discuss in Section 6.1.2, many patterns in the data are inconsistent with this type of selection. In particular, the data show that the main motive for trade is to reduce/increase capacity, not to replace it. Thus, the reason why individuals/firms lease an asset in Hendel and Lizzeri’s model does not seem to apply to the aircraft market. Third, from another file in the main database, I can isolate aircraft involved in sale-leaseback transactions—transactions in which the carrier initially owns the aircraft, then sells it and simultaneously leases it back from a lessor—or aircraft that were once owned by a carrier and are currently owned by a lessor. Presumably, the quality of these aircraft did not change with the type of ownership. However, these aircraft exhibit differences in trading patterns between the periods in which they were owned and the periods in which they were leased that are almost identical to the trading patterns in the cross-sectional data.

6.3 Moral Hazard

Another potential explanation of the empirical results is moral hazard: Carriers abuse leased aircraft because they do not own them (Johnson and Waldman, 2010). However, several other features of the data and institutional details about the aircraft market and airline business are at odds with moral hazard. First, moral hazard arises from unobservability (or non-contractibility) of actions. Here, all parties clearly observe the utilization of the aircraft: I observe how much the aircraft are used, and lessors and lessees observe utilization, too. Second, leasing contracts are contingent on aircraft utilization (hours flown and landings). Third, if moral hazard were a severe problem for aircraft, then we would probably not observe aircraft being leased at all (Smith and Wakeman, 1985). Fourth, leased aircraft trade more frequently than owned aircraft. If carriers can abuse leased aircraft, it is not clear why they trade them more than owned aircraft. Under moral hazard, the opposite should be true—i.e., leased aircraft should trade less frequently than owned aircraft. Fifth, under moral
hazard, carriers always have the incentive to fly leased aircraft more than owned ones. Thus, aircraft utilization distributions should differ in both the upper and lower tails. In contrast, Figure 7 and Appendix A show that only the lower tails differ. Finally, the incentives to abuse a leased aircraft should be stronger if a lessee expects to return rather than keep it. However, Figure 6 shows that this not the case: Lessees are more likely to return aircraft that are used less than those that they keep. Similarly, Figure 6 shows that the differences in trading probabilities between leased and owned aircraft are highest for aircraft that are parked inactive and lower for aircraft that are used the most, as predicted by the model. Under moral hazard, I would expect exactly the opposite.

6.4 Time between Consecutive Lessees

One potential concern with the empirical results is that the analysis neglects the fact that leased aircraft return to the lessors between consecutive lessees. When a lease expires and the aircraft returns to the lessor, the data report this transaction. While in most cases, the lessor immediately transfers the aircraft to another lessee, the aircraft may stay with its lessor for some time between consecutive lessees. If these periods between lessees were frequent and lengthy, the differences in trading patterns and in utilization could be mismeasured. Similarly, the literature on investment (e.g., Cooper and Haltiwanger, 1993) traditionally assumes that firms must shut down operations for a fixed period when adjusting their capital stock. If there is a loss in output during this adjustment period, the estimated output gains could be overestimated.

To address this concern, I use another datafile in the database that reports the historical sequence of operators of each aircraft, with the relevant dates. From this datafile, I can recover the precise date on which each leased aircraft returned to the lessor before being transferred to its current operator/lessee, as reported in the cross-sectional data, and construct the time since the previous lease. Delays between consecutive leases are short—the average delay in this sample is only 28 days—which is further evidence that lessors are quick at redeploying aircraft. As a result, the difference between holding durations (the variable reported in Table 1 and used in Section 5.2) and the time since the previous operator is less than a month for leased aircraft.

Table 6 presents the results of a regression of the time since the previous operator on a set of covariates—the year in which the aircraft was built, aircraft model fixed-effects, engine-maker fixed-effects, and fixed-effects for each maker of the auxiliary power unit. The regression is identical to those used to construct the residuals plotted in Figure 5. Table 6 shows that the results are robust to this concern. The coefficient on the leased dummy in column (1) indicates that leased aircraft
Table 6: Robustness check 1: Leasing and Time since Previous Operator

<table>
<thead>
<tr>
<th>Time Since Previous Operator</th>
<th>(1)</th>
<th>(2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Age</td>
<td>8.689</td>
<td>8.856</td>
</tr>
<tr>
<td></td>
<td>(.292)</td>
<td>(.268)</td>
</tr>
<tr>
<td>Leased</td>
<td>-33.266</td>
<td>-20.208</td>
</tr>
<tr>
<td></td>
<td>(2.401)</td>
<td>(2.319)</td>
</tr>
<tr>
<td>Model Fixed Effects</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Carrier Fixed Effects</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>R²</td>
<td>.589</td>
<td>.684</td>
</tr>
<tr>
<td># Obs</td>
<td>3091</td>
<td>3091</td>
</tr>
</tbody>
</table>

Notes: This table presents a robustness check of the results on the differences in holding durations between leased and owned aircraft reported in Section 5.2. The dependent variable Time Since Previous Operator is the number of months since the aircraft was operated by a different per-passenger carrier than the carrier operating it in April 2003. The equations in specifications (1) and (2) further contain a constant, engine maker fixed-effects, and auxiliary-power-unit-maker fixed-effects (not reported). Robust standard errors in parenthesis.

I also checked the robustness of the results on utilization to the concerns of potential mismeasurement. Specifically, the cross-sectional dataset reports each aircraft’s cumulative hours flown since the delivery date, and I use the log of this variable as the dependent variable in a regression equation similar to equation (1). This regression may not perfectly measure differences between leased and owned aircraft since the dataset reports the ownership type—i.e., leased or owned—only in the cross-sectional data, and an aircraft’s ownership type could change throughout its “life.” Nonetheless, the regression would cast doubt on the validity of the estimated gains if owned aircraft had higher cumulative hours flown than leased aircraft. Column (1) of Table 7 shows that this is not the case: On average, leased aircraft have 6.1 percent more cumulative hours flown than owned ones. Moreover, because the ownership type appears only in the cross-sectional data, I restrict the sample to aircraft younger than ten years of age in specification (2): It is more likely that these young aircraft have been leased since their first flight. The results are almost identical: In this subsample, leased aircraft have 7.6 percent more cumulative hours flown than owned ones.

The sample in Column (1) is identical to the sample employed in the specifications of Table 3. Hence, the sample excludes all aircraft acquired by a carrier between May 2002 and April 2003 and all aircraft that are reported available “for lease” in April 2003 (see Section 5.1 and footnote 6 for the reasons for these exclusions). To check the robustness of the results to these exclusions, I repeat
Table 7: Robustness check 2: Leasing and Average Cumulative Hours Flown

<table>
<thead>
<tr>
<th></th>
<th>(1)</th>
<th>(2)</th>
<th>(3)</th>
<th>(4)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Log(Cumulative Hours Flown)</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Age</td>
<td>0.2265</td>
<td>0.4769</td>
<td>0.3286</td>
<td>0.3369</td>
</tr>
<tr>
<td></td>
<td>(0.0077)</td>
<td>(0.0157)</td>
<td>(0.0144)</td>
<td>(0.0153)</td>
</tr>
<tr>
<td>Age Squared</td>
<td>-0.0044</td>
<td>-0.241</td>
<td>-0.072</td>
<td>-0.078</td>
</tr>
<tr>
<td></td>
<td>(0.0002)</td>
<td>(0.0012)</td>
<td>(0.0004)</td>
<td>(0.0004)</td>
</tr>
<tr>
<td>Leased</td>
<td>0.0610</td>
<td>0.0764</td>
<td>0.0660</td>
<td>0.0627</td>
</tr>
<tr>
<td></td>
<td>(0.0139)</td>
<td>(0.0166)</td>
<td>(0.0276)</td>
<td>(0.0319)</td>
</tr>
<tr>
<td>Model Fixed Effects</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Carrier Fixed Effects</td>
<td>No</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>R²</td>
<td>0.833</td>
<td>0.763</td>
<td>0.690</td>
<td>0.731</td>
</tr>
<tr>
<td># Obs</td>
<td>2846</td>
<td>1434</td>
<td>3226</td>
<td>3226</td>
</tr>
</tbody>
</table>

Notes: This table presents a robustness check of the results on the differences in capacity utilization between leased and owned aircraft reported in Section 5. The dependent variable log(Cumulative Hours Flown) is the total number of hours flown since the delivery date of the aircraft. The sample of specification (1) is identical to the sample used in Table 3. The sample of specification (2) is restricted to all aircraft in the sample of specification (1) that are younger than ten years of age. The sample in specifications (3) and (4) additionally includes all aircraft that were acquired by a carrier between May 2002 and April 2003, and all aircraft reported available “for lease” in April 2003. See footnote 6 for a definition of “for lease” aircraft. The equations in specifications (1) to (4) further contain a constant, engine-maker fixed-effects, and auxiliary-power-unit-maker fixed-effects (not reported). Robust standard errors in parenthesis.

the regression of Column (1) including these aircraft in the sample. The leased dummy is now equal to one if the aircraft is owned by an operating lessor, and zero otherwise. Column (3) reports the results of this regression. The results are almost identical to those in Column (1), indicating that the sample restriction has no substantive effects on the estimates. Specification (4) further adds current carrier fixed-effects to the regression equation and, again, the results are almost identical.

In summary, Table 7 shows that the estimate of the output difference between leased and owned aircraft is robust to potential sample selection biases. Furthermore, the results reported in Table 7 show that the output difference is stable over time and is not specific to the period of the cross-sectional data—i.e., April 2002-March 2003—in which the airline industry faced a downturn.

7 Concluding Remarks

This paper examines the link between the efficiency of aircraft transactions in secondary markets and the efficiency of production of final output—i.e., flights. I argue that aircraft lessors operate as intermediaries that reduce frictions in aircraft trading, and I construct a model of trading in durable capital to understand the role of lessors when trading is subject to frictions. I then use data

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9The fraction of aircraft owned by lessors that has been parked for more than one year is 5.69 percent. The corresponding fraction for owned aircraft is 6.39 percent.
on commercial aircraft to provide empirical evidence on the two main implications of the model: 1) leased aircraft trade more frequently than owned aircraft; and 2) leased aircraft have a higher capacity utilization than owned aircraft. The results indicate that when transaction costs prevent the efficiency of allocation via decentralized trade, firms develop institutions and adopt contractual arrangements that reduce these inefficiencies. The empirical analysis reveals considerable gains due to the particular institution analyzed—i.e., aircraft leasing.

As noted in the Introduction, the aircraft-leasing business started just a few years after the Airline Deregulation Act. I suggest that greater competition as a result of the Act increased the importance of aircraft reallocation, and, therefore, the need for trading intermediaries became stronger. The change in market structure also affected the fragmentation of airline markets, with mergers and the emergence of smaller carriers serving new markets. Aircraft leasing probably also emerged in response to the entry of these new carriers, in turn facilitating their entry. In Figure 8, I superimpose the annual coefficient of variation of fleet size on the fraction of new aircraft bought by lessors, as in Figure 2. The two series are highly correlated. How aircraft leasing affects airline fleet compositions and airline market structures are interesting questions left for future research.
APPENDICES

A Tests of First-Order Stochastic Dominance (FOSD)

Let $X_Z$ and $X_W$ be random variables with corresponding cdfs $G_Z (\cdot)$ and $G_W (\cdot)$. $G_Z (\cdot)$ first-order stochastically dominates $G_W (\cdot)$ if

$$G_Z (x) \leq G_W (x) \text{ for all } x \text{ and}$$

$$G_Z (x) < G_W (x) \text{ for some } x.$$

Let the empirical distributions be defined by

$$\hat{G}_i (x) = \frac{1}{N_i} \sum_{j=1}^{N_i} 1 \{ X_i \leq x \} \text{ for } i = Z, W,$$

where $1 \{ \cdot \}$ denotes the indicator function, and $N_i$ are the number of observations from distribution $G_i$. Using the empirical cdfs, I perform tests of the hypotheses:

$$G_Z (x) = G_W (x), \forall x \in R \quad (5)$$

and

$$G_Z (x) \leq G_W (x), \forall x \in R. \quad (6)$$

The test of (5) is conducted using the Kolmogorov-Smirnov test statistics:

$$S_1 = \left( \frac{N_Z N_W}{N_Z + N_W} \right)^{1/2} \sup_a | \hat{G}_Z (a) - \hat{G}_W (a) |. \quad (7)$$

The test of (6) is conducted using the procedure introduced by Davidson and Duclos (2000): Using a predetermined grid of points $a_j$ for $j = 1, \ldots, m$, we construct the $t$ statistics

$$t (a_j) = \frac{\hat{G}_Z (a_j) - \hat{G}_W (a_j)}{\sqrt{\left( \frac{\hat{G}_Z (a_j) - \hat{G}_Z (a_j)^2}{N_Z} \right) + \left( \frac{\hat{G}_W (a_j) - \hat{G}_W (a_j)^2}{N_W} \right)}} \quad (8)$$

to test $H_1$ (dominance) against $H_2$ (no restriction). The hypothesis $H_1$ is rejected against the unconstrained alternative $H_2$ if any of the $t$ statistics is significant with the positive sign, where significance is determined asymptotically by the critical values $d_{a,m,\infty}$ of the Studentized Modulus (SMM) distribution with $m$ and infinite number of degrees of freedom at the $\alpha\%$ confidence level. In practice, this implies that we fail to reject the hypothesis of $G_Z (\cdot)$ first-order stochastically dominating $G_W (\cdot)$ if

$$-t (a_j) > d_{a,m,\infty} \text{ for some } j \text{ and}$$

$$t (a_j) < d_{a,m,\infty} \text{ for all } j.$$

An undesirable feature of the Davidson and Duclos test is that the comparisons made at a fixed number of arbitrary chosen points introduce the possibility of test inconsistency. Barrett and Donald (2003) follow McFadden (1989) and modify the Kolmogorov-Smirnov test to construct the test statistics

$$\hat{S}_1 = \left( \frac{N_Z N_W}{N_Z + N_W} \right)^{1/2} \sup_a \left( \hat{G}_Z (a) - \hat{G}_W (a) \right). \quad (9)$$

Barrett and Donald show that we can compute p-values by $\exp \left( -2 \left( \hat{S}_1 \right)^2 \right)$.

I perform these tests of FOSD on the distributions of holding durations of leased and owned aircraft, and on the distributions of flying hours and efficiency of lessees and owners. I now describe the details for each case.
Table 8: Tests of FOSD for Holding Durations

<table>
<thead>
<tr>
<th>Percentile</th>
<th>5</th>
<th>10</th>
<th>15</th>
<th>20</th>
<th>25</th>
<th>30</th>
<th>35</th>
<th>40</th>
<th>45</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td>DURATION</td>
<td>7</td>
<td>14</td>
<td>22</td>
<td>29</td>
<td>37</td>
<td>45</td>
<td>52</td>
<td>59</td>
<td>69</td>
<td>76</td>
</tr>
<tr>
<td>t(a_j)</td>
<td>-7.24</td>
<td>-9.36</td>
<td>-10.20</td>
<td>-11.00</td>
<td>-11.17</td>
<td>-11.90</td>
<td>-12.21</td>
<td>-12.54</td>
<td>-12.51</td>
<td>-13.16</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Percentile</th>
<th>55</th>
<th>60</th>
<th>65</th>
<th>70</th>
<th>75</th>
<th>80</th>
<th>85</th>
<th>90</th>
<th>95</th>
<th>99</th>
</tr>
</thead>
<tbody>
<tr>
<td>DURATION</td>
<td>90</td>
<td>105</td>
<td>119</td>
<td>130</td>
<td>143</td>
<td>157</td>
<td>178</td>
<td>211</td>
<td>250</td>
<td>300</td>
</tr>
</tbody>
</table>

Notes: This table presents the results of the test of FOSD developed by Davidson and Duclos (2000). Panel A refers to the distributions of holding durations of leased and owned aircraft, and Panel B refers to the distributions of hours flown of leased and owned aircraft. Percentile corresponds to the percentile of the pooled distribution of holding durations at which the statistics in equation (8) are calculated. Duration and Hours Flown are the values of the holding duration and flying hours, respectively, corresponding to the Percentile reported above them. t(a_j) is the value of the statistics reported in equation (8).

A.1 Holding Durations

I perform separate tests of FOSD on the pairs of distributions in each panel of Figure 5: 1) the distributions of unconditional holding durations of leased and owned aircraft (the left panel); 2) the distributions of residual durations when carrier fixed-effects are not included in the censored regression; and 3) the distributions of residual durations when carrier fixed-effects are included in the censored regression.

1. The Kolmogorov-Smirnov test rejects the null hypothesis of equality of distributions between the durations of owned aircraft and leased aircraft. The asymptotic p-value is $1.4 \times 10^{-38}$.

As for Davidson and Duclos’ test, I choose a grid of equally spaced percentiles of the pooled distribution of holding durations, starting from the fifth percentile, with a step of five percentiles, and ending at the 95th percentile. This results in $m = 19$ points. The critical values, tabulated in Stoline and Ury (1979), are $d_{\alpha,m,\infty} = 4.018$ for $\alpha = 1$, $d_{\alpha,m,\infty} = 3.615$ for $\alpha = 5$ and $d_{\alpha,m,\infty} = 3.425$ for $\alpha = 10$. Panel A of Table 8 presents values of the t statistics. The results show that the distribution of holding durations of owned aircraft first-order stochastically dominates the distribution of holding durations of leased aircraft, as all t statistics are negative and the absolute value of the largest one is 14.97 $> 4.018$.

As for Barrett and Donald’s test, the distribution of holding durations of owned aircraft lies everywhere below the distribution of holding durations of leased aircraft. Hence, the probability of rejection of the null hypothesis of stochastic dominance is zero.

2. Since residual durations are estimated rather than observed, the sampling variability of the estimated parameters must be taken into account when constructing the distributions of the test statistics. Hence, I bootstrap the p-values of the test statistics, following the procedure described in Abadie (2001). Abadie also provides a set of weak regularity conditions to imply
consistency. These assumptions do not require continuity of the distributions and, in particular, are satisfied by distributions with a probability mass.

The Kolmogorov-Smirnov test (7) rejects the null hypothesis of equality of distributions between the durations of owned aircraft and leased aircraft. The \( p \)-value is 0.

As for Davidson and Duclos’ test, in each repetition, I choose a grid of equally spaced percentiles of the pooled distribution of residual durations, starting from the fifth percentile, with a step of five percentiles, and ending at the 95th percentile. I compute the statistics in equation (8) at each of the \( m = 19 \) points. I use 1000 repetitions. The \( p \)-value is .985.

As for Barrett and Donald’s test, in each repetition, I compute the statistics in equation (9) using a grid of 1000 equally spaced points between the first and the 99th percentile of the distribution of estimated residual durations. I use 1000 repetitions. The \( p \)-value is 1.

3. The Kolmogorov-Smirnov test of equation (7) rejects the null hypothesis of equality of distributions between the durations of owned aircraft and leased aircraft. The \( p \)-value is 0.

As for Davidson and Duclos’ test, in each repetition, I choose a grid of equally spaced percentiles of the pooled distribution of residual durations, starting from the fifth percentile, with a step of five percentiles, and ending at the 95th percentile. I compute the statistics in equation (8) at each of the \( m = 19 \) points. I use 1000 repetitions. The \( p \)-value is .917.

As for the Barrett and Donald’s test, in each repetition, I compute the statistics in equation (9) using a grid of 1000 equally spaced points between the first and the 99th percentile of the distribution of estimated residual durations. I use 1000 repetitions. The \( p \)-value is .994.

A.2 Flying Hours and Efficiency

I perform separate tests of FOSD on the following pairs of distributions: 1) the distributions of flying hours of leased and owned aircraft; 2) the distributions of efficiency of operators of leased and owned aircraft estimated from equations (2) and (3) when carrier fixed-effects are not included in the empirical model; 3) the distributions of efficiency of operators of leased and owned aircraft estimated from equations (2) and (3) when carrier fixed-effects are included in the empirical model; and 4) the top 15 percent of the distributions of efficiency of operators of leased and owned aircraft estimated from equations (2) and (3) when carrier fixed-effects are included in the empirical model. Since efficiency is estimated, I bootstrap the \( p \)-values of the test statistics.

1. The Kolmogorov-Smirnov test rejects the null hypothesis of equality between the distributions of flying hours of owned aircraft and of leased aircraft. The asymptotic \( p \)-value is \( 1.5 \times 10^{-10} \).

As for Davidson and Duclos’ test, I choose a grid of equally spaced percentiles of the pooled distribution of flying hours, starting from the fifth percentile, with a step of five percentiles, and ending at the 95th percentile. This results in \( m = 19 \) points. The critical values, tabulated in Stoline and Ury (1979), are \( d_{\alpha,m,\infty} = 4.018 \) for \( \alpha = 1 \), \( d_{\alpha,m,\infty} = 3.615 \) for \( \alpha = 5 \) and \( d_{\alpha,m,\infty} = 3.425 \) for \( \alpha = 10 \). Panel B of Table 8 presents values of the \( t \) statistics. The results show that the distribution of holding durations of owned aircraft first-order stochastically dominates the distribution of holding durations of leased aircraft, as all \( t \) statistics are negative and the absolute value of the largest one is 7.079 > 4.018.

As for the Barrett and Donald’s test, the distribution of holding durations of owned aircraft lies everywhere below the distribution of holding durations of leased aircraft. Hence, the probability of rejection of the null hypothesis of stochastic dominance is zero.
2. The Kolmogorov-Smirnov test of the equality of distributions rejects the null hypothesis of equal distributions (the bootstrapped $p$-value is equal to 0).

As for Davidson and Duclos’ test, in each repetition, I choose a grid of equally spaced percentiles of the pooled distribution of estimated efficiencies, starting from the fifth percentile, with a step of five percentiles, and ending at the 95th percentile. I compute the statistics in equation (8) at each of the $m = 19$ points. I use 1000 repetitions. The $p$-value is equal to .958, so the test fails to reject the null hypothesis that the distribution of productivity of lessees first-order stochastically dominates the distribution of owners’ productivity.

The Barrett and Donald’s test also fails to reject the null hypothesis of dominance. The bootstrapped $p$-value is .989.

3. The Kolmogorov-Smirnov test of the equality of distributions rejects the null hypothesis of equal distributions (the bootstrapped $p$-value is equal to .010).

As for Davidson and Duclos’ test, in each repetition, I choose a grid of equally spaced percentiles of the pooled distribution of estimated efficiencies, starting from the fifth percentile, with a step of five percentiles, and ending at the 95th percentile. I compute the statistics in equation (8) at each of the $m = 19$ points. I use 1000 repetitions. The $p$-value is equal to .940, so the test fails to reject the null hypothesis that the distribution of productivity of lessees first-order stochastically dominates the distribution of owners’ productivity.

The Barrett and Donald’s test also fails to reject the null hypothesis of dominance. The bootstrapped $p$-value is .973.

4. The Kolmogorov-Smirnov test of the equality of distributions does not reject the null hypothesis of equal distributions (the bootstrapped $p$-value is equal to .131).

As for Davidson and Duclos’ test, in each repetition, I choose a grid of equally spaced percentiles of the pooled distribution of estimated efficiencies above the 85th percentile, starting from the fifth percentile, with a step of ten percentiles, and ending at the 95th percentile. I compute the statistics in equation (8) at each of the $m = 9$ points. I use 1000 repetitions. The $p$-value is equal to .474, so the test rejects the null hypothesis that the distribution of productivity of lessees first-order stochastically dominates the distribution of owners’ productivity.

The Barrett and Donald’s test also rejects the null hypothesis of dominance. The bootstrapped $p$-value is .455.

B Omitted Proofs

Before proving all Propositions, I introduce some general notation, derive the value functions and prove two lemmas that I use in several proofs.

B.1 Value Functions

Let $V_O (z, s)$ be the value of a carrier with long-term efficiency $z$ and temporary shocks $s$ that owns and operates an aircraft (I will drop $\alpha$ from the arguments of the value functions if it does not generate ambiguity); $V_L (z, s)$ the value of a carrier with long-term efficiency $z$ and temporary shocks $s$ that leases an aircraft; and $W (z, s)$ the value of a carrier with long-term efficiency $z$ and temporary
shocks $s$ that does not operate (neither owns nor leases) any aircraft. $V_O(z, 1)$ satisfies:

\[
    rV_O(z, 1) = \frac{z + \mu \left( \max \{ V_O(z, 0), W(z, 0) + p - T \} - V_O(z, 1) \} +}{r + \mu + \alpha} 
\]

\[
    \alpha \int \left( \max \{ V_O(x, 1), W(x, 1) + p - T - V_O(z, 1) \} \right) dF(x)
\]

where $T = \tau_p$. Equation (10) has the usual asset-pricing interpretation. A carrier in state $(z, 1)$ has current output/revenue equal to $z$. Then, in any instant, at most one of two events can happen: 1) At rate $\mu$, the carrier receives a temporary shock, and the carrier decides whether to park the aircraft (in which case, it suffers a capital loss equal to $V_O(z, 0) - V_O(z, 1)$) or to sell it (in which case, the capital loss is equal to $W(z, 0) + p - T - V_O(z, 1)$). 2) At rate $\alpha$, the carrier receives a new draw of the efficiency parameter $z$, so the firm takes expectation over its optimal future actions. After learning its new efficiency, the carrier chooses between continuing to operate the aircraft it owns (in which case, it enjoys a capital gain equal to $V_O(x, 1) - V_O(z, 1)$), or lease another one, with capital gain equal to $V_L(x, 1) + p - T - V_O(z, 1)$. (In principle, the firm could also sell the aircraft and exit (capital gain equal to $V_L(x, 1) + p - T - V_O(z, 1)$. However, this, almost trivially, is never optimal, so it is omitted.)

Similarly, we can derive

\[
    rV_L(z, 1) = \frac{z - l + \mu \left( \max \{ V_L(z, 0), W(z, 0) \} - V_L(z, 1) \} +}{r + \mu + \alpha} 
\]

\[
    \alpha \int \left( \max \{ V_O(x, 1) - p, V_L(x, 1), W(x, 1) \} - V_L(z, 1) \right) dF(x).
\]

The interpretation of equation (11) is now simple. The main differences between $V_L(z, 1)$ and $V_O(z, 1)$ are that $V_L(z, 1)$ contains the per-period lease rate $l$ as a flow cost, and that there are no transaction costs in the expression for $V_L(z, 1)$.

Similarly, we can derive

\[
    rV_O(z, 0) = \frac{\lambda \left( \max \{ V_O(z, 1), W(z, 1) + p - T \} - V_O(z, 0) \} +}{r + \mu + \alpha} 
\]

\[
    rV_L(z, 0) = \frac{-l + \lambda \left( \max \{ V_O(z, 1) - p, V_L(z, 1), W(z, 1) \} - V_L(z, 0) \} +}{r + \mu + \alpha} 
\]

\[
    rW(z, 1) = \frac{\mu \left( W(z, 0) - W(z, 1) \right) +}{r + \mu + \alpha} 
\]

\[
    \alpha \int \left( \max \{ V_O(x, 1) - p, V_L(x, 1), W(x, 1) \} - W(z, 1) \right) dF(x),
\]

\[
    rW(z, 0) = \frac{\lambda \left( \max \{ V_O(z, 1) - p, V_L(z, 1), W(z, 1) \} - W(z, 0) \} +}{r + \mu + \alpha} 
\]

\[
    \alpha \int \left( \max \{ V_O(x, 1) - p, V_L(x, 1), W(x, 1) \} - W(z, 0) \right) dF(x).
\]

**B.2 Two Lemmas**

**Lemma 6** $V_O(z, 1) - W(z, 1)$ and $V_L(z, 1) - W(z, 1)$ are increasing in $z$.

**Proof.** I prove that $V_O(z, 1) - W(z, 1)$ is increasing in $z$. Using equations (10) and (14), we obtain:

\[
    V_O(z, 1) - W(z, 1) = \frac{z + \mu \left( \max \{ V_O(z, 0), W(z, 0) + p - T \} - W(z, 0) \} +}{r + \mu + \alpha} + J
\]

where $J = \frac{\alpha \int \max \{ V_O(x, 1), W(x, 1) + p - T \} dF(x)}{r + \mu + \alpha} - \frac{\alpha \int \max \{ V_O(x, 1) - p, V_L(x, 1), W(x, 1) \} dF(x)}{r + \mu + \alpha}$ is a constant that does not depend on $z$. Now there are two cases, depending on the value of $\max \{ V_O(z, 0), W(z, 0) + p - T \}$.

(a) If $\max \{ V_O(z, 0), W(z, 0) + p - T \} = W(z, 0) + p - T$, then $V_O(z, 1) - W(z, 1) = \frac{z + \mu (p - T)}{r + \mu + \alpha} + J$ is increasing in $z$. 
(b) If \( \max \{ V_O(z,0), W(z,0) + p - T \} = V_O(z,0) \), we can use equation (12) to obtain
\[
V_O(z,0) = \frac{\lambda \max \{ V_O(z,1), W(z,1) + p - T \}}{r + \lambda} = \frac{\lambda V_O(z,1)}{r + \lambda}
\]
since, if it was optimal to keep the aircraft when \( s = 0 \), it is optimal to keep it when \( s = 1 \). Now there are two subcases, depending on the value of \( W(z,0) \).

(b1) If \( W(z,0) = \frac{\lambda \max \{ V_O(z,1) - p, W(z,1) \} \lambda V_O(z,1) - p}{r + \lambda} \), then
\[
V_O(z,1) - W(z,1) = \frac{z + \mu \left( \frac{\lambda V_O(z,1) - p}{r + \lambda} - \frac{\lambda V_O(z,1) - p}{r + \lambda} \right)}{r + \mu + \alpha} + J = \frac{z + \lambda \frac{\mu p}{(r+\lambda)}}{r + \mu + \alpha} + J
\]
is increasing in \( z \).

(b2) If \( W(z,0) = \frac{\lambda \max \{ V_O(z,1) - p, W(z,1) \} \lambda V_O(z,1) - p}{r + \lambda} \), then
\[
V_O(z,1) - W(z,1) = \frac{z + \mu \left( \frac{\lambda V_O(z,1) - p}{r + \lambda} - \frac{\lambda V_O(z,1) - p}{r + \lambda} \right)}{r + \mu + \alpha} + J = \left( \frac{z}{r + \mu + \alpha} + J \right) \frac{(r + \lambda)(r + \alpha + \mu)}{r + \mu \frac{r}{r+\lambda} + \alpha}
\]
is increasing in \( z \). This proves that \( V_O(z,1) - W(z,1) \) is increasing in \( z \).

I now prove that \( V_L(z,1) - W(z,1) \) is increasing in \( z \). Using equations (11) and (14), we obtain
\[
V_L(z,1) - W(z,1) = \frac{z - \frac{\mu}{r + \mu + \alpha}}{r + \mu + \alpha},
\]
which is increasing in \( \alpha \).

**Lemma 7** At the time they acquire an aircraft, for all carriers with the same volatility \( \alpha \), \( V_L(z,1) > V_O(z,1) - p \) or \( V_L(z,1) < V_O(z,1) - p \) or \( V_L(z,1) = V_O(z,1) - p \).

**Proof.** Suppose not. Suppose that there are two carriers \( z' \) and \( z'' \) that are acquiring an aircraft, and \( V_L(z',1) > V_O(z',1) - p \) and \( V_L(z'',1) = V_O(z'',1) - p \). (Since \( V_L(z,1) \) and \( V_O(z,1) \) are continuous function, if \( V_L(z,1) < V_O(z,1) - p \) for some \( z \), then there exists a \( z'' \) such that \( V_L(z'',1) = V_O(z'',1) - p \).) The proof proceeds in three steps.

**Step 1:** Note that
\[
V_L(z'',1) = \frac{z'' - l + \mu W(z'',0)}{r + \mu + \alpha} + \alpha \int \max \{ V_O(x,1) - p, V_L(x,1), W(x,1) \} dF(x)
\]
\[
= \frac{z'' - l + \mu \lambda V_L(z'',1)}{r + \mu + \alpha} + \alpha \int \max \{ V_O(x,1) - p, V_L(x,1), W(x,1) \} dF(x)
\]
\[
= \frac{z'' - l}{r + \mu \frac{r}{r+\lambda} + \alpha} + \alpha \int \max \{ V_O(x,1) - p, V_L(x,1), W(x,1) \} dF(x)
\]
Moreover
\[
\max \{ V_O(z'',0), W(z'',0) + p - T \}
\]
\[
= \max \left\{ \frac{\lambda \max \{ V_O(z'',1), V_L(z'',1) + p - T \}}{\lambda + r}, \lambda \max \{ V_O(z'',1) - p, V_L(z'',1) \} + p - T \right\}
\]
\[
= \max \left\{ \frac{\lambda V_O(z'',1)}{\lambda + r}, \frac{\lambda V_O(z'',1) - p}{\lambda + r} + p - T \right\} = \frac{\lambda V_O(z'',1)}{\lambda + r}
\]
since \( \tau > \frac{r}{\lambda + r} \). Thus, substituting the above equality into equation (10), we obtain
\[
V_O(z'',1) = \frac{z'' + \mu \lambda V_O(z'',1)}{r + \mu + \alpha} + \alpha \int \max \{ V_O(x,1), W(x,1) + p - T \} dF(x)
\]
\[
= \frac{z''}{r + \mu \frac{r}{r+\lambda} + \alpha} + \alpha \int \max \{ V_O(x,1), W(x,1) + p - T \} dF(x)
\]
Hence, \( V_L (z'', 1) = V_O (z'', 1) - p \) corresponds to
\[
\frac{z'' - l}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1) - p, V_L (x, 1), W (x, 1) \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha} = \frac{z''}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1), W (x, 1) + p - T \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha} - p,
\]
which is independent of \( z'' \). Thus, the derivative of \( V_L (z'', 1) - V_O (z'', 1) \) is equal to zero at any \( z'' \) such that \( V_L (z'', 1) = V_O (z'', 1) - p \).

**Step 2:** Consider now \( z' \). Using equation (11), we obtain that:
\[
V_L (z', 1) = \frac{z' - l}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1) - p, V_L (x, 1), W (x, 1) \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha}.
\]
Moreover
\[
\max \{ V_O (z', 0), W (z', 0) + p - T \} = \max \left\{ \lambda \max \{ V_O (z', 1), V_L (z', 1) + p - T \}, \lambda \max \{ V_O (z', 1) - p, V_L (z', 1) \} + p - T \right\} = \lambda \max \{ V_L (z', 1), \frac{\lambda V_O (z', 1)}{\lambda + r} + p - T \}.
\]
Suppose that \( \max \{ V_O (z', 0), W (z', 0) + p - T \} = \frac{\lambda V_O (z', 1)}{\lambda + r} \). By the same argument used for \( z'' \), we obtain that \( V_L (z', 1) > V_O (z', 1) - p \) corresponds to
\[
\frac{z' - l}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1) - p, V_L (x, 1), W (x, 1) \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha} > \frac{z'}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1), W (x, 1) + p - T \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha} - p,
\]
which is independent of \( z' \). Thus, the derivative of \( V_L (z', 1) - V_O (z', 1) \) is equal to zero at any \( z' \) such that \( V_L (z', 1) > V_O (z', 1) - p \) and \( \max \{ V_O (z', 0), W (z', 0) + p - T \} = \frac{\lambda V_O (z', 1)}{\lambda + r} \).

**Step 3:** Consider again \( z' \) and suppose that \( \max \{ V_O (z', 0), W (z', 0) + p - T \} = \frac{\lambda V_O (z', 1)}{\lambda + r} + p - T \). Thus
\[
V_O (z', 1) - p = \frac{z' + \mu \left( \frac{\lambda V_L (z', 1)}{\lambda + r} + p - T \right)}{r + \mu + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1), W (x, 1) + p - T \} dF (x)}{r + \mu + \alpha}.
\]
Using equation (11) and the above equality, \( V_L (z', 1) > V_O (z', 1) - p \) corresponds to
\[
\frac{z' - l}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1) - p, V_L (x, 1), W (x, 1) \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha} > \frac{z' + \mu (p - T)}{r + \mu \frac{r}{r + \lambda} + \alpha} + \frac{\alpha \int \max \{ V_O (x, 1), W (x, 1) + p - T \} dF (x)}{r + \mu \frac{r}{r + \lambda} + \alpha} - \frac{r + \alpha + \mu}{r + \mu + \alpha} p,
\]
which again is independent of \( z' \). This, together with Step 2, implies that the derivative of \( V_L (z', 1) - V_O (z', 1) \) is equal to zero at any \( z' \) such that \( V_L (z', 1) > V_O (z', 1) - p \). However, it is impossible that the function \( V_L (z, 1) - V_O (z, 1) \) is larger than \( p \) and has derivative equal to zero at any \( z' \), and is equal to \( p \) and has derivative equal to zero at any \( z'' \), since the function is continuous.

The proof of the case of two carriers \( z' \) and \( z'' \) that are acquiring an aircraft, and \( V_L (z', 1) < V_O (z', 1) - p \) and \( V_L (z'', 1) = V_O (z'', 1) - p \) is identical and, therefore, omitted.
B.3 Proof of Proposition 1

I first show that all carriers with no temporary shock \((s = 1)\) are indifferent between leasing and owning aircraft. Using the equations (10) and (11), we obtain:

\[(r + \mu + \alpha) \left( V_L(z, 1) - (V_O(z, 1) - p) \right) = -l + rp.\]

Since lessors are competitive and \(l = rp\), then \(V_L(z, 1) = V_O(z, 1) - p\).

I now determine the equilibrium allocation. Consider the case of a carrier that leases an aircraft. Using equations (11) and (14),

\[V_L(z, 1) - W(z, 1) = z - l(r + \mu + \alpha).\]

This implies that all carriers with \(s = 1\) and with efficiency \(z \geq \hat{z} = l\) operate aircraft, while carriers with \(z \leq \hat{z}\) do not. Moreover, since there are no transaction costs, all carriers with a temporary shock dispose of their aircraft.

Thus, the cutoff value \(\hat{z}\) satisfies

\[X = (1 - S_0) (1 - F(\hat{z}))\],

(16)

where \(S_0\) is the mass of carriers with a temporary shock. Equation (16) says that, in equilibrium, the mass of aircraft \(X\) is equal to the fraction of carriers with no temporary shock whose efficiency is higher than cutoff \(\hat{z}\). In order to determine \(S_0\), we can use the equality of stocks and flows in an interval of time of length \(\varepsilon\):

\[S_0 = (1 - S_0) \mu \varepsilon + S_0 (1 - \lambda \varepsilon) = \frac{\mu}{\mu + \lambda}\].

The above equation says that, in steady state, the mass of carriers with a temporary shock \(S_0\) is equal to the sum of the mass of carriers that had no temporary shock in the previous instant and just received a temporary shock, plus the mass of carriers whose temporary shock persists.

The marginal carrier \(\hat{z}\) is indifferent between operating an aircraft or not—i.e., \(V_L(\hat{z}, 1) = W(\hat{z}, 1)\). Thus, \(l = \hat{z}\) and \(p = \hat{z}\).

B.4 Proof of Corollary 2

Since Corollary 2 is a special case of Proposition 4, I delay its proof to the Proof of Proposition 4.

B.5 Proof of Proposition 3

(i) I now derive the value \(z^*\) of a carrier that is indifferent between acquiring an aircraft or not. Using the value functions (11) and (14), we obtain that \(z^*\) satisfies

\[V_O(z^*, 1) - p = W(z^*, 1).\]  

(17)

By Lemma 6, \(V_O(z, 1) - W(z, 1)\) is increasing. Thus, all carriers with efficiency \(z \geq z^*\) and \(s = 1\) acquire an aircraft, while carriers with \(z \leq z^*\) do not.

Consider, now, a carrier that owns an aircraft and receives a temporary shock. It is indifferent between selling the aircraft and operating it if its efficiency \(z^{**}\) satisfies \(W(z^{**}, 0) + p - T = V_O(z^{**}, 0)\). Note that

\[V_O(z^{**}, 0) = \frac{\lambda V_O(z^{**}, 1)}{\lambda + r}\]  

(18)

since, if the carrier is staying in today, it stays in once his temporary shock disappears. Moreover,

\[W(z^{**}, 0) = \frac{\lambda \max \{V_O(z^{**}, 1) - p, V_L(z^{**}, 1) - W(z^{**}, 1)\}}{\lambda + r} = \frac{\lambda \max \{V_O(z^{**}, 1) - p, W(z^{**}, 1)\}}{\lambda + r}\]
where the second equality follows because we are assuming that some carriers are owning aircraft. I now prove \( V_O(z^{**},1) - p, W(z^{**},1) = W(z^{**},1) \). Suppose not, then,

\[
\frac{\lambda V_O(z^{**},1)}{\lambda + r} = W(z^{**},0) + p - T = \frac{\lambda (V_O(z^{**},1) - p)}{\lambda + r} + p - T
\]

where the first equality uses the definition of \( z^{**} \) and equation (18). However, this is impossible since \( \tau > \frac{r}{\lambda + r} \). Thus, \( W(z^{**},0) + p - T = V_O(z^{**},0) \) is equivalent to

\[
V_O(z^{**},1) - W(z^{**},1) = \frac{\lambda + r}{\lambda} (p - T).
\] (19)

Consider, now, a carrier with no temporary shock that owns an aircraft and is indifferent between selling it and operating it. The efficiency \( z^{**} \) of this carrier satisfies:

\[
W(z^{**},1) + p - T = V_O(z^{**},1).
\] (20)

I now prove that \( z^* > z^{**} > z^{**} \). Using equations (17), (19) and (20), we obtain:

\[
V_O(z^*,1) - W(z^*,1) = p > V_O(z^{**},1) - W(z^{**},1) = \frac{\lambda + r}{\lambda} (p - T) > V_O(z^{**},1) - W(z^{**},1) = p - T
\]

since \( \tau > \frac{r}{\lambda + r} \). Since, by lemma 6, \( V_O(z,1) - W(z,1) \) is increasing, this proves part (i).

(ii) By Lemma 7, the proof is identical to the proof of Proposition 1.

### B.6 Proof of Proposition 4

Consider two aircraft, one owned and the other leased. The owned aircraft is traded at rate \( \alpha_l F(z^{**}) + \mu H_O(z^{**}) \), where \( H_O(z,1) \) is the endogenous cumulative distribution function of efficiency \( z \) of owners with no temporary shock. To calculate \( H_O(z^{**},1) \), consider the pdf \( h_O(z,s) \) and a small interval of time of length \( \epsilon \). Up to terms in \( o(\epsilon) \), in the interval \( z^{**} \leq z < z^* \) the distribution \( h_O(z,1,\cdot) \) evolves from time \( t \) to time \( t + \epsilon \) according to:

\[
h_O(z,1,t + \epsilon) = \alpha_l \epsilon f(z,t) + (1 - \alpha_l \epsilon - \mu \epsilon) h_O(z,1,t)
\]

Substituting and taking the limit for \( \epsilon \to 0 \), in steady state \( H_O(z^{**},1) \) satisfies:

\[
H_O(z^{**},1) = \frac{\alpha_l (F(z^{**}) - F(z^{**^*}))}{\alpha_l + \mu}.
\] (21)

The leased aircraft is traded at rate \( \alpha_h F(z^*) + \mu \). Since the stochastic processes of \( z \) and \( s \) are Poisson processes, the resulting distribution functions of holding durations of owned aircraft and leased aircraft are exponentials with parameters \( \alpha_l F(z^{**}) + \mu H_O(z^{**}) \) and \( \alpha_h F(z^*) + \mu \), respectively. Since \( \alpha_h > \alpha_l, z^* > z^{**}, H_O(z^{**}) < 1 \), the Proposition follows.

If \( \tau = 0 \), then \( z^* = z^{**} \) and \( z^{**} = +\infty \). Hence, Corollary 2 follows too.

### B.7 Proof of Proposition 5

To prove part (i), note that no leased aircraft is parked. Instead, all owners with efficiency \( z \geq z^{**} \) park the aircraft when they receive a temporary shock.

To prove part (ii), only carriers with no temporary shock fly the aircraft. I now prove that \( z^* \leq l \). The marginal carrier acquiring an aircraft has efficiency \( z^* \) satisfying: \( W(z^*,1,\alpha_l) = V_O(z^*,1,\alpha_l) - p \). Since this carrier could have leased instead, it must be that \( V_O(z^*,1,\alpha_l) - p \geq V_L(z^*,1,\alpha_l) \).
Hence, $W(z^*, 1, \alpha_\ell) \geq V_L(z^*, 1, \alpha_\ell)$. Using (11) and (14), we obtain that $W(z^*, 1, \alpha_\ell) \geq V_L(z^*, 1, \alpha_\ell)$ corresponds to $z^* \leq l$.

Conditional on $z \geq l$, the distributions of efficiency of owners and lessees are identical. Moreover, all operators with efficiency $z^{**} \leq z < l$ are owners. Hence, conditional on flying, the efficiency of lessees is higher than the efficiency of carriers.

Combining (i) and (ii), the first statement of the Proposition follows too.

### B.8 Equilibrium

An equilibrium in which high-volatility carriers lease and low-volatility carriers own aircraft requires that the following conditions hold:

1. Leasing rate is equal to:
   \[ l = (r + m)p. \tag{22} \]

2. The marginal lessee has productivity equal to the lease rate $l$:
   \[ V_L(l, 1, \alpha_h) = W(l, 1, \alpha_h). \tag{23} \]

3. All high-volatility carriers prefer to lease: for $z \geq l$
   \[ V_L(z, 1, \alpha_h) > V_O(z, 1, \alpha_h) - p, \tag{24} \]
   and all low-volatility carriers prefer to own: for $z \geq z^*$
   \[ V_L(z, 1, \alpha_\ell) < V_O(z, 1, \alpha_\ell) - p. \tag{25} \]

4. The marginal carrier acquiring an aircraft has efficiency $z^*$ satisfying:
   \[ V_O(z^*, 1, \alpha_\ell) - p = W(z^*, 1, \alpha_\ell). \tag{26} \]

5. The marginal carrier selling an owned aircraft has efficiency $z^{**}$ satisfying:
   \[ V_O(z^{**}, 0, \alpha_\ell) = W(z^{**}, 0, \alpha_\ell) + p - T. \tag{27} \]

6. The marginal carrier selling an owned aircraft has efficiency $z^{***}$ satisfying:
   \[ V_O(z^{***}, 1, \alpha_\ell) = W(z^{***}, 1, \alpha_\ell) + p - T. \tag{28} \]

7. The mass $1 - \omega$ of low-volatility carriers is composed by the mass $X - X_L$ of carriers that operate an aircraft, the mass $SS_0$ of carriers with no aircraft and no temporary shock, and the mass $L_0$ of carriers with no aircraft and a temporary shock:
   \[ 1 - \omega = X - X_L + SS_0 + L_0, \tag{29} \]
   \[ SS_0 = SS_0 (1 - \alpha_\ell \mu - \mu) + SS_0 \alpha_\ell \epsilon F(z^*) + \lambda \epsilon L_0 + (X - X_L) \alpha_\ell \epsilon F(z^{**}) \]
   \[ = \frac{\mu H_O(z^{**}, 1) + \alpha_\ell \epsilon F(z^{***})}{\alpha_\ell (1 - F(z^*))}, \tag{30} \]
   \[ L_0 = (1 - \lambda \epsilon) L_0 + \mu \epsilon SS_0 + (X - X_L) \mu \epsilon H_O(z^{**}, 1) \]
   \[ \frac{\mu \epsilon SS_0 + (X - X_L) \mu \epsilon H_O(z^{**}, 1)}{\lambda}, \tag{31} \]
   where $H_O(z^{**}, 1)$ is derived in equation (21).
8. The supply $X_L$ of leased aircraft equates the mass of high-volatility carriers with no temporary shock and productivity above the lease rate $l$. This corresponds to:

$$X_L = \frac{\lambda \omega}{\mu + \lambda} (1 - F(l)). \tag{32}$$

Equilibrium requires that equations (22)-(32) are satisfied.

References


