# A Model of Monetary Policy and Risk Premia

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## Monetary policy and risk premia

- 1. Textbook model of monetary policy (e.g. New Keynesian)
  - nominal rate affects real interest rate through sticky prices
  - silent on risk premia
- 2. Yet lower nominal rates decrease risk premia
  - higher equity valuations, compressed credit spreads ("yield chasing")
  - increased leverage by financial institutions
- 3. Today's monetary policy directly targets risk premia
  - "Greenspan put", Quantitative Easing
  - concerns about financial stability
- ⇒ We build a dynamic equilibrium asset pricing model of how monetary policy affects risk taking and risk premia

## Model overview

- 1. Central bank sets nominal rate to influence financial sector's cost of leverage and thereby economy's aggregate risk aversion
- 2. Endowment economy, 2 agent types
  - low risk aversion: pool wealth as equity of financial sector ("banks")
  - high risk aversion: "depositors"
  - banks take leverage by issuing risk-free deposits
- 3. Taking deposits exposes banks to funding shocks in which a fraction of deposits are pulled  $\rightarrow$  must reduce assets
  - liquidating risky assets rapidly is costly (fire sales)
  - $\Rightarrow$  to insure against this banks hold a buffer of liquid assets
- 4. Central bank regulates the liquidity premium via nominal rate
  - nominal rate = cost of holding reserves (most liquid asset)
  - nominal rate  $\propto$  liquidity premia on other liquid assets (govt bonds)
  - lower nominal rate  $\rightarrow$  liquidity buffer less costly to hold
    - $\rightarrow~$  taking leverage is cheaper
    - $\rightarrow~$  bank risk taking rises
    - $\rightarrow$  risk premia and cost of capital fall

# Nominal rate and the liquidity premium

- 1. Graph plots FF-Tbill spread (Tbill liquidity premium) against FF rate
  - liquidity premium co-moves strongly with nominal rate
  - see also results in Nagel (2014)
- 2. Banks hold large liquid security buffers ( $\approx$  30%) against short-term debt ( $\approx$  75% of all liabilities)
  - similarly, broker-dealers, SPVs, hedge funds, open-end mutual funds



## Related literature

- "Credit view" of monetary policy: Bernanke and Gertler (1989); Kiyotaki and Moore (1997); Bernanke, Gertler, and Gilchrist (1999); Gertler and Kiyotaki (2010); Curdia and Woodford (2009); Adrian and Shin (2010); Brunnermeier and Sannikov (2013)
- Bank lending channel: Bernanke and Blinder (1988); Kashyap and Stein (1994); Stein (1998); Stein (2012)
- 3. Government liabilities as a source of liquidity: Woodford (1990); Krishnamurthy and Vissing-Jorgensen (2012); Greenwood, Hanson, and Stein (2012)
- Empirical studies of monetary policy and asset prices: Bernanke and Blinder (1992); Bernanke and Gertler (1995); Kashyap and Stein (2000); Bernanke and Kuttner (2005); Gertler and Karadi (2013); Landier, Sraer, and Thesmar (2013); Hanson and Stein (2014); Sunderam (2013); Nagel (2014); Drechsler, Savov, and Schnabl (2015b)
- Asset pricing with heterogeneous agents: Dumas (1989); Wang (1996); Longstaff and Wang (2012)
- 6. Margins and asset prices: Gromb and Vayanos (2002); Geanakoplos (2003, 2009); Brunnermeier and Pedersen (2009); Garleanu and Pedersen (2011)

## Setup

- 1. Aggregate endowment:  $dY_t/Y_t = \mu_Y dt + \sigma_Y dB_t$
- 2. Two agent types: A is risk tolerant, B is risk averse:

$$U^A = E_0 \left[ \int_0^\infty f^A(C_t, V_t^A) dt \right]$$
 and  $U^B = E_0 \left[ \int_0^\infty f^B(C_t, V_t^B) dt \right]$ 

- f<sup>i</sup>(C<sub>t</sub>, V<sup>i</sup><sub>t</sub>) is Duffie-Epstein-Zin aggregator
   γ<sup>A</sup> < γ<sup>B</sup> creates demand for leverage (risk sharing)
- 3. State variable is A agents (banks) share of wealth:

$$\omega_t = \frac{W_t^A}{W_t^A + W_t^B}$$

#### **Financial assets**

1. Risky asset is a claim to  $Y_t$  with return process

$$dR_{t} = \mu\left(\omega_{t}\right)dt + \sigma\left(\omega_{t}\right)dB_{t}$$

- 2. Instantaneous risk-free bonds (deposits) pay  $r(\omega_t)$ , the real rate
- 3. Deposits subject to funding shocks  $\rightarrow$  fraction of deposits are pulled
  - rapidly liquidating risky assets is costly (fire sales)
- $\Rightarrow$  Banks want to fully self insure by holding liquid assets in proportion to deposits/leverage
  - $w_{S,t} = risky$  asset portfolio share
  - $w_{L,t}$  = liquid assets portfolio share

$$\begin{array}{ll} w_{L,t} & \geq & \max\left[\lambda\left(w_{S,t}-1\right),0\right] \\ w_{L,t} & = & \underbrace{w_{G,t}}_{\text{Govt./Agency bonds}} + \underbrace{m}_{>1} \times \underbrace{w_{M,t}}_{\text{Reserves}} \end{array}$$

#### Inflation and the nominal rate

1. Each \$ of reserves is worth  $\pi_t$  consumption units. We take reserves as the numeraire, so  $\pi_t$  is the inverse price level.

$$-\frac{d\pi_t}{\pi_t} = i(\omega_t)dt$$

- For simplicity, we restrict attention to nominal rate policies under which  $d\pi/\pi$  is locally deterministic
- 2. Define the nominal rate

$$n_t = r_t + i_t$$

- $n_t$  = nominal deposit rate in the model = Fed funds rate
- $n_t = n(\omega_t)$  is the central bank's policy rule, which agents know

## Liquidity premium

1. Reserves' liquidity premium equals opportunity cost of holding them

$$r_t - \frac{d\pi_t}{\pi_t} = r_t + i = n_t$$

2. Government bonds pay a real interest rate  $r_t^g$ . Their liquidity premium is

$$r_t - r_t^g = \frac{1}{m} n_t$$

- In data: 78% correlation of FF and FF-Tbill spread

3. Since government liabilities earn a liquidity premium, they generate seigniorage profits at the rate

$$\Pi_t \frac{n_t}{m}$$

where  $\Pi_t$  is the liquidity value of government liabilities

- govt refunds seigniorage in proportion to agents' wealth

### Optimization

1. HJB equation for each agent type is:

$$0 = \max_{c,w_{S},w_{L}} f(cW,V)dt + E\left[dV\left(W,\omega\right)\right]$$

subject to

$$w_{L} = \max \left[ \lambda \left( w_{S} - 1 \right), 0 \right]$$

$$\frac{dW}{W} = \left[ r - c + w_{S} \left( \mu - r \right) - w_{L} \frac{n}{m} + \prod \frac{n}{m} \right] dt + w_{S} \sigma dB$$

- n/m is the liquidity premium of government bonds
- $\prod \frac{n}{m}$  is seignorage payments

### Optimality conditions

 $1. \ \mbox{Each}$  agent's value function has the form

$$V(W,\omega) = \left(\frac{W^{1-\gamma}}{1-\gamma}\right) J(\omega)^{\frac{1-\gamma}{1-\psi}}$$

- 2. The FOC for consumption gives  $c^* = J$
- 3. If  $\frac{\lambda}{m}n < (\gamma^B \gamma^A)\sigma_Y^2$ , the portfolio FOCs give  $w_S^A > 1$  with

$$w_{S}^{A} = \frac{1}{\gamma^{A}} \left[ \frac{\mu - \left( r + \frac{\lambda}{m} n \right)}{\sigma^{2}} + \left( \frac{1 - \gamma^{A}}{1 - \psi^{A}} \right) \frac{J_{\omega}^{A}}{J^{A}} \omega \left( 1 - \omega \right) \frac{\sigma_{\omega}}{\sigma} \right]$$

- $\Rightarrow$  raising *n* raises the cost of taking leverage
- $\Rightarrow$  reduces risk taking  $w_S^A$
- $\Rightarrow$  increases risk premia (effective aggregate risk aversion)

How does the central bank change the nominal rate?

- 1. The supply of liquidity must evolve consistent with the liquidity demand that obtains under the chosen policy  $n_t = n(\omega_t)$ .
  - given in Proposition 3 in the paper
- ⇒ Implementing rate increase (liquidity demanded  $\downarrow$ ) requires a contraction in reserves or liquid bonds
- 2. In practice, retail bank deposits are a major source of household liquidity (\$8 trillion)
  - DSS (2015b) show that when  $n_t$  increases, banks reduce the supply of retail deposits and raise their price/liquidity premium
  - DSS (2015b) show this is due to banks' market power over retail deposits

# Retail deposit supply and the nominal rate (DSS 2015b)

- When the nominal rate rises, banks increase the interest spread charged on retail deposits and decrease deposit supply



 $\Rightarrow$  When the nominal rate increases, private liquidity supply contracts

### Results

- 1. Solve HJB equations simultaneously for  $J^{A}(\omega)$  and  $J^{B}(\omega)$
- 2. Global solution by Chebyshev collocation

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Risk aversion A	$\gamma^{A}$	1.5
Risk aversion B	$\gamma^{B}$	15
EIS	$\psi^{A},\psi^{B}$	3
Endowment growth	$\mu_{Y}$	0.02
Endowment volatility	$\sigma_Y$	0.02
Time preference	ho	0.01
Funding shock size	$\lambda/(1+\lambda)$	0.29
Govt. bond liquidity	1/m	0.25
Nominal rate 1	<i>n</i> 1	0%
Nominal rate 2	<i>n</i> <sub>2</sub>	5%

# Risk taking



- 1. As the nominal rate increases, bank leverage falls and depositor risk taking increases
  - increases effective risk aversion of marginal investor

The price of risk and the risk premium



- 1. As nominal rate falls, the price of risk falls
- 2. Risk premium shrinks ("reaching for yield")
  - effect scales up for riskier assets

#### Real interest rate



Risk-free rate r

- 1. Real rate is lower under the higher nominal rate policy
- 2. Reduction in risk sharing increases precautionary savings
  - increase in effective risk aversion lowers the real rate (as in homogenous economy)

Drechsler, Savov, and Schnabl (2015)

## Valuations/cost of capital

Price-dividend ratio P/Y



- 1. Lower rates increase valuations for all  $\boldsymbol{\omega}$ 
  - effect is largest for moderate  $\omega$ , where aggregate risk sharing/leverage is at its peak

# Volatility

 $\sigma$ 



- 1. There is greater excess volatility at lower nominal rates
  - $\omega$  more volatile since leverage is higher
  - and risk premium more sensitive to  $\boldsymbol{\omega}$

# Wealth distribution



Stationary density of  $\boldsymbol{\omega}$ 

- 1. For stationarity: introduce births/deaths
  - agents die at rate  $\kappa$  and are born as (A, B) with fraction  $(\overline{\omega}, 1-\overline{\omega})$
  - wealth is distributed evenly to newly born
- 2. Lower nominal rate  $\rightarrow$  greater mean, variance, and left tail of  $\omega$  distribution, due to greater bank risk taking

### Applications: the zero lower bound

- 1. When n = 0, there is no cost to taking leverage so banks are at their unconstrained optimum
- 2. Because banks cannot be forced to take leverage, the nominal rate cannot go negative by no-arbitrage
- 3. Central bank can raise asset prices further by lowering *expected future* nominal rates (forward guidance)

# Forward guidance



1. Forward guidance delays nominal rate hike from  $\omega = 0.25$  to  $\omega = 0.3$ 

- 2. Prices are higher under forward guidance even for  $\omega \ll 0.25$
- 3. Prices most sensitive to policy timing near liftoff ("taper tantrum")

# "Greenspan put"



1. Rates lowered in response to large negative shocks ( $\omega \leq 0.3$ )

- 2. Near  $\omega = 0.3$  valuations are flat in  $\omega$  as central bank cuts rates in response to negative shocks (as though investors own a put)
- 3. But heightened leverage  $\rightarrow$  further shocks cause prices to fall quickly
- 4. Volatility low for  $\omega$  close to 0.3 but rises sharply for lower  $\omega$

### Nominal rate shocks and economic activity

1. Introduce unexpected/independent shocks to nominal rate  $n_t$ 

$$dn_{t} = -\kappa_{n} \left[ n_{t} - n_{0} \left( \omega_{t} \right) \right] dt + \sigma_{n} \sqrt{\left( n_{t} - \underline{n} \right) \left( \overline{n} - n_{t} \right)} dB_{t}^{n}$$

- push  $n_t$  away from the known benchmark rule  $n_0\left(\omega_t
  ight)$
- $n_t$  now a second state variable (in addition to  $\omega_t$ )
- 2. To study effects on output, add production: capital  $k_t$ , investment  $\iota_t$

$$\frac{dk_{t}}{k_{t}} = \left[\phi\left(\iota_{t}\right) - \delta\right] dt + \sigma_{k} dB_{t}^{k}$$

- investment subject to convex adj. cost:  $\phi^{\prime\prime} < 0$
- output from capital  $Y_t = ak_t$
- price of one unit of capital:  $q_t = q\left(\omega_t, n_t
  ight)$
- optimal investment (q-theory):  $q_t \phi'(\iota_t) = 1$
- 3. Make real rate invariant to nominal shocks by incorporating a transitory component in total output (an output gap, e.g., labor)
  - otherwise output is rigid in the short run
  - $\Rightarrow$  nominal shocks affect capital price *q* only through risk premium
- 4. Parameters consistent with data/literature

### Impulse responses: financial markets



- Persistent drop in bank risk taking/leverage
- $\Rightarrow$  Long-lived drop in bank net worth; "financial accelerator"
- $\Rightarrow$  Persistent rise in Sharpe ratio

Drechsler, Savov, and Schnabl (2015)

### Impulse responses: economic activity



- Increase in risk premia  $\Rightarrow$  drop in the price of capital

- $\Rightarrow$  Investment falls (initially even below depreciation rate)
- $\Rightarrow$  Output growth stalls, level is permanently lower in the long run

Drechsler, Savov, and Schnabl (2015)

# The nominal yield curve



- 1. Curve slopes up even in steady state (when  $E[n_T]$  is flat)
  - $\Rightarrow$  model generates substantial term premium
    - because high nominal rates  $\rightarrow$  low risk sharing/high marginal utility
- 2. Forward term premia increase substantially with positive rate shocks
  - pprox 10 bps at long end
  - consistent with finding of Hanson and Stein (2014)

### Takeaways

- 1. Monetary policy affects/targets risk premia, not just interest rates
- 2. An asset pricing framework for studying the effect of monetary policy on risk premia
- 3. Monetary policy  $\Rightarrow$  liquidity premium  $\Rightarrow$  risk taking/leverage  $\Rightarrow$  risk premia
- 4. Dynamic applications: forward guidance, "Greenspan put," economic activity, the yield curve