

## Problem Set 3: Productivity

Allan Collard-Wexler (starting with a problem set written by Aviv Nevo)

Due Date: Friday April 13, 2012

The file GMdata.csv contains the data from the Griliches-Mairesse (1995) NBER working paper. There are 9 variables (which appear in this order in the ASCII file): *index* (firm ID), *sic3* (3 digit SIC), *yr* ( $\text{year} \in \{73, 78, 83, 88\}$ ), *ldsal* (log of deflated sales), *lemp* (log of employment), *ldnpt* (log of deflated capital), *ldrst* (log of deflated R&D capital), *ldrnd* (log of deflated R&D), *ldinv* (log of deflated investment). See the Griliches-Mairesse paper for more details on how the data set was collected. The equation you want to estimate is:

$$ldsal_i^t = \beta_1 lemp_i^t + \beta_2 ldnpt_i^t + \beta_3 ldrst_i^t + d^t + d^t d357 + a_i + \omega^t \quad (1)$$

where  $d^t$  are time dummy variables and *d357* is a dummy variable for computers(SIC 357).

1. Report sample statistics (number of observations, mean, median, standard deviation, etc.) for the variables for both the all sample and the balanced sun-panel (i.e., those firms that are present in all years). Also report these statistics for the firms that existed at least 2 periods. Do these statistics seem different? If so what does this suggest?
2. (a) Using only the balanced sub-panel compute (and report) the total, fixed-effects and random effects estimators, for the above equation.  
(b) Generate measured productivity  $\hat{\omega}_i^t$  as the residual from the above regression using the OLS estimator. Describe the autocorrelation with 5 and 10 year lags of productivity. What does this tell you about the nature of productivity dynamics.  
(c) What have you learned about firm heterogeneity from these results?

- (d) Using the full (unbalanced) panel compute the total and first difference estimators. Also compute an OLS estimator using only the firms that were present at least 2 periods. How do these estimates compare to the balanced panel estimates? What does this tell you?

### 3. Selection

- (a) Use a Probit model to estimate the probability that the firm exists in  $t + 1$  as a function of  $ldnpt$ ,  $ldrst$  and  $ldinv$ . Compute the implied inverse mills ratio (the ratio  $\frac{\phi(x)}{\Phi(x)}$  from the Heckman selection model) and include it in the above 1st difference regression and the OLS regression which used the firms that were present in at least 2 periods.
- (b) What does this Heckit procedure (and in particular the coefficient on the propensity score) tell you?

### 4. Bootstraps (use 200 bootstrap replications)

- (a) Compute bootstrapped standard errors for the OLS estimator of the production function in equation 1 for the entire sample.
- (b) Compute bootstrapped standard errors for the OLS estimator of the production function in equation 1 for the entire sample correcting for correlation across sectors (i.e. clustering by sic codes).
- (c) Compute bootstrapped standard errors for the OLS estimator of the production function in equation 1 for only the sample which is fully balanced, and correct for serial correlation (i.e. clustering by plant).
- (d) Compute standard errors for the Heckman selection model using the bootstrap that account for i) error in the probit regression in the first stage and ii) the correlation by sector.<sup>1</sup>

### 5. Control Functions

- (a) Do the first-stage ACF Regression with investment controls. What other state variables should be included? What is the effect of the investment proxy.

---

<sup>1</sup>You may need to investigate the stata code snippet in the lecture notes on the bootstrap.

- (b) Do the second-stage moment conditional to estimate the  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  with  $\omega_{it} = \alpha\omega_{it-1} + \mu + \xi_{it}$  as the evolution regression. (I've attached a set of MATA code to help you out with doing GMM in STATA).
- (c) Do the second-stage moment conditional to estimate the  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  with a survival control in the evolution of  $\omega$ , where the survival depends on firm capital and year.
- (d) Interpret the production function coefficients you've estimated and how they differ from the OLS results.
- (e) Estimate Standard errors for your estimates in a and b using bootstrap and clustering on the firm.

#### 6. Reallocation

- (a) Compute the Olley-Pakes Aggregate Productivity  $\Omega$ , average productivity  $\bar{\omega}$  and Covariance by year for the entire dataset.
- (b) Compute the Dynamic Decomposition (for entrants, exitors, cross, between and within) for the entire sample.
- (c) Interpret what you've found in a and b.