Value: More than a Number

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Croatia and Slovenia, May 2010



A motive for valuation and corporate finance...

" One hundred thousand lemmings cannot be wrong"

Graffiti

Let's start with an accounting balance sheet...



And replace it with a financial balance sheet...

Assets	Liabilities
Existing Investments Generate cashflows today Includes long lived (fixed) and short-lived(working capital) assets	Place Debt Fixed Claim on cash flows Little or No role in managem <i>Fixed Maturity</i> <i>Tax Deductible</i>
Expected Value that will be created by future investments Growth As	Equity Residual Claim on cash flow Significant Role in managem Perpetual Lives

Corporate Finance: First Principles



Connecting to Valuation...



Misconceptions about Valuation

Myth 1: A valuation is an objective search for "true" value

- Truth 1.1: All valuations are biased. The only questions are how much and in which direction.
- Truth 1.2: The direction and magnitude of the bias in your valuation is directly proportional to who pays you and how much you are paid.
- Myth 2.: A good valuation provides a precise estimate of value
 - Truth 2.1: There are no precise valuations
 - Truth 2.2: The payoff to valuation is greatest when valuation is least precise.
- Myth 3: . The more quantitative a model, the better the valuation
 - Truth 3.1: One's understanding of a valuation model is inversely proportional to the number of inputs required for the model.
 - Truth 3.2: Simpler valuation models do much better than complex ones.

Valuation: The Big Picture

If you get the big picture, the details will follow...

Discounted Cash Flow Valuation

- What is it: In discounted cash flow valuation, the value of an asset is the present value of the expected cash flows on the asset.
- **Philosophical Basis**: Every asset has an intrinsic value that can be estimated, based upon its characteristics in terms of cash flows, growth and risk.
- Information Needed: To use discounted cash flow valuation, you need
 - to estimate the <u>life of the asset</u>
 - to estimate the <u>cash flows</u> during the life of the asset
 - to estimate the <u>discount rate</u> to apply to these cash flows to get present value
- Market Inefficiency: Markets are assumed to make <u>mistakes</u> in pricing assets <u>across time</u>, and are assumed to correct themselves over time, as new information comes out about assets.

DCF Choices: Equity Valuation versus Firm Valuation









Valuation: The Details

I. Estimating Discount Rates

Cost of Equity



A. The Riskfree Rate

On a riskfree asset, the actual return is equal to the expected return. Therefore, there is no variance around the expected return.

For an investment to be riskfree, then, it has to have

- <u>No default risk</u>
- <u>No reinvestment risk</u>
- 1. <u>Time horizon matters</u>: Thus, the riskfree rates in valuation will depend upon when the cash flow is expected to occur and will vary across time.
- 2. <u>Not all government securities are riskfree</u>: Some governments face default risk and the rates on bonds issued by them will not be riskfree.

For a rate to be riskfree in valuation, it has to be long term, default free and currency matched (to the cash flows)

Estimating the Riskfree Rate in Croatian HKR... and US dollars..

- Assume that you decide to value Adris Grupa in Croatian HKR. The Croatian government had 10-year HKR bonds outstanding, with a yield to maturity of 6.25% on April 1, 2010. In January 2010, the Croatian government's <u>local</u> <u>currency</u> sovereign rating of Baa3. The default spread (over a default free rate) for Baa3 rated country bonds in early 2010 was 2%.
- The riskfree rate in Croatian HKR is
- a) The yield to maturity on the 10-year bond (6.25%)
- b) The yield to maturity on the 10-year bond + Default spread (6.25%+2%)=8.25\%)
- c) The yield to maturity on the 10-year bond Default spread (6.25%-2% = 4.25%)
- d) None of the above
- If you wanted to do you entire valuation in US dollars, what would you use as your riskfree rate?
- How would your answer change if you were doing the analysis in Euros?

A Euro Riskfree Rate



Why do riskfree rates vary?



b. Equity Risk Premiums

The historical premium is the premium that stocks have historically earned over riskless securities.

Practitioners never seem to agree on the premium; it is sensitive to

- How far back you go in history...
- Whether you use T.bill rates or T.Bond rates
- Whether you use geometric or arithmetic averages.
- For instance, looking at the US:

	Arithmetic Average		Geometric Average	
	Stocks –	Stocks –	Stocks –	Stocks –
	T. Bills	T. Bonds	T. Bills	T. Bonds
1928-2009	7.53%	6.03%	5.56%	4.29%
	(2.28%)	(2.40%)		
1960-2009	5.48%	3.78%	4.09%	2.74%
	(2.42%)	(2.71%)		
2000-2009	-1.59%	-5.47%	-3.68%	-7.22%
	(6.73%)	(9.22%)		

The perils of trusting the past.....

<u>Noisy estimates</u>: Even with long time periods of history, the risk premium that you derive will have substantial standard error. For instance, if you go back to 1928 (about 80 years of history) and you assume a standard deviation of 20% in annual stock returns, you arrive at a standard error of greater than 2%:

Standard Error in Premium = $20\%/\sqrt{80} = 2.26\%$

Survivorship Bias: Using historical data from the U.S. equity markets over the twentieth century does create a sampling bias. After all, the US economy and equity markets were among the most successful of the global economies that you could have invested in early in the century.

These problems get exacerbated in markets like Croatia and Slovenia, where there is far less historical data and survivor bias is worse.



Implied Premiums in the US



The Anatomy of a Crisis: Implied ERP from September 12, 2008 to January 1, 2009



Implied Premium for Croatia & Slovenia: April 2010

	Slovenia	Croatia
Index used	LJSE Composite	Zagreb Crobex
Level	3892	2124
FCFE Yiled	3.45%	4.28%
Expected growth rate	12%	15%
Riskfree rate	3%	4.25%
IRR (Expected return)	8.22%	11.18%
ERP	5.22%	6.93%

A solution: Estimate a mature market premium with an added country risk premium

Assume that the equity risk premium for the US and other mature equity markets is 4.5%. You could then add on an additional premium for investing in an emerging markets.

Two ways of estimating the country risk premium:

- *Default spread on Country Bond*: In this approach, the country equity risk premium is set equal to the default spread of the bond issued by the country.
 - Equity Risk Premium for Croatia = 4.5% + 2% = 6.5%
 - Equity Risk Premium for Slovenia = 4.5% + 0.6% = 5.1%
- *Adjusted for equity risk*: The country equity risk premium is based upon the volatility of the market in question relative to U.S market.
- Melded approach: In this approach, we multiply the default spread by the relative volatility of equity markets to the government bond.
 - Country risk premium for Croatia = 2% (21%/14%) = 3%
 - Total risk premium for Croatia = 4.5% + 3% = 7.5%



From Country Risk Premiums to Corporate Risk premiums

Approach 1: Assume that every company in the country is equally exposed to country risk. In this case,

E(Return) = Riskfree Rate + Country ERP + Beta (US premium)

Approach 2: Assume that a company's exposure to country risk is similar to its exposure to other market risk.

E(Return) = Riskfree Rate + Beta (US premium + Country ERP)

Approach 3: Treat country risk as a separate risk factor and allow firms to have different exposures to country risk (perhaps based upon the proportion of their revenues come from non-domestic sales)

E(Return)=Riskfree Rate+ β (US premium) + λ (Country ERP)

Country ERP: Additional country equity risk premium

Estimating Company Exposure to Country Risk

- Different companies should be exposed to different degrees to country risk. For instance, a Korean firm that generates the bulk of its revenues in Western Europe and the US should be less exposed to country risk than one that generates all its business within Korea.
- The factor " λ " measures the relative exposure of a firm to country risk. One simplistic solution would be to do the following:

 $\lambda = \%$ of revenues domestically_{firm}/ % of revenues domestically_{avg firm}

Consider two firms – HyundaI Heavy Industries and Megastudy, both Korean companies. The former gets about 20% of its revenues in Korea and the latter gets 100%. The average Korean firm gets about 80% of its revenues in Korea:

 $\lambda_{Hyundai} = 20\%/80\% = 0.25$

 $\lambda_{Megastudy} = 100\%/80\% = 1.25$

- There are two implications
 - A company's risk exposure is determined by where it does business and not by where it is located
 - Firms might be able to actively manage their country risk exposures

Estimating lambda

	KRKA	Adris Grupa
% of revenues locally	10.67%	54%
% of revenues for average company	71.00%	80%
Lambda - local market	0.15	0.68
% of revenues developed markets	58.50%	10%
Lambda - developed markets	NA	NA
% of revenues other emerging markets	30.80%	29%
% of revenues for average company	77.00%	69%
Lambda- other emerging markets	0.4	0.42

Estimating Beta

The standard procedure for estimating betas is to regress stock returns (R_j) against market returns (R_m) -

$$\mathbf{R}_{\mathbf{j}} = \mathbf{a} + \mathbf{b} \ \mathbf{R}_{\mathbf{m}}$$

• where a is the intercept and b is the slope of the regression.

The slope of the regression corresponds to the beta of the stock, and measures the riskiness of the stock.

- This beta has three problems:
 - It has high standard error
 - It reflects the firm's business mix over the period of the regression, not the current mix
 - It reflects the firm's average financial leverage over the period rather than the current leverage.

A standard regression.. A beta for KRKA



And Adris Grupa



Determinants of Betas



Bottom-up Betas


Bottom Up Beta Estimates

	KRKA	Adris Grupa
Business	European pharma firms	Tourism & Tobacco
Unlevered Beta	0.62	0.68
D/E Ratio	7.18%	2.70%
Levered Beta	0.65	0.70

			Unevered
	Revenues	Estimated Weight	Beta
Tobacco	2297	82.21%	0.56
Tourism	497	17.79%	1.15
Adris Group	2794		0.68

From Cost of Equity to Cost of Capital



What is debt?

General Rule: Debt generally has the following characteristics:

- Commitment to make fixed payments in the future
- The fixed payments are tax deductible
- Failure to make the payments can lead to either default or loss of control of the firm to the party to whom payments are due.
- As a consequence, debt should include
 - Any interest-bearing liability, whether short term or long term.
 - Any lease obligation, whether operating or capital.

Debt and Equity

	KRKA	Adris Grupa
Book value of equity	€ 920.00	HRK 6,598.00
Book value of debt	€ 156.00	HRK 150.50
Market value of equity	€ 2,306.23	HRK 5,207.00
Market value of debt	€ 165.57	HRK 140.60
Debt ratio - Book value	14.50%	2.23%
Debt ratio - Market value	6.70%	2.63%

Estimating the Cost of Debt

- If the firm has bonds outstanding, and the bonds are traded, the <u>yield to</u> <u>maturity</u> on a long-term, straight (no special features) bond can be used as the interest rate.
- If the firm is rated, use <u>the rating and a typical default spread</u> on bonds with that rating to estimate the cost of debt.
- If the firm is not rated,
 - and it has recently borrowed long term from a bank, <u>use the interest rate on the</u> <u>borrowing</u> or
 - estimate a synthetic rating for the company, and use the <u>synthetic rating</u> to arrive at a default spread and a cost of debt
- The cost of debt has to be estimated in the same currency as the cost of equity and the cash flows in the valuation.

Estimating Synthetic Ratings

The rating for a firm can be estimated using the financial characteristics of the firm. In its simplest form, the rating can be estimated from the interest coverage ratio

Interest Coverage Ratio = EBIT / Interest Expenses

- The interest coverage ratio can be linked to a debt rating, which in turn can provide an estimate of default spread and the cost of debt for a company. Cost of debt = Riskfree Rate + Default spread for the company
- In emerging markets, where governments themselves have default risk, the cost of debt for a company will include some or all of the default spread for the country.

Cost of debt = Riskfree Rate + Default spread for the country + Default spread for the company

Interest Coverage Ratios, Ratings and Default Spreads

If interest coverage ratio is			
greater than	≤ to	Rating is	Spread is
-100000	0.499999	D	15.00%
0.5	0.799999	С	12.00%
0.8	1.249999	CC	10.00%
1.25	1.499999	CCC	8.50%
1.5	1.999999	B-	5.50%
2	2.499999	В	5.25%
2.5	2.999999	B+	4.25%
3	3.499999	BB	4.00%
3.5	3.9999999	BB+	3.50%
4	4.499999	BBB	2.00%
4.5	5.999999	A-	1.50%
6	7.499999	A	1.25%
7.5	9.499999	A+	1.00%
9.5	12.499999	AA	0.75%
12.5	100000	AAA	0.50%

Estimating the cost of debt

	KRKA	Adris Grupa
EBIT	€ 235.00	HRK 527.90
Interest expenses	€ 10.50	HRK 9.70
Interest coverage ratio	22.38	54.42
Rating	AAA	AAA
Company Default Spread	0.50%	0.50%
Country Default Spread	1.20%	2.00%
Riskfree Rate	3%	4.25%
Cost of debt - pre-tax	4.10%	6.75%
Marginal tax rate	21.00%	20.00%
Cost of debt - after-tax	3.24%	5.40%

Estimating Cost of Capital

	KRKA	Adris Grupa
Beta	0.65	0.70
Lambda	0.15	0.68
Lambda - other markets	0.40	0.42
Cost of equity	7.26%	10.70%
Synthetic rating	AAA	AAA
Cost of debt	4.10%	6.75%
Cost of debt - after-tax	3.24%	5.40%
Debt Ratio	6.70%	2.79%
Cost of capital	6.99%	10.55%



Defining Cashflow



From Reported to Actual Earnings



Aswath Damodaran

Dealing with Operating Lease Expenses

- Operating Lease Expenses are treated as operating expenses in computing operating income. In reality, operating lease expenses should be treated as financing expenses, with the following adjustments to earnings and capital:
- Debt Value of Operating Leases = Present value of Operating Lease <u>Commitments</u> at the pre-tax cost of debt
 - When you convert operating leases into debt, you also create an asset to counter it of exactly the same value.
- Adjusted Operating Earnings Adjusted Operating Earnings = Operating Earnings + Operating Lease Expenses -Depreciation on Leased Asset
 - As an approximation, this works:
 - Adjusted Operating Earnings = Operating Earnings + Pre-tax cost of Debt * PV of Operating Leases.

R&D Expenses: Operating or Capital Expenses

- Accounting standards require us to consider R&D as an operating expense even though it is designed to generate future growth. It is more logical to treat it as capital expenditures.
- To capitalize R&D,
 - Specify an amortizable life for R&D (2 10 years)
 - Collect past R&D expenses for as long as the amortizable life
 - Sum up the unamortized R&D over the period. (Thus, if the amortizable life is 5 years, the research asset can be obtained by adding up 1/5th of the R&D expense from five years ago, 2/5th of the R&D expense from four years ago...:

What tax rate?

- The tax rate that you should use in computing the after-tax operating income should be
- The effective tax rate in the financial statements (taxes paid/Taxable income)
- □ The tax rate based upon taxes paid and EBIT (taxes paid/EBIT)
- **D** The marginal tax rate for the country in which the company operates
- □ The weighted average marginal tax rate across the countries in which the company operates
- $\Box \quad \text{None of the above}$
- Any of the above, as long as you compute your after-tax cost of debt using the same tax rate

Capital expenditures should include

- <u>Research and development expenses</u>, once they have been re-categorized as capital expenses. The adjusted net cap ex will be
 - Adjusted Net Capital Expenditures = Net Capital Expenditures + Current year's R&D expenses - Amortization of Research Asset
 - <u>Acquisitions of other firms</u>, since these are like capital expenditures. The adjusted net cap ex will be
 - Adjusted Net Cap Ex = Net Capital Expenditures + Acquisitions of other firms -Amortization of such acquisitions

Two caveats:

- 1. Most firms do not do acquisitions every year. Hence, a <u>normalized measure of</u> <u>acquisitions</u> (looking at an average over time) should be used
- 2. The best place to find acquisitions is in the statement of cash flows, usually categorized under <u>other investment activities</u>

Working Capital Investments

- In accounting terms, the working capital is the difference between current assets (inventory, cash and accounts receivable) and current liabilities (accounts payables, short term debt and debt due within the next year)
- A cleaner definition of working capital from a cash flow perspective is the difference between <u>non-cash current assets</u> (inventory and accounts receivable) and <u>non-debt current liabilities</u> (accounts payable)
- Any investment in this measure of working capital ties up cash. Therefore, any increases (decreases) in working capital will reduce (increase) cash flows in that period.
- When forecasting future growth, it is important to forecast the effects of such growth on working capital needs, and building these effects into the cash flows.

Estimating FCFF

	KRKA	Adris Grupa
EBIT	€ 235.00	HRK 527.90
Effective tax rate	€ 0.24	HRK 0.17
EBIT (1-t)	€ 179.33	HRK 436.29
Net Cap Ex	€ 15.00	HRK 3.12
Chg in WC	€ 68.00	-HRK 118.07
Reinvestment	€ 83.00	-HRK 114.95
FCFF	€ 96.33	HRK 551.24
Reinvestment Rate - last year	46.28%	-26.35%

Growth in Earnings

Look at the past

- The historical growth in earnings per share is usually a good starting point for growth estimation
- Look at what others are estimating
 - Analysts estimate growth in earnings per share for many firms. It is useful to know what their estimates are.

Look at fundamentals

• Ultimately, all growth in earnings can be traced to two fundamentals - how much the firm is investing in new projects, and what returns these projects are making for the firm.

The Determinants of Growth



Measuring Return on Capital (Equity)



Measuring Return on Capital

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	KRKA	Adris Grupa
EBIT (1-t)	€ 179.33	HRK 436.29
BV of Debt	€ 184.00	HRK 101.00
BV of Equity	€ 783.00	HRK 5,941.00
Cash	€ 8.30	HRK 1,038.00
Invested Capital	€ 958.70	HRK 5,004.00
ROC	18.71%	8.72%
ROC - last 5 years	20.70%	9.69%

Measuring Reinvestment Rate and Expected Growth

	KRKA	Adris Grupa
Reinvestment Rate last year	46.28%	-26.35%
Reinvestment Rate last 5 years	82.70%	70.83%
Reinvestment rate last 5 years - no acquisitions	57.13%	70.83%

	KRKA	Adris Grupa
ROC	20.70%	9.69%
Reinvestment Rate	57.13%	70.83%
Expected Growth rate	11.83%	6.86%



Getting Closure in Valuation

A publicly traded firm potentially has an infinite life. The value is therefore the present value of cash flows forever.

Value =
$$\sum_{t=1}^{t=\infty} \frac{CF_t}{(1+r)^t}$$

Since we cannot estimate cash flows forever, we estimate cash flows for a "growth period" and then estimate a terminal value, to capture the value at the end of the period:

Value =
$$\sum_{t=1}^{t=N} \frac{CF_t}{(1+r)^t} + \frac{\text{Terminal Value}}{(1+r)^N}$$

Ways of Estimating Terminal Value



Stable Growth and Terminal Value

- When a firm's cash flows grow at a "constant" rate forever, the present value of those cash flows can be written as:
 - Value = Expected Cash Flow Next Period / (r g)

where,

- r = Discount rate (Cost of Equity or Cost of Capital)
- g = Expected growth rate
- While companies can maintain high growth rates for extended periods, they will all approach "stable growth" at some point in time. When they will do so will depend upon:
 - How large they are relative to the market in which they operate
 - Their competitive advantages

Four Rules for Terminal value

- <u>Respect the cap</u>: The stable growth rate <u>cannot exceed the growth rate of the</u> <u>economy</u> but it can be set lower. One simple proxy for the nominal growth rate of the economy is the riskfree rate.
 - Riskfree rate = Expected inflation + Expected Real Interest Rate
 - Nominal growth rate in economy = Expected Inflation + Expected Real Growth
- Stable period excess returns: Firms that generate returns on capital that vastly exceed their costs of capital should see these excess returns shrink in stable growth as competition enters and size works against them.
- Reinvest to grow: Growth is never free and this is especially true in stable growth. To grow at a perpetual rate, firms have to reinvest and how much they reinvest will be a function of the return on capital:

Reinvestment Rate = Stable growth rate/ Stable ROC

- <u>Adjust risk and cost of capital</u>: The cost of equity and capital in stable growth should be reflective of a mature firm in stable growth. In particular,
 - Betas should move towards one
 - Debt ratios should converge on long-term sustainable averages

1. How high can the stable growth rate be?

- The stable growth rate <u>cannot exceed the growth rate of the economy</u> but it can be set lower.
 - If you assume that the economy is composed of high growth and stable growth firms, the growth rate of the latter will probably be lower than the growth rate of the economy.
 - The stable growth rate can be negative. The terminal value will be lower and you are assuming that your firm will disappear over time.
 - If you use nominal cashflows and discount rates, the growth rate should be nominal <u>in the currency</u> in which the valuation is denominated.
- One simple proxy for the nominal growth rate of the economy is the riskfree rate.
 - Riskfree rate = Expected inflation + Expected Real Interest Rate
 - Nominal growth rate in economy = Expected Inflation + Expected Real Growth

2. When will the firm reach stable growth?

Size of the firm

• Success usually makes a firm larger. As firms <u>become larger</u>, it becomes much more difficult for them to maintain high growth rates

Current growth rate

- While past growth is not always a reliable indicator of future growth, there is a <u>correlation between current growth and future growth</u>. Thus, a firm growing at 30% currently probably has higher growth and a longer expected growth period than one growing 10% a year now.
- Barriers to entry and differential advantages
 - Ultimately, high growth comes from high project returns, which, in turn, comes from <u>barriers to entry</u> and <u>differential advantages</u>.
 - The question of how long growth will last and how high it will be can therefore be framed as a question about <u>what the barriers to entry are, how long they will stay up and how strong they will remain.</u>

3. What else should change in stable growth?

In stable growth, firms should have the characteristics of other stable growth firms. In particular,

- The risk of the firm, as measured by beta and ratings, should reflect that of a stable growth firm.
 - Beta should move towards one
 - The cost of debt should reflect the safety of stable firms (BBB or higher)
- The debt ratio of the firm might increase to reflect the larger and more stable earnings of these firms.
 - The debt ratio of the firm might moved to the optimal or an industry average
 - If the managers of the firm are deeply averse to debt, this may never happen
- The return on capital generated on investments should move to sustainable levels, relative to both the sector and the company's own cost of capital.

4. What excess returns will you generate in stable growth and why does it matter?

- Strange though this may seem, the terminal value is not as much a function of stable growth as it is a function of what you assume about excess returns in stable growth.
- The key connecting link is the reinvestment rate that you have in stable growth, which is a function of your return on capital:

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Reinvestment Rate = Stable growth rate/ Stable ROC
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The terminal value can be written in terms of ROC as follows:

Terminal Value = EBIT_{n+1} (1-t) (1 – g/ ROC)/ (Cost of capital – g)

- In the scenario where you assume that a firm earns a return on capital equal to its cost of capital in stable growth, the terminal value will not change as the growth rate changes.
- If you assume that your firm will earn positive (negative) excess returns in perpetuity, the terminal value will increase (decrease) as the stable growth rate increases.

Stable Growth Assumptions

		KRKA	Adris Grupa
Beta	High Growth	0.65	0.70
	Stable Growth	0.80	0.80
Lambda	High Growth	0.15	1.10
	Stable Growth	0.15	1.10
CRP	High Growth	0.90%	3.00%
	Stable Growth	0.60%	2.00%
Cost of equity	High Growth	7.26%	10.70%
	Stable Growth	7.89%	10.05%
Cost of capital	High Growth	6.99%	10.55%
	Stable Growth	7.60%	9.92%
Return on capital	High Growth	20.70%	9.69%
	Stable Growth	7.60%	9.92%
Reinvestment Rate	High Growth	57.13%	70.83%
	Stable Growth	39.47%	40.32%
Expected growth rate	High Growth	11.83%	6.86%
	Stable Growth	3.00%	4.00%

Terminal Value and Growth

	KRKA		Adris Grupa	
Stable Growth Rate	Reinvestment Rate	Value of firm	Reinvestment Rate	Value of firm
0%	0.00%	€ 4,400	0.00%	HRK 6,155
1%	13.16%	€ 4,400	10.06%	HRK 6,155
2%	26.31%	€ 4,400	20.11%	HRK 6,155
3%	39.47%	€ 4,400	30.17%	HRK 6,155
4%	52.62%	€ 4,400	40.23%	HRK 6,155
5%	65.78%	€ 4,400	50.28%	HRK 6,155

V. Tying up Loose Ends

For firm value to equity value per share

1. Value cash and other non-operating assets

When you discount operating cash flows at the cost of capital, you have valued only the operating assets (that contribute to the operating income) of the firm. Any assets whose earnings are not counted as part of operating income have not been valued yet. In particular, these would include:

- Cash and marketable securities: The income from these are not part of operating income. Hence, the current value of these assets has to be added to the value of the operating assets.
- Non-operating assets: If the firm own other assets that have value but do not contribute to operations, the value of these assets should also be included in the firm value.
- The key, though, is to not double count an asset. Thus, an asset (say your office headquarters building) that has value but is used for operations should not be added on to the value of operating assets.
2. Dealing with Holdings in Other firms

Cross holdings in other firms can create problems because the accounting for these holdings can vary widely across countries, across companies and even within the same company, across different holdings. In particular, we care about

• How the income from these holdings is accounted for in the income statement

- What is counted as income? (Operating income, Net income or just dividends)
- Where is it shown? (Above or below the operating income line)
- How much of the income is shown? (The share of the holding, 100%?)
- How is the value of the asset recorded on the balance sheet?
 - Is it recorded at original cost, updated book value or market value?
 - Is just the net value of the holding shown or are all of the assets and liabilities recorded?

How to value holdings in other firms.. In a perfect world..

In a perfect world, we would strip the parent company from its subsidiaries and value each one separately. The value of the combined firm will be

- Value of parent company + Proportion of value of each subsidiary
- To do this right, you will need
 - to be provided detailed information on each subsidiary to estimated cash flows and discount rates.
 - To have a manageable number of subsidiaries

Three compromise solutions...

- <u>The market value solution</u>: When the subsidiaries are publicly traded, you could use their traded market capitalizations to estimate the values of the cross holdings. You do risk carrying into your valuation any mistakes that the market may be making in valuation.
- <u>The relative value solution</u>: When there are too many cross holdings to value separately or when there is insufficient information provided on cross holdings, you can convert the book values of holdings that you have on the balance sheet (for both minority holdings and minority interests in majority holdings) by using the average price to book value ratio of the sector in which the subsidiaries operate.
- The "take what I can get" solution: Estimate the market value of those holdings that are publicly traded, the relative value of those holdings where there are publicly traded investments to obtain multiples from and book value for the rest.

3. Subtract out "debt"

If you have under funded pension fund or health care plans, you should consider the under funding at this stage in getting to the value of equity.

- If you do so, you should not double count by also including a cash flow line item reflecting cash you would need to set aside to meet the unfunded obligation.
- You should not be counting these items as debt in your cost of capital calculations....
- If you have contingent liabilities for example, a potential liability from a lawsuit that has not been decided - you should consider the expected value of these contingent liabilities
 - Value of contingent liability = Probability that the liability will occur * Expected value of liability

4. Value other claims on equity

- In recent years, firms have turned to giving employees (and especially top managers) equity option packages as part of compensation. These options are usually
 - Long term
 - At-the-money when issued
 - On volatile stocks
- Options outstanding
 - Step 1: List all options outstanding, with maturity, exercise price and vesting status.
 - Step 2: Value the options, taking into accouting dilution, vesting and early exercise considerations
 - Step 3: Subtract from the value of equity and divide by the actual number of shares outstanding (not diluted or partially diluted).

Getting to per share value

	KRKA	Adris Grupa
Value of operating assets	€ 3,577.69	HRK 4,311.77
+ Cash	€ 14.20	HRK 1,740.00
+ Holdings in other companies	€ 9.70	HRK 46.60
Value of firm	€ 3,601.59	HRK 6,098.37
- Debt	€ 165.57	HRK 149.67
- Minority interests	€ 4.25	HRK 465.01
- Options	€ 0.00	HRK 5,483.69
Value of equity in stock	€ 3,431.77	HRK 5,483.69

Corporate Finance meets Value: The secret to value enhancement

Price Enhancement versus Value Enhancement



Aswath Damodaran

NAME THAT STOCK

New Markets, New Names

In the bull market, adding dot-com to a company name made a stock soar. Lately those zippy new monikers are disappearing.



New Name, Higher Price

But the stocks still get a bounce when dotcom goes away. Chart shows returns in the days before and after the name change.



Sources: Thomson Datastream; P. Raghavendra Rau, Michael J. Cooper, Igor Osobov, Purdue Univ.; Ajay Khorana, Virginia Univ.; Ajay Patel, Wake Forest Univ.

Value-Neutral Actions

- Stock splits and stock dividends change the number of units of equity in a firm, but cannot affect firm value since they do not affect cash flows, growth or risk.
- <u>Accounting decisions</u> that affect reported earnings but not cash flows should have no effect on value.
 - <u>Changing inventory valuation methods</u> from FIFO to LIFO or vice versa in financial reports but not for tax purposes
 - <u>Changing the depreciation method</u> used in financial reports (but not the tax books) from accelerated to straight line depreciation
 - <u>Major non-cash restructuring charges</u> that reduce reported earnings but are not tax deductible
 - <u>Using pooling instead of purchase</u> in acquisitions cannot change the value of a target firm.
- Decisions that create new securities on the existing assets of the firm (without altering the financial mix) such as <u>tracking stock</u>.

The Paths to Value Creation.. Back to the determinants of value..



Value Creation 1: Increase Cash Flows from Assets in Place



Value Creation 2: Increase Expected Growth

- Keeping all else constant, increasing the expected growth in earnings will increase the value of a firm.
- The expected growth in earnings of any firm is a function of two variables:
 - The amount that the firm reinvests in assets and projects
 - The quality of these investments



Value Creating Growth... Evaluating the Alternatives..



Aswath Damodaran

Seven reasons why acquisitions fail...

- 1. <u>Risk Transference</u>: Attributing acquiring company risk characteristics to the target firm. Just because you are a safe firm and operate in a secure market, does not mean that you can transfer these characteristics to a target firm.
- 2. <u>Debt subsidies</u>: Subsiding target firm stockholders for the strengths of the acquiring firm is providing them with a benefit they did not earn.
- 3. <u>Auto-pilot Control</u>: Adding 20% or some arbitrary number to the market price just because other people do it is a recipe for overpayment. Using silly rules such as EPS accretion just makes the problem worse.
- 4. <u>Elusive Synergy</u>: While there is much talk about synergy in mergers, it is seldom valued realistically or appropriately.
- 5. <u>Its all relative</u>: The use of transaction multiples (multiples paid by other acquirers in acquisitions) perpetuates over payment.
- 6. <u>Verdict first, trial afterwards</u>: Deciding you want to do an acquisition first and then looking for justification for the price paid does not make sense.
- 7. <u>It's not my fault:</u> Holding no one responsible for delivering results is a sure-fire way not to get results...

III. Building Competitive Advantages: Increase length of the growth period



Value Creation 4: Reduce Cost of Capital



Debt Ratio	Beta	Cost of Equity	Bond Rating	Interest rate on debt	Tax Rate	Cost of Debt (after-tax)	WACC	Firm Value (G)
0%	0.61	7.04%	AAA	4.10%	21.00%	3.24%	7.04%	€ 2,459
10%	0.67	7.39%	AAA	4.10%	21.00%	3.24%	6.97%	€ 2,479
20%	0.74	7.83%	AA	4.35%	21.00%	3.44%	6.95%	€ 2,486
30%	0.82	8.40%	А	4.85%	21.00%	3.83%	7.03%	€ 2,460
40%	0.94	9.16%	BB	7.60%	21.00%	6.00%	7.90%	€ 2,203
50%	1.10	10.22%	В	8.85%	21.00%	6.99%	8.61%	€ 2,029
60%	1.34	11.82%	CC	13.60%	21.00%	10.74%	11.17%	€ 1,580
70%	1.75	14.47%	CC	13.60%	21.00%	10.74%	11.86%	€ 1,491
80%	2.59	20.03%	CC	13.60%	19.51%	10.95%	12.76%	€ 1,389
90%	5.31	37.86%	С	15.60%	15.12%	13.24%	15.70%	€ 1,137

As D/E ratio changes, the Levered Beta = Unlevered Beta (1+ (1-t) (D/E)) Debt increases -> Interest Expenses increase -> Interest coverage ratio decreases -> Ratings drop -> Cost of debt increases

Optimal Financing Mix: Adris Grupa

Debt Ratio	Beta	Cost of Equity	Bond Rating	Interest rate on debt	Tax Rate	Cost of Debt (after-tax)	WACC	Firm Value (G)
0%	0.69	10.56%	AAA	6.75%	20.00%	5.40%	10.56%	HRK 5,346
10%	0.75	11.12%	AAA	6.75%	20.00%	5.40%	10.55%	HRK 5,353
20%	0.82	11.83%	А	7.50%	20.00%	6.00%	10.66%	HRK 5,280
30%	0.92	12.73%	BB	10.25%	20.00%	8.20%	11.37%	HRK 4,846
40%	1.05	13.93%	В	11.50%	20.00%	9.20%	12.04%	HRK 4,496
50%	1.23	15.61%	B-	11.75%	20.00%	9.40%	12.51%	HRK 4,279
60%	1.51	18.14%	CC	16.25%	20.00%	13.00%	15.06%	HRK 3,381
70%	2.01	22.74%	CC	16.25%	17.36%	13.43%	16.22%	HRK 3,082
80%	3.06	32.40%	С	18.25%	13.52%	15.78%	19.11%	HRK 2,522
90%	6.11	60.56%	С	18.25%	12.02%	16.06%	20.51%	HRK 2,315

If debt is cheaper than equity (and it is), why is there no benefit to borrowing money?



Aswath Damodaran

The value of a voting share

The value of a voting share derives entirely from the capacity you have to change the way the firm is run. In this case, we have two values for Adris Grupa's Equity.

Status Quo Value of Equity = 5,469 million HKR

All shareholders, common and preferred, get an equal share of the status quo value.

Value for a non-voting share = 5469/(9.616+6.748) = 334 HKR/share

Optimal value of Equity = 5,735 million HKR

Value of control at Adris Grupa = 5,735 - 5469 = 266 million HKR

Only voting shares get a share of this value of control

Value per voting share =334 HKR + 266/9.616 = 362 HKR

V. From fair value to fair price..

There is many a slip between the cup and the lip...

Are markets fair?

In an efficient market, the market price converges instantaneously on value. Thus, a firm that takes value increasing actions will see its stock price go up and a firm that is value destructive will be punished by the market.

- In practice, there are three potential impediments to this process working smoothly:
 - Investors may be irrational and/or short term.
 - Markets may not trust the managers of the firm.
 - Information about the actions may not get to markets or the message may be muddled.

I. The "right" investors

Optimally, a firm that is focused on long term value would like to get investors who

- Have long time horizons
- Care about fundamentals
- Do their research/homework
- While firms do not get to pick their investors, they can influence the composition by
 - Having a core of long term investors who may also be insiders in the firm
 - Choosing a dividend policy that attracts the right type of investors
 - What they focus on when they make decisions

II. Management Trust

- Management trust is earned through a history of being focused on delivering value to investors. In other words, firms that have delivered solid returns to stockholders over time and taken good investments earn the trust of their stockholders, whereas firms that have delivered poor returns or over promised lose that trust.
- When a firm loses the trust of its stockholders, it will not only find every action that it takes subjected to scrutiny and scrutiny but will come under intense pressure to return more of its cash to stockholders.

A Symbol of Distrust How much cash is too much cash?



III. Information Gaps

For markets to react appropriately to actions taken by a firm, information about those actions has to be conveyed clearly and credibly to markets. In practice, information disclosure is hindered by

- An unwillingness to provide "key" details of actions, for fear of letting competitors in on secrets.
- A belief that investors are not intelligent or informed enough to use information appropriately.
- An inability to communicate effectively and directly.
- Complexity and confusion in the disclosure,
- Managers will be better served trusting their investors to make the right judgments about actions and providing them with the information (positive and negative) to make these judgments.

Information Overload A Discount for Complexity

	Company A	Company B			
Operating Income	5 1 billion	\$ 1 billion			
Tax rate	40%	40%			
ROIC	10%	10%			
Expected Growth	5%	5%			
Cost of capital	8%	8%			
Business Mix	Single Business	Multiple Businesses			
Holdings	Simple	Complex			
Accounting	Transparent	Opaque			

■ Which firm would you value more highly?

Measuring Complexity: Volume of Data in Financial Statements

Company	Number of pages in last $10Q$	Number of pages in last 10K
General Electric	65	410
Microsoft	63	218
Wal-mart	38	244
Exxon Mobil	86	332
Pfizer	171	460
Citigroup	252	1026
Intel	69	215
AIG	164	720
Johnson & Johnson	63	218
IBM	85	353

Measuring Complexity: A Complexity Score

tem	Factors	Follow-up Question	Answer	Weighting factor	Gerdau Score	GE Score
Operating Income	1. Multiple Businesses	Number of businesses (with more than 10% of				
		revenues) =	1	2.00	2	30
	2. One-time income and expenses	Percent of operating income =	10%	10.00	1	0.8
	3. Income from unspecified sources	Percent of operating income =	0%	10.00	0	1.2
	4. Items in income statement that are volatile	Percent of operating income =	15%	5.00	0.75	1
ax Rate	1. Income from multiple locales	Percent of revenues from non-domestic locales =	70%	3.00	2.1	1.8
	2. Different tax and reporting books	Yes or No	No	Yes=3	0	3
	3. Headquarters in tax havens	Yes or No	No	Yes=3	0	0
	4. Volatile effective tax rate	Yes or No	Yes	Yes=2	2	0
apital Expenditures	1. Volatile capital expenditures	Ves or No	Vec	Vec-2	2	2
	2. Frequent and large acquisitions	Vec er Ne	Vac	Voc-4	2	1
	3. Stock payment for acquisitions and		105	105-4	4	4
	investments	Yes or No	No	Yes=4	0	4
orking capital	1. Unspecified current assets and current					
	liabilities	Yes or No	No	Yes=3	0	0
	2. Volatile working capital items	Yes or No	Yes	Yes=2	2	2
xpected Growth rate	1. Off-balance sheet assets and liabilities					
	(operating leases and R&D)	Yes or No	No	Yes=3	0	3
	2. Substantial stock buybacks	Ves or No	No	Ves-3	0	3
	3. Changing return on capital over time	Is your raturn on conital valatile?	Vac	Voc-5	5	5
	4. Unsustainably high return	Is your feturi on capital volatile?	ICS NL-	Ver 5	3	5
ost of capital	1. Multiple businesses	is your firm's ROC much nigher than industry average?		res=5	0	0
1	2. Operations in emerging markets	Number of businesses (more than 10% of revenues) =	1	1.00	1	20
	3 Is the debt market traded?	Percent of revenues=	50%	5.00	2.5	2.5
	1 Does the company have a rating?	Yes or No	No	No=2	2	0
	F. Does the company have a fatting?	Yes or No	Yes	No=2	0	0
	5. Does the company have on-balance sheet					
o-operating assets	Minority holdings as percent of book assets	Yes or No	No	Yes=5	0	5
rm to Equity value	Consolidation of subsidiarias	Minority holdings as percent of book assets	0%	20.00	0	0.8
		Minority interest as percent of book value of equity	63%	20.00	12.6	1.2
er snare value	Snares with different voting rights	Does the firm have shares with different voting rights?	Yes	Yes = 10	10	0
	Equity options outstanding	Options outstanding as percent of shares	0%	10.00	0	0.25
		Complexity Score =			48.95	90.55

Aswath Damodaran

Relative Valuation

Aswath Damodaran

Aswath Damodaran

Relative valuation is pervasive...

Most asset valuations are relative.

- Most equity valuations on Wall Street are relative valuations.
 - Almost 85% of equity research reports are based upon a multiple and comparables.
 - More than 50% of all acquisition valuations are based upon multiples
 - Rules of thumb based on multiples are not only common but are often the basis for final valuation judgments.
- While there are more discounted cashflow valuations in consulting and corporate finance, they are often relative valuations masquerading as discounted cash flow valuations.
 - The objective in many discounted cashflow valuations is to back into a number that has been obtained by using a multiple.
 - The terminal value in a significant number of discounted cashflow valuations is estimated using a multiple.

The Reasons for the allure...

"If you think I'm crazy, you should see the guy who lives across the hall" Jerry Seinfeld talking about Kramer in a Seinfeld episode

" A little inaccuracy sometimes saves tons of explanation" H.H. Munro

" If you are going to screw up, make sure that you have lots of company" Ex-portfolio manager

The Four Steps to Deconstructing Multiples

Define the multiple

- In use, the same multiple can be defined in <u>different ways</u> by different users. When comparing and using multiples, estimated by someone else, it is critical that we <u>understand how the multiples have been estimated</u>
- Describe the multiple
 - Too many people who use a multiple have <u>no idea what its cross sectional</u> <u>distribution</u> is. If you do not know what the cross sectional distribution of a multiple is, it is difficult to look at a number and pass judgment on whether it is too high or low.
- Analyze the multiple
 - It is critical that we <u>understand the fundamentals</u> that drive each multiple, and the <u>nature of the relationship</u> between the multiple and each variable.
- Apply the multiple
 - Defining the <u>comparable universe</u> and <u>controlling for differences</u> is far more difficult in practice than it is in theory.

Definitional Tests

Is the multiple consistently defined?

 Proposition 1: Both the value (the numerator) and the standardizing variable (the denominator) should be to the same claimholders in the firm. In other words, the value of equity should be divided by equity earnings or equity book value, and firm value should be divided by firm earnings or book value.

Is the multiple uniformly estimated?

- The variables used in defining the multiple <u>should be estimated uniformly</u> across assets in the "comparable firm" list.
- If earnings-based multiples are used, the <u>accounting rules</u> to measure earnings should be applied consistently across assets. The same rule applies with book-value based multiples.

Example 1: Price Earnings Ratio: Definition

PE = Market Price per Share / Earnings per Share

There are a number of variants on the basic PE ratio in use. They are based upon how the price and the earnings are defined.

- Price: is usually the current price is sometimes the average price for the year
- EPS:earnings per share in most recent financial year
earnings per share in trailing 12 months (Trailing PE)
forecasted earnings per share next year (Forward PE)
forecasted earnings per share in future year

Example 2: Enterprise Value /EBITDA Multiple

The enterprise value to EBITDA multiple is obtained by netting cash out against debt to arrive at enterprise value and dividing by EBITDA. Enterprise Value Market Value of Equity + Market Value of Debt - Cash

 $\frac{\text{EBITDA}}{\text{EBITDA}} = \frac{\text{Market Value of Equily + Market Value of Best - Cas}}{\text{Earnings before Interest, Taxes and Depreciation}}$

- Why do we net out cash from firm value?
- What happens if a firm has cross holdings which are categorized as:
 - Minority interests?
 - Majority active interests?
Descriptive Tests

- What is the <u>average and standard deviation</u> for this multiple, across the universe (market)?
 - What is the <u>median</u> for this multiple?
 - The median for this multiple is often a more reliable comparison point.
 - How <u>large are the outliers</u> to the distribution, and <u>how do we deal</u> with the outliers?
 - Throwing out the outliers may seem like an obvious solution, but if the outliers all lie on one side of the distribution (they usually are large positive numbers), this can lead to a biased estimate.
- Are there cases where the multiple <u>cannot be estimated</u>? Will ignoring these cases lead to a <u>biased estimate</u> of the multiple?
- How has this multiple <u>changed over time?</u>

Looking at the distribution of PE ratios...



PE: Deciphering the Distribution

		Jan-09		Jan-08				
	Current PE	Trailing PE	Forward PE	Current PE	Trailing PE	Forward PE		
Mean	18.91	17.48	20.04	45.02	32.44	32.21		
Standard								
Error	0.98	0.91	0.87	4.64	1.96	1.47		
Median	9.80	9.89	11.69	18.16	17.00	17.28		
Standard								
Deviation	61.97	55.61	45.74	299.11	123.29	80.82		
Kurtosis	668.30	1073.76	174.18	1618.20	1241.97	269.80		
Skewness	21.06	27.18	11.66	35.41	30.30	14.23		
Maximum	2442.83	2475.71	933.00	15126.20	5713.00	1912.33		
Count	4010	3737	2795	4155	3944	3004		
Sample size	6871	6871	6871	7155	7155	7155		
Largest(400)	29.50	26.18	25.06					
Smallest(400)	3.00	2.76	5.74					

Comparing PE Ratios: US, Europe, Japan and Emerging Markets



US Emerging Markets Europe Japan

And isolating Eastern Europe



And 6 times EBITDA may not be cheap...



Analytical Tests

What are the <u>fundamentals</u> that determine and drive these multiples?

- Proposition 2: Embedded in every multiple are all of the variables that drive every discounted cash flow valuation growth, risk and cash flow patterns.
- In fact, using a simple discounted cash flow model and basic algebra should yield the fundamentals that drive a multiple
- How do <u>changes in these fundamentals</u> change the multiple?
 - The relationship between a fundamental (like growth) and a multiple (such as PE) is seldom linear. For example, if firm A has twice the growth rate of firm B, it will generally not trade at twice its PE ratio
 - Proposition 3: It is impossible to properly compare firms on a multiple, if we do not know the nature of the relationship between fundamentals and the multiple.

PE Ratio: Understanding the Fundamentals

To understand the fundamentals, start with a basic <u>equity</u> discounted cash flow model.

With the dividend discount model, $P_0 = \frac{DPS_1}{r - g_n}$

Dividing both sides by the current earnings per share,

 $\frac{P_0}{EPS_0} = PE = \frac{Payout Ratio * (1 + g_n)}{r - g_n}$

■ If this had been a FCFE Model,



The Determinants of Multiples...



Application Tests

Given the firm that we are valuing, what is a "comparable" firm?

- While traditional analysis is built on the premise that firms in the same sector are comparable firms, valuation theory would suggest that a comparable firm is one which is similar to the one being analyzed in terms of fundamentals.
- Proposition 4: There is no reason why a firm cannot be compared with another firm in a very different business, if the two firms have the same risk, growth and cash flow characteristics.
- Given the comparable firms, how do we adjust for differences across firms on the fundamentals?
 - Proposition 5: It is impossible to find an exactly identical firm to the one you are valuing.

An Example: Comparing Multiples across a Sector: KRKA

Company							EV/ Invested		Return on	Return on Capital (ROC or	Net Profit	Pre-tax Operating
Name	Current PE	Trailing PE	Forward PE	PBV	PS	EV/EBITDA	Capital	EV/Sales	Equity	ROIC)	Margin	Margin
Sanitas AB			5.29	0.96	0.79	6.16	0.98	1.64	-3.58%	6.20%	-4.12%	13.41%
Deva Holding AS				1.60	2.39		1.46	2.87	-12.32%	-0.99%	-10.94%	-1.67%
EIS Eczacibasi	19.62	19.62	4.58		1.75	124.82		1.75			8.93%	-0.69%
Ilaç Sanayi ve Ticaret A.S.												
Genera d.d.				0.63	0.69	44.56	0.68	0.87			-21.93%	-3.70%
Pharmstanda rd Group	19.44	16.56	19.74	4.78	4.75	10.99	4.92	4.71	30.61%	41.49%	23.83%	36.77%
Veropharm Co. Ltd.	7.78	8.06	7.44	1.98	1.66	5.98	1.93	1.82	24.04%	27.47%	22.84%	27.26%
Antibiotice S.A.	26.65	26.65	15.36		1.30	4.33		1.30	7.49%	22.80%	4.87%	17.90%
AS Olainfarm		10.94	8.52	0.81	0.67	14.84	0.89	1.02	8.31%	8.50%	5.83%	8.31%
BioFarm SA												
Biovet JSC												
JSC Grindeks	4.13	11.41	4.92	0.72	0.60	3.96	0.77	0.81	7.00%	6.81%	5.81%	6.45%
KrKa dd Novo Mesto	14.20	13.79	13.00	2.48	2.33	7.69	2.34	2.51	21.28%	28.04%	16.12%	25.17%
Average	15.30	15.29	10.51	1.86	1.79	27.14	1.86	1.96	12.34%	19.16%	6.15%	12.87%
Median	16.82	13.79	8.52	1.60	1.66	9.34	1.46	1.75	8.31%	22.80%	5.83%	8.31%

PBV versus ROE – East European Pharmaceuticals

Dependent variable is: PBV

R squared = 48.3%

PBV = 1.16 + 9.13 ROE(1.33) (2.57)

Evaluating KRKA, with its ROE of 21.28%: Predicted PBV for KRKA = 1.16 + 9.13 (.2128) = 3.1028Actual PBV for KRKA = 2.48Stock is undervalued by about 20% (3.10/2.48)

Real Options: Fact and Fantasy

Aswath Damodaran

The Basis for Real Options

In the last few years, there are some who have argued that discounted cashflow valuations under valued some companies and that a real option premium should be tacked on to DCF valuations. To understanding its moorings, compare the two trees below:



2. Make better decisions based on learning

When is there an option embedded in an action?

- An option provides the holder with the **right** to buy or sell a specified quantity of an underlying asset at a fixed price (called a strike price or an exercise price) at or before the expiration date of the option.
- There has to be a <u>clearly defined underlying asset</u> whose value changes over time in unpredictable ways.
- The <u>payoffs on this asset</u> (real option) have to be <u>contingent on an specified</u> <u>event</u> occurring within a finite period.







When does the option have significant economic value?

- For an option to have significant economic value, there has to be a <u>restriction</u> <u>on competition in the event of the contingency</u>. In a perfectly competitive product market, no contingency, no matter how positive, will generate positive net present value.
- At the limit, real options are <u>most valuable when you have exclusivity</u> you and only you can take advantage of the contingency. They become less valuable as the barriers to competition become less steep.

Exclusivity: Putting Real Options to the Test

Product Options: Patent on a drug

- Patents restrict competitors from developing similar products
- Patents do not restrict competitors from developing other products to treat the same disease.
- Growth Options: Expansion into a new product or market
 - Barriers may range from strong (exclusive licenses granted by the government as in telecom businesses) to weaker (brand name, knowledge of the market) to weakest (first mover).

Determinants of option value

Variables Relating to Underlying Asset

- <u>Value of Underlying Asset</u>; as this value increases, the right to buy at a fixed price (calls) will become more valuable and the right to sell at a fixed price (puts) will become less valuable.
- <u>Variance in that value</u>; as the variance increases, both calls and puts will become more valuable because all options have limited downside and depend upon price volatility for upside.
- <u>Expected dividends on the asset</u>, which are likely to reduce the price appreciation component of the asset, reducing the value of calls and increasing the value of puts.
- Variables Relating to Option
 - <u>Strike Price of Options</u>; the right to buy (sell) at a fixed price becomes more (less) valuable at a lower price.
 - <u>Life of the Option</u>; both calls and puts benefit from a longer life.
- Level of Interest Rates; as rates increase, the right to buy (sell) at a fixed price in the future becomes more (less) valuable.

When can you use option pricing models to value real options?

- The notion of a replicating portfolio that drives option pricing models makes them most suited for valuing real options where
 - The underlying asset is traded this yield not only observable prices and volatility as inputs to option pricing models but allows for the possibility of creating replicating portfolios
 - An active marketplace exists for the option itself.
 - The cost of exercising the option is known with some degree of certainty.
- When option pricing models are used to value real assets, we have to accept the fact that
 - The value estimates that emerge will be far more imprecise.
 - The value can deviate much more dramatically from market price because of the difficulty of arbitrage.

Valuing a Product Patent as an option: Avonex

Biogen, a bio-technology firm, has a patent on Avonex, a drug to treat multiple sclerosis, for the next 17 years, and it plans to produce and sell the drug by itself. The key inputs on the drug are as follows:

PV of Cash Flows from Introducing the Drug Now = S =\$ 3.422 billion

PV of Cost of Developing Drug for Commercial Use = K =\$ 2.875 billion

Patent Life = t = 17 years Riskless Rate = r = 6.7% (17-year T.Bond rate)

Variance in Expected Present Values $=\sigma^2 = 0.224$ (Industry average firm variance for bio-tech firms)

Expected Cost of Delay = y = 1/17 = 5.89%

d1 = 1.1362 N(d1) = 0.8720

d2 = -0.8512 N(d2) = 0.2076

Call Value= 3,422 exp^{(-0.0589)(17)} (0.8720) - 2,875 (exp^{(-0.067)(17)} (0.2076)= 907 million

One final example: Equity as a Liquidation Option



Application to valuation: A simple example

- Assume that you have a firm whose assets are currently valued at \$100 million and that the standard deviation in this asset value is 40%.
- Further, assume that the face value of debt is \$80 million (It is zero coupon debt with 10 years left to maturity).
- If the ten-year treasury bond rate is 10%,
 - how much is the equity worth?
 - What should the interest rate on debt be?

Valuing Equity as a Call Option

Inputs to option pricing model

- Value of the underlying asset = S = Value of the firm = \$ 100 million
- Exercise price = K = Face Value of outstanding debt = \$ 80 million
- Life of the option = t = Life of zero-coupon debt = 10 years
- Variance in the value of the underlying asset = σ^2 = Variance in firm value = 0.16
- Riskless rate = r = Treasury bond rate corresponding to option life = 10%
- Based upon these inputs, the Black-Scholes model provides the following value for the call:
 - d1 = 1.5994 N(d1) = 0.9451
 - d2 = 0.3345 N(d2) = 0.6310
- Value of the call = $100 (0.9451) 80 \exp^{(-0.10)(10)} (0.6310) = 75.94 million
- Value of the outstanding debt = 100 75.94 = 24.06 million
- Interest rate on debt = $(\$ 80 / \$24.06)^{1/10} 1 = 12.77\%$

The Effect of Catastrophic Drops in Value

- Assume now that a catastrophe wipes out half the value of this firm (the value drops to \$ 50 million), while the face value of the debt remains at \$ 80 million. Consider the new inputs into the equity valuation:
 - Value of the underlying asset = S = Value of the firm = \$50 million
 - Exercise price = K = Face Value of outstanding debt = \$ 80 million
 - Life of the option = t = Life of zero-coupon debt = 10 years
 - Variance in the value of the underlying asset = σ^2 = Variance in firm value = 0.16
 - Riskless rate = r = Treasury bond rate corresponding to option life = 10%
- Based upon these inputs, the Black-Scholes model provides the following value for the call:
 - d1 = 1.0515 N(d1) = 0.8534
 - d2 = -0.2135 N(d2) = 0.4155
 - Value of the call (Equity)= 50 (0.8534) 80 $\exp^{(-0.10)(10)}(0.4155) = 30.44 million
 - Value of the debt= \$50 \$30.44 = \$19.56 million

Equity value persists ..



Back to Lemmings...

