Identifying expertise and using it to extract the Wisdom of the Crowds

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Abstract

The "wisdom of the crowds" refers to the ability of statistical aggregates based on multiple opinions to outperform individuals, including experts, in various prediction and estimation tasks. For example, crowds have been shown to be effective at forecasting outcomes of future events. We seek to improve the quality of such aggregates by eliminating poor performing individuals, if we can identify them. We propose a new measure of contribution to assess the judges' performance relative to the group and use positive contributors to build a weighting model for aggregating forecasts. In Study 1, a dataset of 1,233 judges forecasting 104 binary current events served to illustrate the superiority of our model over unweighted models and models weighted by measures of absolute performance. We also demonstrate the validity of our model by substituting the judges with fictitiously "random" judges. In Study 2, we used a dataset of 93 judges predicting winners of games for the 2007 NFL season and evaluated our model's rate of convergence with a benchmark of simulated experts. The model does an excellent job of identifying the experts quite quickly. We show that the model derives its power by identifying experts who have consistently outperformed the crowd.

1 Introduction

Nostradamus looked to the stars to foretell disasters, Gallup surveys the populace to model future election outcomes, and sports commentators examines athletes’ past performances to predict scores of future games (statistically and otherwise). Whether the discussion centers on the art or the science of forecasting, decades of research have focused on the quality of predictive judgments spanning various domains such as economics, finance, sports and popular culture (e.g., Armstrong, 2001; Clemen & Winkler, 1999; Gaismaier & Marewski, 2011; Simmons, Nelson, Galak, & Frederick, 2011; Surowiecki, 2004). The simplest approach is to solicit forecasts, but the literature suggests that individual judgments are riddled with biases, such as being systematically too extreme or over-confident about reported probabilities, overly anchored on an initial estimate, biased toward the most emotionally available information,
neglectful of the event’s base rate, etc. (Bettman, Luce & Payne, 1998; Dawes, 1979; Gilovich, Griffin & Kahneman, 2002; Kahneman & Tversky, 2000; Simonson, 1989). A natural remedy is to seek experts in the relevant domain and hope that they would be less likely to succumb to such biases. Unfortunately, expertise is ill defined and, not always easy to identify. Although in some domains (e.g. short term precipitations) the experts are highly accurate (e.g, Wallsten & Budescu, 1983), this is not the case in general (see, for example, Tetlock’s work in the political domain, 2005).

An alternative approach that has received lots of attention recently is to improve predictive judgment by mathematically combining multiple opinions or forecasts from groups of individuals – knowledgeable experts or plain volunteers – rather than depend on a sole expert (Hastie & Kameda, 2005; Larrick & Soll 2006; Soll & Larrick 2009) or a consensus derived from interactions between the experts in the group (Sunstein, 2006). Surowiecki (2004) has labeled this approach the “wisdom-of-crowds” (WOC). The claim is that some mathematical or statistical aggregates (e.g., measures of central tendency) of the (presumably, independent) judgments of a group of individuals will be more accurate compared to the typical or mean judge by exploiting the benefit of error cancellation. Indeed, Larrick, Mannes, and Soll (2011) define the WOC effect as the fact that the average of the judges beats the average judge. Davis-Stober, Budescu, Dana, and Broomell (2012) propose a more general definition of the effect, namely that aggregate linear combination of the crowd’s estimates should beat a randomly selected member of the crowd.

The first demonstration of WOC is attributed to Francis Galton (1907) who, ironically, hoped to show that “lay folks” are poor at making judgment even when guessing the weight of an ox at a regional fair (Surowiecki, 2004). Instead, Sir Galton found that, although no individual was able to accurately predict the precise weight, the crowd’s median estimate was surprisingly precise, just one pound from the ox’s true weight. The performance of WOC depends on where the truth is found in respect to the central tendency of judgments. Simple aggregates of the crowd can be more accurate than the predictions of the best judges when the truth lies near the average distribution of the forecasts. In instances when the truth is far from the central tendency (e.g., at the tail or even away from the distribution), WOC produces predictions that are equal or more accurate than the average judge, but not the best ones (Larrick et al. 2011).
The principles of WOC have been applied to many cases ranging from prediction markets to informed policy making (Hastie & Kameda, 2005; Sunstein, 2006; Surowiecki, 2004; Yaniv, 2004). Budescu (2006) suggests that aggregation of multiple sources of information is appealing because it (a) maximizes the amount of information available for the decision, estimation or prediction task; (b) reduces the potential impact of extreme or aberrant sources that rely on faulty, unreliable and inaccurate information (Armstrong, 2001; Ariely, Au, Bender, Budescu, Dietz, Gu, Wallsten & Zauberman, 2000; Clemen, 1989; Johnson, Budescu & Wallsten, 2001; Wallsten, Budescu & Diederich, 1997); and (c) increases the credibility and validity of the aggregation process by making it more inclusive and ecologically representative. Interestingly, the judges need not be “experts” and can be biased, as long as they have relevant information that can be combined for a prediction (Hertwig, 2012; Hogarth, 1978; Koriat 2012; Makridakis & Winkler, 1983; Wallsten & Diederich, 2001).

Critics of WOC have pointed to instances where the crowd’s wisdom has failed to deliver accurate predictions because the aggregate estimate was largely distorted by systematic group bias or by a large number of uninformed judges (Simmons et al., 2011). As an alternative to simply averaging individual judgments by assigning equal weights to all, researchers have proposed weighting models that favor better, wiser, judges in the crowd (Aspinall, 2010; Wang, Kulkarni, Poor & Osherson, 2011). Such models are a compromise between the two extreme views that favor quality (expertise) and those that rely on quantity (crowds). To benefit fully from both the quality of the experts and the quantity of the crowd, the dilemma lies in assigning appropriate weight or building a model to appropriately weigh the judgments (Budescu & Rantilla, 2000).

We address this weighting problem and propose a novel measure of “contribution to the crowd”, which assesses the individual predictive abilities based on the difference of the accuracy of the crowd’s aggregate estimate with, and without, the judge’s estimate in a series of previous forecasts in the domain of interest. This method explores the diversity of the crowd by providing an easy to implement approach of identifying the best (and worst) individuals within the crowd such that they can be over (and under) weighted. In the limit, the best subset of judges can be identified and averaged while ignoring all the others.
We validate this individual contribution measure of performance, and test whether a weighted model based on individual contributions to the crowd can be reliably better than simply averaging estimates. Even when there is sufficient knowledge in the crowd to facilitate prediction of future events, there is a strong element of chance involved in forecasting them, so assessment of WOC needs to be performed over a substantial number of events and an extended period of time. Imagine, for example, a stock market which, on average, gains in value on 60% of the trading days (or a sports league where the home teams win 60% of the games) and a forecaster who predicts its closing (results) on 10 independent days. There is a probability of 0.367 (calculated by the Binomial with p = 0.6 and n = 10) that the market will not go up (or that the home teams will not win) in a majority (6 or more) of the days. Thus, to measure properly accuracy (of an individual or an aggregate) using cross-validation and dynamic modeling one requires multiple, and preferably, longitudinal data. We consider two studies. The first consists of events made over a few months regarding current events in five different domains: business, economy, military, policy and politics. The second is based on a dataset from Massey, Simmons and Armor (2011) on NFL football score predictions over games played during a 17 week season.

2 Wisdom of the crowd
The premise behind WOC is that individual knowledge (signals) can be extracted, while biases or misinformation (noise) can be eliminated by aggregating judgments (Makridakis & Winkler 1983). For the crowd to be wiser than the individuals, the distribution of estimated forecasts of the individuals must “bracket” the actual value (Larrick & Soll, 2006). In essence, WOC requires that judges in the group be knowledgeable, incentivized to express their beliefs, that the responses be obtained independently from each other, and that there is a diversity of knowledge to prevent any systematic bias of the group (see also Larrick, Mannes & Soll, 2011).

2.1 Diversity
One of the big selling points of WOC is that the aggregated estimate embodies a diversity of opinions from the crowd. Indeed, successful implementations of WOC have gone out of their way to foster diversity of opinions by: (1) selecting judges with different backgrounds, (2) eliciting their inputs independently, and (3) forcefully injecting diverse thoughts to affect their original estimates (Herzog & Hertwig, 2009).
Jain, Bearden and Filipowicz (2012) analyzed the accuracy of aggregated judgment as a function of the diversity of personality in the crowd. The authors paired 350 participants. In each pair, the two judges either had very similar or very different personalities (as measured by the Big Five personality scores from McRae & John, 1992). Every judge was asked to forecast the fate of a particular World Cup team and to guess the number of M&Ms candy in a jar. The aggregated estimates from the diverse pairs were correct 42% of the time for the World Cup teams compared to 32% for the similar pairs and 30% for individuals. The diverse pairs were also the closest to the true number of M&Ms (23% off as compared to 26% off for the similar pairs and 48% for the individuals). Although the underlying psychological principle at work is not clear, these results highlight the benefit of selecting judges with different personalities and, presumably, diverse opinions, to improve accuracy of predictions.

Diversity is derived not only from the group’s composition, but also from the method by which information is shared in the group. If individuals are not given a chance to think independently before responding, their judgments would be biased by responses from the group (Larrick et al., 2011). In fact, the higher the correlation between the individual estimates, the more judges are necessary to achieve the same level of accuracy (e.g., Broomell & Budescu, 2009; Clemen & Winkler, 1986; Hogarth, 1978). Lorenz, Rauhutb, Schweitzer, and Helbing (2011) demonstrated that even mild social influence can undermine the effect of WOC in simple estimation tasks. In their experiment 144 judges could reconsider their estimates to factual questions after having received the mean, trend or full information of other judges’ estimates but without interacting. The subjects’ estimates were compared for convergence of estimates and improvements in accuracy over five consecutive rounds with a control (no information of others’ estimates). The results showed that social influence triggers convergence of the individual estimates and significantly reduces the diversity of the group without improving its accuracy. However Miller and Steyvers (2012) showed that group aggregation performance on more complex tasks, such as reconstructing the order of time-based and magnitude-based series of items from memory, is better for judges who shared information with another judge (after they have given their estimates) than for independent ones. Independent judgment through the initial elicitation process (no social influence triggers) allowed for diversity of judgment, and later information sharing can increased accuracy of estimates.
Taken to the extreme, WOC can be applied by treating the individual judge as a “pseudo crowd”. Herzog and Hertwig (2009) changed the judges’ perceptions of the facts underlying the event by asking the participants to assume that the first answer given was incorrect, to think of reasons that the answer may be wrong, and provide a new answer. By forcefully injecting diversity, the treatment elicited a greater variance of thought from the participants than simply asking for repeated answers, and the results also produced the best aggregate estimated. Diversity not only allows for greater variance, it serves to eliminate high degrees of correlation among judges that can move the crowd to poor predictions.

2.2 Expertise

Of course, at least some of the judges must possess information, but in some cases the level of information can be minimal. For example, Herzog and Hertwig (2011) report a study predicting outcomes of three soccer and two tennis tournaments relying on the recognition heuristic. Predictions based solely on the judges’ ability to recognize some of the players’ names (through their exposure to different media) gave the group a diverse collective knowledge that was sufficient to consistently perform above chance, and as accurately as predictions based on the official rankings of the teams and players.

In most WOC forecasting applications the aggregation method gives equal weight to judges without distinguishing any level of expertise. Indeed, most applications of WOC simply average the judgments (Larrick et al., 2011). The outcome of such an approach may be suboptimal because it neglects external information (e.g., expertise) and, as such, reduces the potential of benefiting from implicit wisdom to be found in the crowd. In a recent study, Evgeniou, Fang, Hogarth, and Karelaia, (2012) found average deviations from consensus of earnings per share increase as markets become more volatile especially for stock market analysts of lower skills (measured by both past forecasting accuracy and education). The data suggest that low performers tend to make bolder predictions – with the potential for greater reward – driving the average prediction to more extreme positions. Lee Zhang and Shi (2011) examined the bids of players on the popular game show “The Price Is Right.” The researchers

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aggregated the bids to produce a price estimate that was superior to the individual estimates. The aggregation models, especially those that took into account strategy and bidding history, outperformed all the individuals, and the aggregation models that used external information outperformed the simple mean. Thus, including the judges’ level of expertise could improve the quality of the crowd’s forecasts.

WOC is about capturing the central tendency of the group that represents knowledge beyond the grasp of any individual (Sniezek & Henry, 1989). Nevertheless, WOC is subject to prediction failures that result from systematic biases and artificially high correlation among judges.

### 3 Aggregating probabilistic forecasts

We focus on aggregation of individuals who provide probabilities of future uncertain events. Our goal is to combine the, possibly conflicting, probabilistic judgments made by different individuals into one “best” judgment. French (2011) refers to this as “the expert problem.” Typically, the judgments are probabilities or odds, but one could also combine qualitative forecasts (see Wallsten, Budescu, & Zwick, 1993). The literature proposes two main paradigms for combining individual judgments about uncertainties (Genest & Zidek, 1986): behavioral and mathematical aggregations.

In behavioral aggregation the judges seek a consensus probability through an interactive procedure, in which they revise their opinions after receiving feedback. The feedback can vary from descriptive statistics of the group’s opinions to justifications on individual probabilistic judgment. Examples of these techniques are the Delphi method, (see Rowe & Wright, 2001 for a detailed description) and decision conferences (Phillips, 2007) among others. Behavioral aggregation methods are not without criticism, the main one being that after several rounds of interactions, the judges may still disagree, and some sort of non-behavioural aggregation is needed. The second is that the benefits derived from the various methods are

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2 Broomell and Budescu (2009) developed a quantitative model of the inter-judge correlations that identifies the stand – alone contributions of several environmental and individual variables on the inter-judge agreement.
highly dependent on the composition of the groups and the structure of the within group interaction. Any change to the structure can compromise the interaction process, and thus reduce the quality of the solution. The third criticism is that identifying real experts and assembling a panel of experts can be costly without necessarily providing more accurate forecasts (French, 2011).

The second paradigm is based on mathematical aggregation of the reported individual probabilities. Two main approaches have been developed: Bayesian aggregation and opinion pools (weighting models) (see Budescu & Yu, 2006). The Bayesian approaches treat the individuals’ judgments as data and seek to develop appropriate likelihood functions that allow the aggregation of probabilities by the Bayes formula applied to a prior probability judgment (Clemen & Winkler, 1990). The key difficulty in this approach is the development of prior and likelihood probability models. It is especially difficult to specify the covariance structure among the data (experts). We focus on pooling because the approach is much simpler to implement without making assumptions about priors, correlation of errors between experts, and likelihood functions.

Opinion pools of the individuals’ probability judgments are the most frequently applied weighting schemes in practice: from predictions of volcanic eruptions to risk assessments in the nuclear power industry (Aspinall, 2010; Cooke & Goossens, 2004). Although there are more general formulas (French, 1985; Genest & Zidek, 1986), the most common aggregation rules are the weighted arithmetic (linear) and the weighted geometric pools (means):

\[
\text{and}
\]

where \( p_i \) is the individual \( i \)'s reported probability for an event of interest \( x \) and the linear opinion pool is the results from combining \( k \) individuals based on assignment of non-negative weights \( w \), such that \( \sum w = 1 \). In general, \( w_i \leq 1 \) and, as a consequence, it reduces the influence of the extremely high values. Variations of these themes involve averaging
the log-odds, \( \log \left( \frac{p}{1-p} \right) \), and back transforming the mean log odds to the probability scale (Bordley, 2011).

The weights in an opinion pool often represent the individuals’ relative expertise, but the concept of “relative expertise” is ill defined and subject to many interpretations (French, 2011). One possibility is to assign weights based on individuating features of the judges. These could be objective (e.g., historical track record, education level, seniority and professional status), subjective (e.g., ratings of expertise provided by the judges themselves or others, such as peers or supervisors) or a combination of the two. Another approach is to define the weights empirically based on the experts’ performance on a set of uncertain “test” events, the resolution of which are unknown to the experts, but known to the “aggregator” (person or software) that assigns the weights in the opinion pool for the events of interest (Bedford & Cooke, 2001; Cooke, 1991).

Clemen (2008) and Lin and Cheng (2009) have compared the performance of Cooke’s empirical linear opinion pool method with equal weighting linear pools (“plain WOC”) and with the best expert’s judgement. The weighted method generally outperformed both the equal weights method and the best expert. Note, however, that the weights vary as a function of the scoring rule used in the elicitation process and different scoring rules lead to different weights. Wang et al. (2011) proposed that scores be accompanied by a cost (such as an incoherence penalty based in part on violation of probability axioms and logic principles) to adequately weigh individuals, especially in longitudinal and conditional probabilistic studies.

A critique of the empirical weighting linear pools is that they over-weight a few individuals (i.e., true experts), which can lead to extreme predictions (Soll & Larrick, 2009). This may be advantageous when there is a high correlation between the test events and the actual events of interest. As the two sets of events diverge and the correlation between performances of the two is reduced, an equal weighted average may be is preferable because equal weighting values diversity of opinions, and downplays the “experts”. In this paper, we develop and employ a new empirically weighted linear opinion pool (with a cost parameter). Unlike Cooke’s approach, we do not use an independent stand-alone set of pre-test events to identify relative expertise. Instead, the weights emerge in the process of forecasting and they are based on the judges’ performance relative to others (i.e., contribution to the crowd). We also develop a
dynamic version of the model that adapts to changes in the contribution measure as new events are being resolved and included in the model.

4 Contribution weighted model

We define an individual’s contribution to the crowd to be a measure of the individual expertise, relative to the crowd. More specifically, it measures the change in the crowd’s aggregated performance, with and without the target individual. Once such individual contributions are calculated, a contribution weighted model (CWM) is devised to be applied in future predictions by the same crowd of judges. To quantify the effects of WOC we need an appropriate measure of quality of the aggregate (and the individuals). In the context of probability judgment this score is, typically, a proper scoring rule (e.g. Bickel, 2007). We use the Brier score (Brier, 1950), but the proposed approach and procedure can be applied to all other (proper or improper) scoring schemes. To determine the contributions of each judge:

(1) The performance of the crowd of all N judges is aggregated across all the events, based on the Brier score (Score):

\[ \text{Score} = \frac{1}{T} \sum_{t=1}^{T} \left( 2p_t - 1 \right)^2 + b \left( 1 - p_t \right), \]

where T is the number of forecasting instances (events), \( p_t \) is the mean probability of the crowd for event t (where t = 1...T) that takes a value between 0 and 1, and \( b \) is the binary indicator of the actual outcome for each event (0=occur or 1=not occur). In our case we use constants \( a = 100 \) and \( b = -50 \), which yields Scores ranging from 0 to 100, where 0 indicates the worst possible performance (assigning a probability of 1 to all events with \( b = 0 \) and a probability of 1 to all cases with \( b = 0 \)), 100 indicates perfect performance (assigning a mean probability of 1 to all events with \( b = 1 \) and a probability of 0 to all cases with \( b = 0 \), and, 75 is the expected score by “chance” (assigning a probability of 0.5 to all events).

(2) Each of the N judges is excluded (separately) from the crowd and the crowd’s Score is recalculated based on the remaining (N-1) judges, to obtain N “partial” Scores (one for each judge).
The contribution of each judge is calculated by taking the difference between the crowd’s original Score, and the “partial” Score without the target judge. Each judge’s contribution can be expressed as the following:

\[ C_F = \sum_{t=1}^{T} (S_{t,F} - S_{t}) \]

where \( T \) is the number of events, \( \bar{S} \) is the mean transformed Brier score of the crowd (all N forecasters) of each event, and \( S_{t} \) is the corresponding mean Score of that event, of (N-1) forecasters, excluding the very judge \( F \) for whom the contribution is being computed.

A judge’s contribution can be positive (indicating that his / her forecasts improve, on average, the crowd’s Score) or negative (suggesting that his / her forecasts reduce the average Score of the crowd), with an occasional 0 for judges whose presence or absence does not affect the crowd’s mean performance. Clearly, we focus on, and value, positive contributions since the higher is the contribution of a judge then the more he/she adds to the accuracy of the crowd.

This view of contribution is inspired by statistical literature on measures of influence (e.g., Kutner, Nachtsheim, Neter, & Li, 2005), that seek to establish if, and by how much, various parameters and predictions of complex statistical models are affected by specific observations, by eliminating them (one at a time) from the sample. By analogy, we measure the influence of each member of the crowd on the group’s performance in the relevant metric (in this case the Score). We hypothesize that this measure would outperform weights based on the judges past performance (“track record”). The key intuition behind this prediction is that, on average, and in most cases the predictions of the various judges will be highly correlated (see Broomell & Budescu, 2009 for a list of examples). Thus, there will be many cases where almost everyone in the crowd will have very good Scores and, conversely, cases where practically all the members of the crowd will perform poorly. Straight measures of absolute performance are not likely to be very discriminating in such cases. Our contribution measure recognizes good performance in a relative sense. Judges get high contribution scores if they do well in cases where the majority of the crowds performs poorly, i.e., when they do not follow the crowd when it is wrong.

One does not necessarily have to perform exceptionally well, to stand out. Imagine an event that is true (i.e., \( o_t=1 \)) and a crowd of (n-1) judges whose mean judged probability is \( p \), so
their Brier score is \((p-1)^2\). Now we consider a new judge, so the crowd’s size has increased to \(n\). The target judge’s prediction is closer to the truth, say \(p^* = (p+\Delta)\) where \(0 \leq \Delta \leq (1-p)\). The mean probability of the new crowd is \((p + \Delta/n)\) and their Brier score is \([(p-1) + \Delta/n]^2\). The difference between the two Brier scores is \([\Delta/n]^2 - (2\Delta(1-p)/n]\). It is easy to show that this difference is always negative (because \(\Delta \leq (1-p)\)). In other words, the Brier score with the new judge is closer to the ideal 0. The magnitude of the improvement increases as a function of \(\Delta\) and decreases as the crowd size, \(n\), grows. For example, assume \((n-1) = 9\) judges estimate the probability to be 0.2 with a Brier score of \((1 - 0.2)^2 = 0.64\). The target judge’s estimate is 0.7 \((\Delta = 0.5)\) which is closer to 1, but far from stellar. The new mean probability is 0.25 which yields a considerably better Brier score of \((1 - 0.25)^2 = 0.5625\). Under our scoring rule, this judges’ contribution would be positive.

Our weighted aggregated model, CWM, employs only judges with positive contributions in forecasting new events. These contributions are normalized to build weights, such that the aggregated prediction of the crowd is the weighted mean of the positive contributors’ probabilities.

5 Study 1: Forecasting current events

To validate the weighting procedure and verify that it can identify quality judges in the crowd, we analyzed data gathered from the ACES forecasting website (http://forecastingace.com). Launched in July 2010, the website elicits probability forecasts from volunteer judges on current events. The judges sign-up to become forecasters, and can choose to answer, at any time, any subset of events from various domains including: business, economy, entertainment, health, law, military, policy, politics, science and technology, social events, and sports. Although there are a variety of event formats, we focus here only on binary ones that refer to occurrence of specific target events. Each event describes a precise outcome that may, or may not occur, by a specific deadline (closing date) to allow an unambiguous determination of its ground truth at the deadline. On average, 15 to 20 events are posted at various times every month with various closing dates (some as short as 3 days and some as long as 6 months) as a function of the nature of the event. There are no restrictions on the number of events a judge can answer, and every week a newsletter is sent to all forecasters to announce new events being posted and encourage participation.
Figure 1 shows a screenshot of an event. Upon viewing the event, the judge first makes a prediction on whether or not the event will occur, and then enters his / her subjective probability of the event’s occurrence by moving the slider. The webpage enforces binary additivity (i.e. forces the probability of the event occurring \( P(A) \) and the probability of the event not occurring \( P(\sim A) \) to sum to 1). Judges have the option of listing rationales to justify their forecast, but less than 10% of them provide rationales. The predictions and probabilities can be revised any time before the closing date, but most judges (90%) do not revise their initial judgments. The current data analysis was conducted only on the last reported probability for every judge for any given event.

The judges are scored based on their participation (number of forecasts performed) and accuracy of prediction. The individual scores serve as an intrinsic motivator for participation and they are the only explicit incentive provided by the website. In addition to providing forecasts, judges were encouraged to complete a background questionnaire pertaining to their expertise in the various domains. The questionnaire covers their self-assessed knowledge of the domains, the hours they spend reading the news, education level, and years of experience in forecasting.

5.1 Data collection

1,233 judges provided probabilistic forecasts for 104 events between the launch of the site and January 2012. The judges answered an average number of 10 events (i.e., on average judges responded to 10% of the events posted) and the average number of respondents per event is 127. Only judges who had answered 10 or more events (n=420) were included in our analysis. Some descriptive statistics are presented in Table 1. These judges responded to a mean number
of 23 events, reported a mean general knowledge on current issues around 5 (1 is no knowledge, and 7 is extremely knowledgeable) and reported spending on average 23 minutes a day reading the news. The level of education ranges from high school (4%) to Ph.D. (10%) and most of them (64%) have at least a Bachelor’s degree. Only 37% of the judges have experience in forecasting with an average of 5 years. Since judges could choose to make forecasts at various times we derived a measure of timing\(^3\), that ranges from 0 (when an event is answered on the day it is posted, or on the day a judge joins the site) and 1 (when an event is answered on the date an event is scheduled to close, or on the date the outcome has occurred\(^4\)). The mean timing is 0.19 indicating that most events are answered close to the time they are posted. The correlations between these variables and individual contributions can be found in the Appendix.

<p>| Table 1 Descriptive statistics of contributors (N=420): |
|-----------------|-----------|--------|-------|--------|--------|--------|--------|</p>
<table>
<thead>
<tr>
<th>Number of event answered</th>
<th>Mean</th>
<th>Min</th>
<th>Q1</th>
<th>Median</th>
<th>Q3</th>
<th>Max</th>
<th>SD</th>
</tr>
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<tbody>
<tr>
<td>General knowledge (from 1 to 7)</td>
<td>5.01</td>
<td>2</td>
<td>4</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>0.83</td>
</tr>
<tr>
<td>Reading news (in hours)</td>
<td>0.39</td>
<td>0</td>
<td>0.25</td>
<td>0.33</td>
<td>0.50</td>
<td>1</td>
<td>0.26</td>
</tr>
<tr>
<td>Education (from 1 to 5)</td>
<td>3.17</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>1.07</td>
</tr>
<tr>
<td>Forecasting Experience (years)</td>
<td>5.20</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>6</td>
<td>50</td>
<td>0.91</td>
</tr>
<tr>
<td>Timing or response (relative to event duration)</td>
<td>0.19</td>
<td>0</td>
<td>0.10</td>
<td>0.17</td>
<td>0.25</td>
<td>1</td>
<td>0.14</td>
</tr>
</tbody>
</table>

5.2 Comparison of aggregation models

We hypothesized that CWM will provide more accurate forecasts by its method of overweighting positive contributors and underweighting, or even dismissing, negative contributors. The performance of CWM was compared against seven competing models listed in Table 2.

<p>| Table 2 Alternative aggregation models considered |</p>
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\(^3\) Timing is the difference between the closing date of the item and the user submit date of the reported probability, divided by the duration of the item, i.e., close date minus the open date, or the period the user started participating, i.e., close date minus the first time the user submitted a forecast, depending on whichever is the shortest period:

\(^4\) Some items are resolved at a predetermined fixed date (e.g. item about the mortgage rate in Figure 1), but others can occur at any point in time prior to a given date (e.g. The DOWJ will drop below 12,000 at anytime before the end of 2012),
<table>
<thead>
<tr>
<th>Model</th>
<th>Description</th>
<th>Justification</th>
</tr>
</thead>
<tbody>
<tr>
<td>ULinOp</td>
<td>Equally weighted Score for all 1233 judges (the crowd).</td>
<td>Test CWM against unweighted Score of entire dataset.</td>
</tr>
<tr>
<td>UWM</td>
<td>Equally weighted Score for the subset of 420 forecasters, who answered 10 or more events.</td>
<td>Test CWM against unweighted Score of the same subset.</td>
</tr>
<tr>
<td>Contribution</td>
<td>Equally weighted Score of all positive contributors from the subset of 420 forecasters, who answered 10 or more events.</td>
<td>Compare the advantage of weighting contributors.</td>
</tr>
<tr>
<td>BWM</td>
<td>Weights are calculated with Score for all of the 420 judges. The weights depend only on the judge’s past performance (Score).</td>
<td>Compare CWM with weighted model based on absolute past performance.</td>
</tr>
<tr>
<td>xBWM</td>
<td>Same as BWM, but using a percentage of positive contributors similar to CWM.</td>
<td>Compare CWM with weighted model based on absolute past performance with the same number of positive contributors.</td>
</tr>
<tr>
<td>UnifCWM</td>
<td>Instead of using the probabilities reported by the judges to compute contribution as in CWM, the probabilities are drawn from a uniform distribution (0,1).</td>
<td>Assess the robustness of CWM using uniform random distribution.</td>
</tr>
<tr>
<td>BetaCWM</td>
<td>Instead of using the probabilities reported by the judges to compute contribution as in CWM, the probabilities are drawn from beta distributions whose means and variances match the values for that event.</td>
<td>Assess the expertise of contributors using the same mean and variance for each event.</td>
</tr>
</tbody>
</table>

The first two models (UWM and ULinOp) are unweighted and serve as a baseline to all other weighted models. The difference between UWM and ULinOp shows the effect of trimming the sample to include only those who have answered 10 or more events. The Contribution model is an unweighted model using only positive contributors to assess the effect of the new “contribution to the crowd” metric. BWM and xBWM are weighted models built with the judges’ past Score, and unlike CWM the weights are independent of the performance of the other members of the crowd. BWM did not select for best performers, while xBWM, similar to CWM, selected for a mean number of 220 best judges to compute the weighted model.

In order to use as much information as possible to compute each judge’s contribution, yet avoid over-fitting, we cross-validated the models by eliminating one event at a time (jackknifing). The CWM model used all events, except for the one being eliminated to compute
the weights and the aggregated forecast of the jackknifed event was determined as a weighted average of forecasts from positive contributors\(^5\). Thus, all predictions being considered are “out of sample”. The last two models, UnifCWM and BetaCWM, are pure simulations designed to assess the robustness of CWM. The first, UnifCWM, used a uniform distribution to assign probabilities randomly to forecasts, and BetaCWM generated probabilities for each event from a beta distribution with the same mean and variance as the crowd’s estimates for that event. Each model was ran 100 times.

A summary of all model fits in the Score metric is provided in Table 3 in which the models are listed according to their mean Scores. CWM produces the highest Score (highlighted in bold) with Contribution a close second.

Table 3 Model results (In terms of their Score):

<table>
<thead>
<tr>
<th>Model</th>
<th>Judges Included</th>
<th>Mean positive contributors</th>
<th>Score of models across all events</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>Min.</td>
</tr>
<tr>
<td>CWM</td>
<td>420</td>
<td>220</td>
<td>39.93</td>
</tr>
<tr>
<td>Contribution</td>
<td>420</td>
<td>220</td>
<td>39.52</td>
</tr>
<tr>
<td>UWM</td>
<td>420</td>
<td>---</td>
<td>41.58</td>
</tr>
<tr>
<td>Union</td>
<td>1233</td>
<td>---</td>
<td>42.81</td>
</tr>
<tr>
<td>BetaCWM(^5)</td>
<td>420</td>
<td>212</td>
<td>10.07</td>
</tr>
<tr>
<td>xBWM</td>
<td>420</td>
<td>220</td>
<td>9.46</td>
</tr>
<tr>
<td>BWM</td>
<td>420</td>
<td>---</td>
<td>25.31</td>
</tr>
<tr>
<td>UnifCWM(^7)</td>
<td>420</td>
<td>215</td>
<td>46.15</td>
</tr>
</tbody>
</table>

Table 3 shows that only CWM, and its close variant, Contribution, beat the unweighted models, UWM and UlinOp, (which are almost equally good) by about 28%\(^8\). The models that

\(^5\) BWM, xBWM, unifCWM and betaCWM were cross-validated following the same jackknifing procedure.

\(^6\) The values represent an average for all simulations with a unweighted Score of 81.42 and the standard deviation among simulations was 1.05

\(^7\) The values represent an average for all simulations with a unweighted Score of 74.95 and the standard deviation among simulations was 0.94

\(^8\) This relative change (improvement or decline) is calculated based on a bounded maximum for the Score. % improvement = 100*(difference in Score/(100-Score of the model being compared to)
weighted judges by past performance performed worse than the unweighted averages from UWM with a decline of 39% for BWM and 22% for xBWM.

The results of the simulated models are also summarized in the table. The UnifCWM converged towards a mean probability of 0.5, which leads, as expected, to a Score of 75. The BetaCWM was based on the mean and variance of each event and it performed better, but not as well as the unweighted crowd, or the CWM model. The big difference is that although each event is predicted equally well, the contributions to the crowd are randomly distributed across judges.

The CWM’s superior performance stems from its ability to identify the judges with specific knowledge. The Contribution model (giving equal weights to positive contributors) produced 17% improvement over the UWM. In other words, 60% of CWM’s impact comes from identifying expertise and the rest is from over-weighting those who perform better than the crowd consistently.

Figure 2 presents boxplots of difference between the Score of three weighted models (CWM, BWM and xBWM) and the baseline model (UWM). The figure shows that there are less outliers with CWM because the contribution score is in reference to the group and less about individual performances, which have higher variances.

---

9 Percentage of impact = difference in Score between contribution and UWM/ difference in Score between CWM and UWM
5.3 Sensitivity and domain analyses of CWM

The robustness of CWM to extreme forecasts was investigated by re-computing the individual contributions using the following variation:

1. **CWM**: is the basic model described earlier (without any trimming).
2. **Max-min-trim**: CWM where the most extreme events (the max and min contributions of each judge) are removed.
3. **10%-trim**: is CWM where 10% (5% at each end) of event contributions of each judge are removed.
4. **20%-trim**: is CWM where 20% (10% at each end) of event contributions of each judge are removed.
5. **Median**: is CWM where the contribution is computed with the median for all events of any given judge.

The results of these methods are presented in Table 4, again using jackknifing as a method of cross-validation. Clearly, CWM is not sensitive to extreme values with less than 1% of impact on the difference between Score of weighted and equally weighted models.

<table>
<thead>
<tr>
<th>Trimming</th>
<th>Mean positive contributors</th>
<th>CWM</th>
<th>Difference in Score between UWM and the specific CWM</th>
<th>% difference to CWM</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>Min  Median Mean  Max  SD</td>
<td></td>
</tr>
<tr>
<td>10%-trim</td>
<td>227</td>
<td>88.56</td>
<td>-14.6 4.8 4.83 23.3 5.94</td>
<td>0.34</td>
</tr>
<tr>
<td>20%-trim</td>
<td>244</td>
<td>88.43</td>
<td>-14.3 4.8 4.70 23.5 5.76</td>
<td>0.0019</td>
</tr>
</tbody>
</table>
Contributions can be calculated separately for specific domains. We applied the CWM model to each of the 5 major domains separately again using only judges answering 10 or more events in each domain, and cross-validated by jackknifing each event. Figure 5 shows positive correlations between the domains, validating the interpretation of the Contribution as a measure of expertise. Table 5 shows that the crowd (not necessarily the same judges in each domain) performed better under the weighted than in the equally weighted model. The CWM excelled, compared to the UWM, in the domain of policy with a 46% improvement (in bold) and fared worst in economy with only an 18% improvement. The normalized average percent improvement, based on the number of events, for the five domains is 35%. This cannot be directly compared to the general model of 28% because some events were included in multiple domains (note that the total number of events across the five domains is 135, which is greater than the total number of events, 104)\(^{10}\), and the domain specific weights were calculated with a threshold of 10 events for each domain.

---

\(^{10}\) For example, an item about military budget approval would count both as a military and policy
Figure 3 Scatterplot matrix of individual contributions measures in the five domains

Table 5 Domain specific CWM compared to Unweighted Mean:

<table>
<thead>
<tr>
<th>Domain</th>
<th># of events</th>
<th>Mean # of judges</th>
<th>Mean positive contributors</th>
<th>UWM</th>
<th>CWM</th>
<th>Mean difference in Score</th>
<th>SD</th>
<th>% of improvement</th>
</tr>
</thead>
<tbody>
<tr>
<td>All</td>
<td>104</td>
<td>420</td>
<td>220</td>
<td>83.73</td>
<td>88.26</td>
<td>4.53</td>
<td>5.41</td>
<td>27.86</td>
</tr>
<tr>
<td>Policy</td>
<td>32</td>
<td>105</td>
<td>52</td>
<td>84.33</td>
<td>91.51</td>
<td>7.18</td>
<td>4.90</td>
<td>45.84</td>
</tr>
<tr>
<td>Business</td>
<td>23</td>
<td>48</td>
<td>23</td>
<td>83.52</td>
<td>90.00</td>
<td>6.48</td>
<td>10.55</td>
<td>39.32</td>
</tr>
<tr>
<td>Politics</td>
<td>45</td>
<td>139</td>
<td>77</td>
<td>86.36</td>
<td>91.67</td>
<td>5.31</td>
<td>4.89</td>
<td>38.93</td>
</tr>
<tr>
<td>Military</td>
<td>19</td>
<td>61</td>
<td>33</td>
<td>84.78</td>
<td>87.71</td>
<td>2.93</td>
<td>5.97</td>
<td>19.27</td>
</tr>
<tr>
<td>Economy</td>
<td>16</td>
<td>18</td>
<td>10</td>
<td>77.85</td>
<td>81.73</td>
<td>3.88</td>
<td>7.72</td>
<td>17.51</td>
</tr>
</tbody>
</table>

5.4 Dynamic CWM

As a test of CWM’s true predictive powers, we introduced 90 new events (posted between January 2012 and April 2012) and re-computed the weights in a dynamic fashion. We used the original set of 104 events to compute the initial weights for aggregating the probabilities of the first new event, and new weights were re-computed with every new event that was resolved for predicting the next one, and so on. The dynamic modeling of CWM for new events showed an overall improvement of 39%, despite the fact that the response rate of the new events was lower (39 compared to 127 judges per event in the initial set).
The dynamic model did better at the aggregate level, and the Score based on CWM was better than the one based on the UWM in 71 out of 90 events (79%). This split is significantly better than chance (50%) by a Wilcoxon signed rank test with \( p < 0.001 \). We also implemented the dynamic model for each domain using the same recursive procedure. Table 6 summarizes the results. The CWM improved the Score in all domains, except for economy, and the greatest improvement was for military events. The superiority of the CWM over the UWM model was significant in 3 of the 5 domains (military, politics and policy).

**Table 6 Summary of the performance of the dynamic CWM for each domain:**

<table>
<thead>
<tr>
<th>Domain</th>
<th># of events</th>
<th>Mean # of judges</th>
<th>Mean positive contributors</th>
<th>UWM</th>
<th>CWM</th>
<th>Mean difference in Score</th>
<th>% of improvement</th>
</tr>
</thead>
<tbody>
<tr>
<td>All</td>
<td>90</td>
<td>39.30</td>
<td>17.46</td>
<td>83.56</td>
<td>87.90</td>
<td>4.35</td>
<td>39.40*</td>
</tr>
<tr>
<td>Military</td>
<td>15</td>
<td>47.00</td>
<td>13.53</td>
<td>85.41</td>
<td>92.46</td>
<td>7.05</td>
<td>54.12*</td>
</tr>
<tr>
<td>Politics</td>
<td>49</td>
<td>36.80</td>
<td>14.84</td>
<td>84.26</td>
<td>91.13</td>
<td>6.87</td>
<td>53.36*</td>
</tr>
<tr>
<td>Policy</td>
<td>25</td>
<td>40.96</td>
<td>13.28</td>
<td>81.74</td>
<td>84.35</td>
<td>2.61</td>
<td>30.48*</td>
</tr>
<tr>
<td>Business</td>
<td>19</td>
<td>44.68</td>
<td>10.74</td>
<td>82.75</td>
<td>82.97</td>
<td>0.22</td>
<td>14.76</td>
</tr>
<tr>
<td>Economy</td>
<td>16</td>
<td>37.31</td>
<td>9.75</td>
<td>83.73</td>
<td>78.59</td>
<td>-5.15</td>
<td>-10.13</td>
</tr>
</tbody>
</table>

*Note: * significant \( (\alpha = 0.05) \) by a sign test

6 Study 2: NFL Predictions

We seek to replicate the results from Study 1 in a different context involving predictions for the National Football League (NFL) 2007 season. In this replication we apply CWM, as the model is intended, in a purely dynamic setting while addressing three potential shortcomings of the ACES dataset. We wanted to eliminate potential effects induced by: (1) the somewhat arbitrary fashion in which events are forecasted whenever a judge chooses (i.e., in arbitrary order) which events to predict and in what order by using a data set with a more rigid and systematic temporal structure where all forecasters follow the same sequence for predicting games, (2) the possibility of biases induced by the forecasters’ ability to select which events to predict, and (3) the complexity associated with multiple domains. The intention is to show the rate at which the metric of contribution can identify experts and CWM can produce an aggregate prediction in comparison to a benchmark.

6.1 Data collection and simulations

Massey et al. (2011) invited NFL fans to complete weekly online surveys on the following week’s NFL games. The NFL consists of 32 teams that play 16 games in the regular season over 17
weeks. The sample is composed of 386 judges (45% female and 55% male, mean age = 35 years), who completed more than 14 weeks of surveys. Each week they were asked to predict the winning team and list the point differences (i.e., difference between the final score of the two teams) for all games. They were also asked for their favorite team with a mean number of 12 participants per team (SD =3.57). They were awarded up to $3.50 per week based on the average absolute difference between their predictions and the game outcomes, and the best performer of the week was also given a $50 gift card.

Massey et al. (2011) found that the crowd was biased towards their “favorite” teams more than “underdogs” and the bias increased over the four-month-long experiment despite the obvious opportunity to learn with experience. The results illustrate a failure of that crowd’s wisdom due to the systematic bias of the group to follow one’s pull towards the favorite teams rather than learn from evidence.

We selected a subset of the Massey’s data set for our analysis. To control for favorite team bias, 3 forecasters were randomly selected among those who identified a particular team as their favorite. This yielded a sample of (31 teams x 3 judges =) 93 people (one team had only one participant who picked it as their favorite).

The prediction of football scores is notoriously difficult (Winkler, 1971) with a base rate of 64%\(^{11}\) for all games in this study compared to 18%\(^{12}\) for events in Study 1. In other words, a judge answering based solely on these base rates would predict correctly \((0.64^2 + -0.36^2)\) only 54% of the games. In contrast, in study 1 a judge answering based on the same principle would predict correctly \((0.18^2 + 0.82^2)\), i.e., 70% of the events. Another indication of this task’s difficulty is the performance of the 93 judges in our sample. Their predictions have a mean absolute error of 12.42 points (SD=9.72) with an average individual correlation of 0.21 (SD=0.08) between the predicted and the actual scores.

\(^{11}\) This is the percentage of agreement between the official estimate at vegasinsider.com and the true outcome of each game.

\(^{12}\) This is a percentage of the event occurring over the total number of events.
Given this obvious lack of “expertise” we decided to validate the CWM model by simulating “experts”, combining them with the judges and testing if the model can identify these experts and properly overweight them. For every judge (j), we generated a matched expert (e) with a smaller error in the predicted point differences (point.diff). More precisely, for each of the 244 games predicted by each judge, we calculated the absolute prediction error. In those cases where it was greater than 15 (a value we selected to be 1.5 times the standard deviation of the prediction errors) we reduced it to 15, preserving its direction. When the error was less than 15 we made no changes. Thus the experts’ predictions are never more than 15 points from the outcome of the game. The experts have a mean correlation between prediction and outcome of 0.49 (SD=0.03), making them slightly better than the judges.

For the purpose of analysis, we created three mixed groups by replacing, in each case, one of the three judges favoring each of the 31 teams in the sample with his / her expert counterpart. Thus, each group is a combination of 62 original judges and 31 simulated experts, for a total of 93 forecasters. The mean correlation between predictions and outcomes in the 3 mixed groups is 0.31 (SD=0.15).

Figure 4 presents boxplots of the individual correlations between the predictions and outcomes of the games based on the judges, the experts, and the three mixed groups.
We converted the predicted point differences to probabilities of winning (p). This allows us to use the same metric in the analysis as we did in Study 1. We converted the point spread to probabilities using the linear equation:

\[
p = a + b \cdot \text{spread}
\]

where \(a = 0.5\) and \(b = 0.03\). This equation was obtained by regressing the outcomes of more than 7,000 games (all NFL games played from 1978 to 2009) on the point spreads posted, at the time, on vegasinsider.com. The fit was very good (\(R^2 = 0.94\)).

The dynamic model for the football data was implemented at the weekly level. The first contribution measure for each forecaster (either judge or expert) was computed based on all games predictions for the first week. CWM then used this first week’s contributions to compute the aggregate predictions for games in the second week. In the third week, CWM applied the mean contribution measures from the first and second weeks to determine the aggregates of that week. The model proceeded thusly.

6.2 Identification of experts

Based on the proposed metric of contribution, knowledgeable forecasters are those who increase the performance of the crowd. We computed contributions and isolated the positive contributors for the dynamic CWM with each of the 3 mixed groups. The mean number of positive contributors for the mixed groups, across all weeks, is 37 (SD=3.96), out of which 31 (SD=0.54) are simulated experts and 6 (SD=4.57) are human judges. Figure 5 depicts the average number of positive contributors and the SEs (across the 3 replications) for each week. It clearly shows that by the third week all of the experts have been identified and they continue to be a positive influence in the continuing weeks. The total number decreases as original judges are slowly eliminated from the group of positive contributors. By the twelfth week of the season only one or two of judges maintained a positive contribution. Also note the systematic decrease in the standard errors across the weeks,
The influence of judges (mean=0.08, SD=0.02) also decreases with the passing weeks as their weights in the contribution model approached zero, while the opposite effect is observed for experts (mean=0.94, SD=0.01). Figure 6 illustrates that by the third week 90% of the weights for the model come from the experts.

In essence, the metric of contribution not only identified the consistently knowledgeable forecasters, but the variance of contribution also decreased as more information is gathered. Using only positive contributors diminished the effect of chance over time, and skill emerged from the model.

6.3 Impact of expertise and diversity on CWM
One benefit of simulating experts is the ability to create different groups whose comparison allows us to test the CWM. We ran the model using (1) only the original judges, (2) only the simulated experts, and (3) a combination of the two (with expert to judge ratio of 1:2). Figure 7 shows the resulting mean Scores of the judges, experts and average of the mixes for the season. The average mix group produced a mean Score of 82.79 (SD = 2.97) much closer to that of the experts (mean=83.63, SD=3.05) than that of the original judges (mean=77.20, SD=3.03). In fact, CWM of the mixes generated aggregate forecasts in the initial week of prediction almost as accurate as a benchmark CWM of experts. This pattern of a close match between CWMs of the average mix and experts is stable over time.

The CWM is a composite model that first computes individual contributions and then uses them to weigh predictions. It is natural to test which of these two stages drives the performance of the model. The mean improvement in prediction (relative to the unweighted mean, UWM) for (a) the simple average of positive contributors with no differential weighing (contribution) was 2.41 (SD=0.57, α < 0.05) or 11.95%, and (b) the differential weighing (CWM) was 2.98 (SD=0.74, α < 0.05) or 14.77%. Clearly, the strength of the model is derived mostly from identifying the positive contributors, with 81% of CWM’s improvement over UWM due to contributions, rather than weighing their predictions.

Although positive contributors have a significant effect on the average mix group (15% improvement from UWM to CWM), this was not observed in the homogenous groups of experts (4% improvement) and judges (2% decline). Figure 8 depicts the mean Score for UWM,
contribution and CWM for experts, judges and the average mix group. It shows that diversity in the heterogeneous group allowed significant improvement of Score by the model and that most of the impact is attributed to identifying positive contributors.

Figure 8 Comparison of models for experts, judges and mix

7 General Discussion

There are two distinct approaches in the quest for the most accurate probabilistic forecasts. One approach seeks individual expertise, and the other seeks to aggregate multiple opinions from a crowd without paying much attention to its individual members. The key ideas of WOC are that the aggregation process can reduce the effects of individual biases, and that one can use the central tendency of the crowd’s opinions to forecast the target events. We suggest a new approach that combines the two philosophies by (a) identifying the experts in the crowd and (b) averaging their opinions, while ignoring the estimates of the non-experts. In a sense this can also be seen as a compromise between the two approaches. The major technical contribution of the current paper is the new measure for identifying experts in a crowd by measuring their contribution to the crowd’s performance.

We often assume that expertise can be identified simply by relying on past performance on similar tasks. Indeed, if the at some point in the process one would be asked to choose a single expert, we cannot think of a way of selecting an expert that would beat this intuitive metric of absolute quality of performance. However, if one continues to rely on a crowd (or at
least a subset of its members), our results show that one can do considerably better by relying on the proposed measure of relative quality. We illustrated this approach in two longitudinal studies. By isolating the experts (those who make positive contributions to the crowd), the mean Brier score improved by 17% in Study 1 and 12% in Study 2 compared to the average of the crowd. The weighted model (CWM) implemented with positive contributors furthered improved performance by 28% in Study 1 and 15% in Study 2. This is not to say that every event predicted in Study 1 was improved by using only the reported probabilities of these experts, but over time, the variance decreased and the model proved overall significantly better than the simple (unweighted) mean(s) and weighted means relying on past performance. Our selection of experts is not based on the best performers (highest Scores) because their performances can be skewed by one or a few extreme predictions (Denell & Fang, 2010). We pick those who have consistently outperformed the group, and our model is updated dynamically to reduce variance due to chance results and to reflect “true” expertise that emerges in the process. This is best observed in the analysis of the NFL games where we can trace how well and how quickly the simulated experts rise to the top.

The success of our approach is quite intuitive, once one realizes that judges are usually highly correlated (see Broomell & Budescu, 2009) because they share certain assumptions and/or have access to the same information. Consequently, crowds often behave like herds as almost everyone expects certain events to happen (or not). This can backfire when the assumptions are false and/or the information is incomplete or biased. A good example is the recent case when prediction markets’ “failed” to predict the US Supreme Court’s decision regarding the Affordable Care Act (Prediction markets estimated a 75% chance that it would not be upheld by the court). Our contribution metric identifies and over weights the predictions of those judges who do not necessarily follow the crowd in such cases and helps avoid such traps.

An interesting theoretical issue is what makes the CWM work – its ability to identify the experts or their differential weighting. Results from both studies clearly suggest that it is primarily the model’s ability to identify the experts to be positively weighted (or, in other words, its ability to identify those members of the crowd who should be excluded), that are responsible for most of the model’s improvement. This is not surprising, as the relative insensitivity of the model to departures from optimal weighting is well recognized in the literature (e.g., Broomell & Budescu, 2009; Davis-Stober, Dana & Budescu, 2010; Dawes, 1979).
Sensitivity analyses confirmed the robustness of the CWM model, as its performance was largely unaffected by various degrees of trimming. Three analyses support the validity of the approach: (1) the model clearly outperformed randomly simulated responses with matching means and variances (Model betaCWM in Study 1); (2) its performance improved when it was applied separately to various domains of expertise in Study 1; and (3) the model was able to identify – almost perfectly and very rapidly – the simulated experts in Study 2. All three results indicate that the contribution measures we extract reflect real expertise.

The dynamic implementation of CWM is, probably, the most attractive feature from a practical point of view. Our results demonstrate that the CWM can easily adapt to new events and games (producing 39% improvement over UWM in Study 1 and 15% in Study 2) by including new experts or discarding old ones as their mean contribution changes. For Study 1, the dynamic model was especially useful in correlated domains like military, policy and politics (where predictions enhanced by 54%, 53% and 31% respectively) for judges possessing knowledge that was adaptable to all three. The model improves as more information is gathered by reducing the variance that is associated with chance success to distil the true experts from the crowd, as shown by the frequency (Figure 5) and weights (Figure 6) of experts and judges for positive contributors in the mix groups over time. By benchmarking CWM to a model including only experts in Study 2, we observed that the predictions of the CWM model were almost as good as those of the “ideal” model. Clearly, the model can be applied successfully in continuous and longitudinal setups, even in sparse cases (as in Study 1).

8 Conclusion

We proposed a new measure of individual contribution that is simple, reliable, easily interpreted and useful for assessing forecaster’s performance relative to the crowd. We tested our model in two contexts, and it both cases it outperformed models built solely on past, individual performance and on the simple average of the crowd. The model gets its power mostly by identifying experts who have consistently outperformed the crowd. It works well when there is longitudinal data even if in cases of sparse data, and it identifies the experts relatively quickly.

References


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We thank Dr Cade Massey and his colleagues for allowing us to re-analyze their NFL prediction results.
Appendix: Correlation analyses of contribution

We computed individual contributions to the crowd for the 420 judges. Note that in this case each judge’s contribution is based only on the subset of events he/she answered (which varies in size – as shown in Table 2 – and its composition across judges). As expected, about half of the judges (220) had positive contributions. The mean contribution is 0.004 and the standard deviation is 0.089. Figure 9 depicts a scatter matrix of 8 variables: contribution score, Score, the number of events answered, self-reported knowledge, self-reported time spent reading the news, timing for answering events, education, and years of experience. Most correlations are low. As anticipated, the strongest correlation was found between contribution and mean SCORE of judges ($r=0.75$). Some mild correlations were also present between timing and other variables such as contribution ($r=0.10$), the number of events answered ($r=0.21$), and years of experience ($r=0.11$). Most participants answered events closer to the opening dates, which can be due to the email alerts that they received when new events are introduced on the site. People with less experience answered at the opening of the event and those with more experience tended to answer later. Judges with high contribution scores also tended to answer near the closing date. Some of the self-reported measures are also correlated, such as education with SCORE ($r=0.13$) and years of experience ($r=0.10$), knowledge with years of experience ($r=0.12$). Additionally, the more educated is the participant the more events they answered ($r=0.12$).

In principle, the later a forecast is submitted relative to the timing of the event, the more accurate (high Score) it should be, based on the fact that the forecasters have access to more information with time. To investigate the effect of timing of answers on contribution, we correlated the two variables for each of the 420 judges, across all the events they answered. Figure 10 shows a histogram and boxplot of the distributions for the 420 correlations. The mean value for the distribution in Figure 10 is -0.0658, describing virtually no correlation between timing and contributions for the judges.

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13 This differs from the analysis described in Figure 9, where the correlation is based on the mean contribution and mean timing for each judge.
Figure 9 Scatterplot matrix\textsuperscript{14} of correlation for overall descriptive statistics.

\textsuperscript{14} Missing values for self-reported measures are represented on the last column of each plot.
Figure 10 Histogram combined boxplot of correlations for timing and contributions