Aswath Damodaran

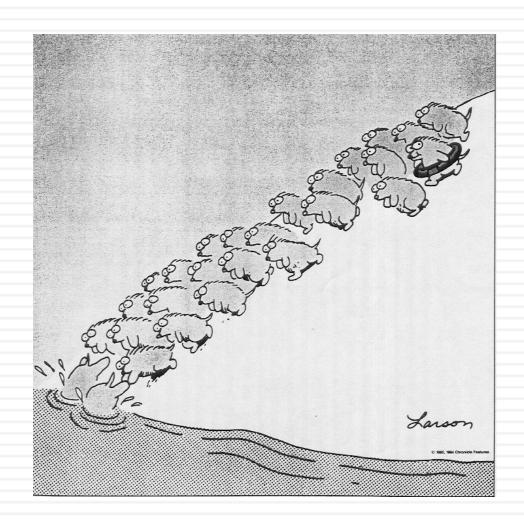
VALUATION: ART, SCIENCE OR MAGIC?

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Some Initial Thoughts

"One hundred thousand lemmings cannot be wrong"

Graffiti

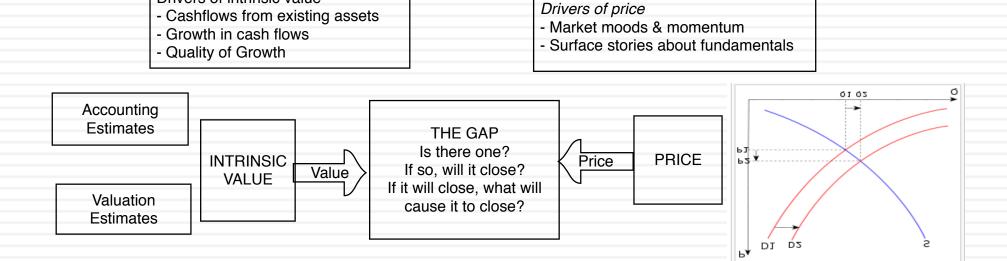


Theme 1: Characterizing Valuation as a discipline

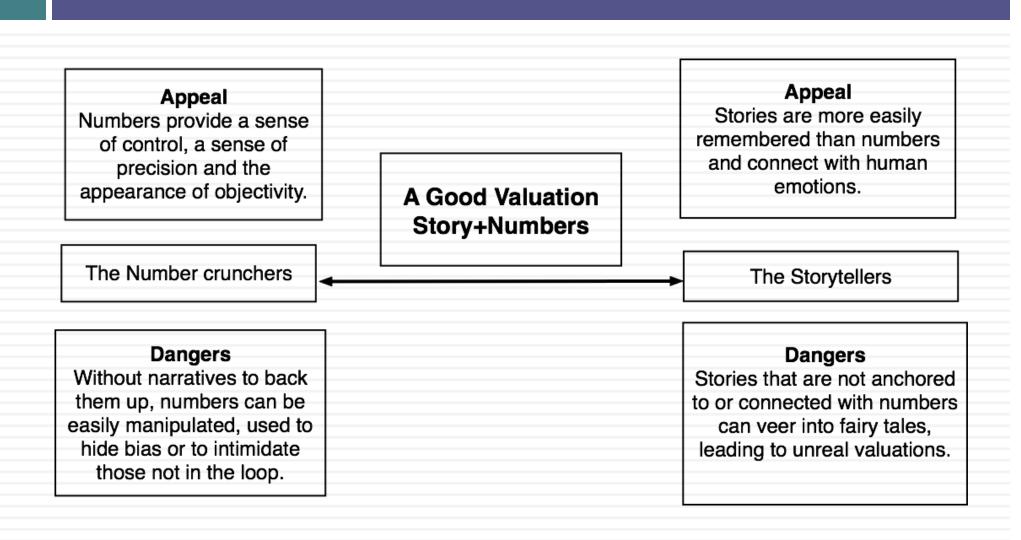
- In a science, if you get the inputs right, you should get the output right. The laws of physics and mathematics are universal and there are no exceptions. Valuation is not a science.
- In an art, there are elements that can be taught but there is also a magic that you either have or you do not. The essence of an art is that you are either a great artist or you are not. Valuation is not an art.
- A craft is a skill that you learn <u>by doing</u>. The more you do it, the better you get at it. Valuation is a craft.

Theme 2: Valuing an asset is not the same as pricing that asset

Drivers of intrinsic value



Theme 3: Good valuation = Story + Numbers



Theme 4: If you value something, you should be willing to act on it..

- There is very little theory in valuation and I am not sure what an academic valuation would like like and am not sure that I want to find out.
- Pragmatism, not purity: The end game is to estimate a value for an asset. I plan to get there, even if it means taking short cuts and making assumptions that would make purists blanch.
- To act on your valuations, you have to have faith in
 - In your own valuation judgments.
 - In markets: that prices will move towards your value estimates. That faith will have to be earned.

Misconceptions about Valuation

- Myth 1: A valuation is an objective search for "true" value
 - Truth 1.1: All valuations are biased. The only questions are how much and in which direction.
 - Truth 1.2: The direction and magnitude of the bias in your valuation is directly proportional to who pays you and how much you are paid.
- Myth 2.: A good valuation provides a precise estimate of value
 - Truth 2.1: There are no precise valuations
 - Truth 2.2: The payoff to valuation is greatest when valuation is least precise.
- Myth 3: . The more quantitative a model, the better the valuation
 - Truth 3.1: One's understanding of a valuation model is inversely proportional to the number of inputs required for the model.
 - Truth 3.2: Simpler valuation models do much better than complex ones.

Approaches to Valuation

- Intrinsic valuation, relates the value of an asset to the present value of expected future cashflows on that asset. In its most common form, this takes the form of a discounted cash flow valuation.
- Relative valuation, estimates the value of an asset by looking at the pricing of 'comparable' assets relative to a common variable like earnings, cash flows, book value or sales.
- Contingent claim valuation, uses option pricing models to measure the value of assets that share option characteristics.

Discounted Cash Flow Valuation

- What is it: In discounted cash flow valuation, the value of an asset is the present value of the expected cash flows on the asset.
- Philosophical Basis: Every asset has an intrinsic value that can be estimated, based upon its characteristics in terms of cash flows, growth and risk.
- Information Needed: To use discounted cash flow valuation, you need
 - to estimate the life of the asset
 - to estimate the cash flows during the life of the asset
 - to estimate the discount rate to apply to these cash flows to get present value
- Market Inefficiency: Markets are assumed to make mistakes in pricing assets across time, and are assumed to correct themselves over time, as new information comes out about assets.

Risk Adjusted Value: Three Basic Propositions

The value of a risky asset can be estimated by discounting the expected cash flows on the asset over its life at a risk-adjusted discount rate:

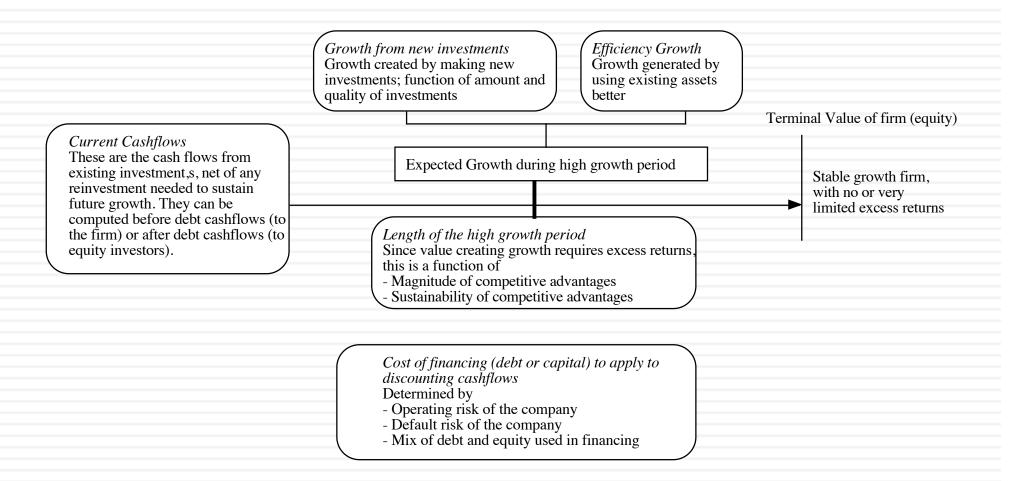
Value of asset =
$$\frac{E(CF_1)}{(1+r)} + \frac{E(CF_2)}{(1+r)^2} + \frac{E(CF_3)}{(1+r)^3} + \dots + \frac{E(CF_n)}{(1+r)^n}$$

- 1. The IT Proposition: If "it" does not affect the cash flows or alter risk (thus changing discount rates), "it" cannot affect value.
- The DUH Proposition: For an asset to have value, the expected cash flows have to be positive some time over the life of the asset.
- The DON'T FREAK OUT Proposition: Assets that generate cash flows early in their life will be worth more than assets that generate cash flows later; the latter may however have greater growth and higher cash flows to compensate.

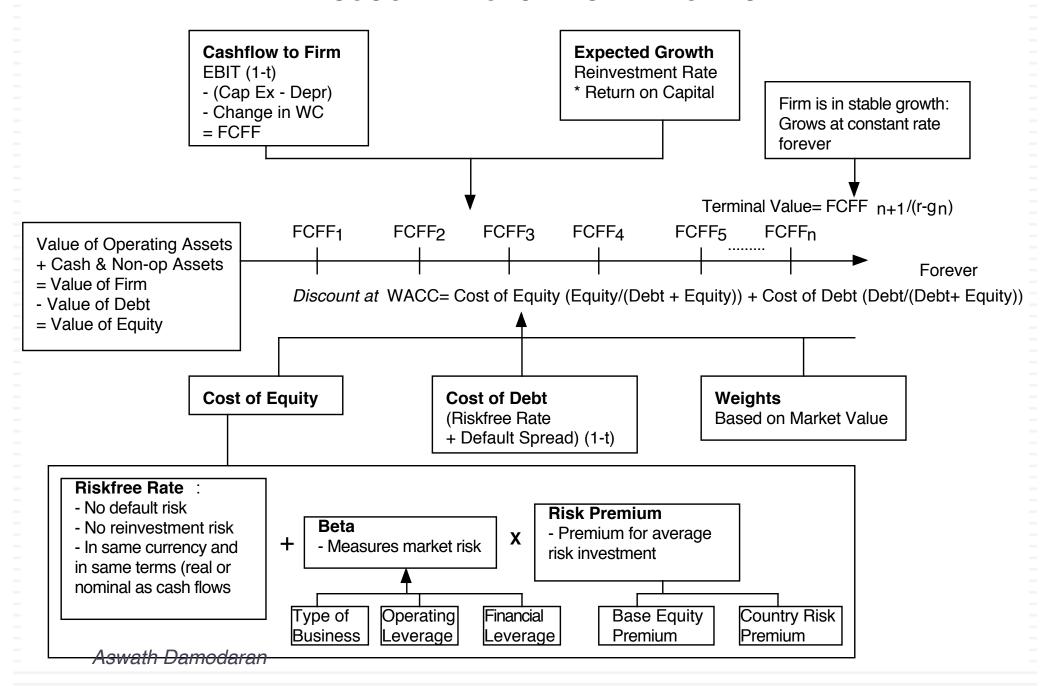
DCF Choices: Equity Valuation versus Firm Valuation

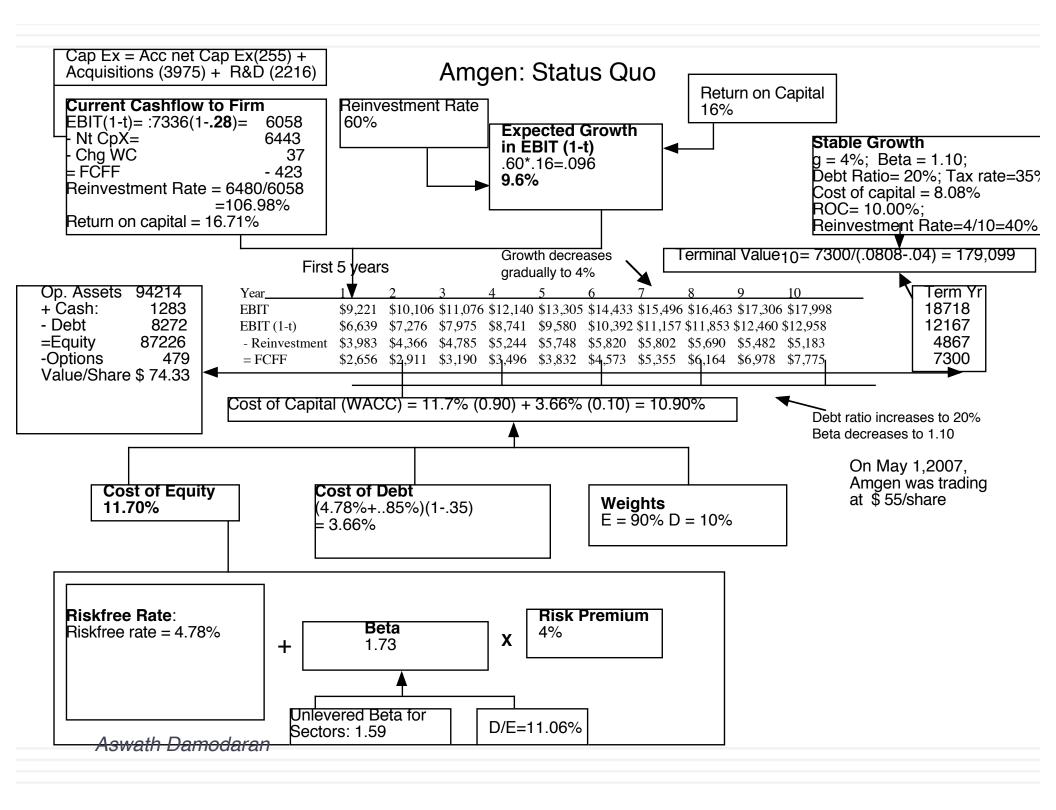
Firm Valuation: Value the entire business Liabilities **Assets Existing Investments** Fixed Claim on cash flows Assets in Place Debt Generate cashflows today Little or No role in management Includes long lived (fixed) and Fixed Maturity short-lived(working Tax Deductible capital) assets Growth Assets **Equity** Residual Claim on cash flows Expected Value that will be Significant Role in management created by future investments Perpetual Lives Equity valuation: Value just the equity claim in the business

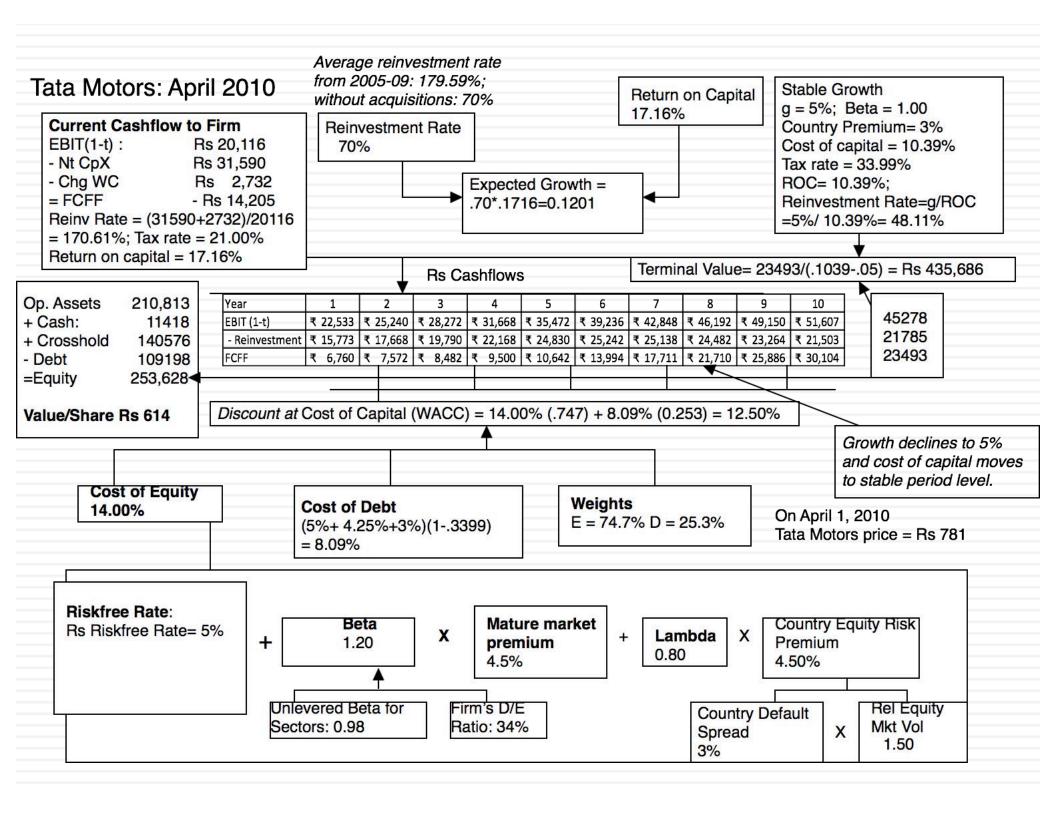
The Drivers of Value...

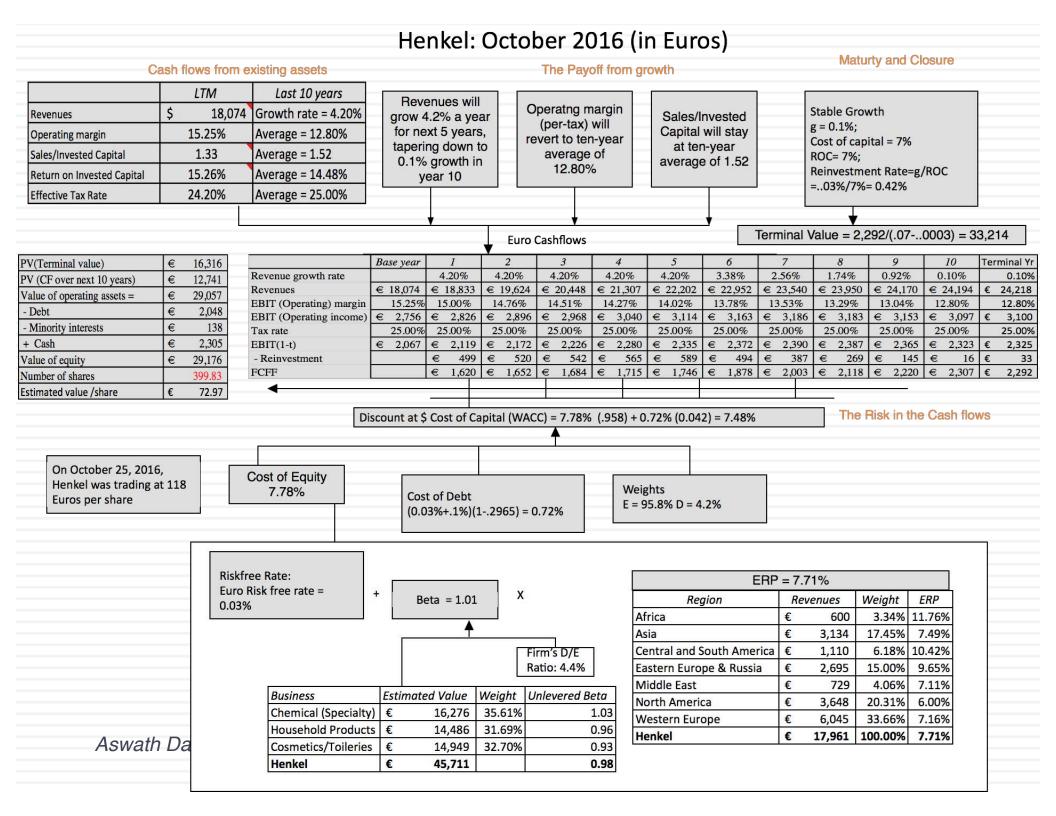


DISCOUNTED CASHFLOW VALUATION





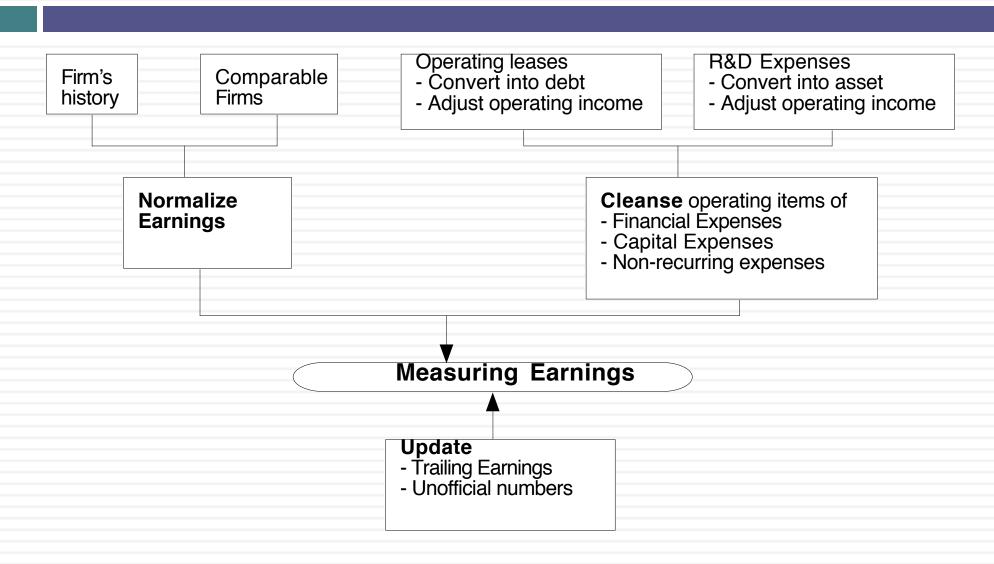




DCF INPUTS

"Garbage in, garbage out"

I. Measure earnings right...



Operating Leases at Amgen in 2007

Amgen has lease commitments and its cost of debt (based on it's A rating) is 5.63%.

Year	Commitment	Present Value
1	\$96.00	\$90.88
2	\$95.00	\$85.14
3	\$102.00	\$86.54
4	\$98.00	\$78.72
5	\$87.00	\$66.16
6-12	\$107.43	\$462.10 (\$752 million prorated)

□ Debt Value of leases =

- \$869.55
- Debt outstanding at Amgen = \$7,402 + \$870 = \$8,272 million
- Adjusted Operating Income = Stated OI + Lease expense this year Depreciation
 = 5,071 m + 69 m 870/12 = \$5,068 million (12 year life for assets)
- □ Approximate Operating income= stated OI + PV of Lease commitment * Pre-tax cost of debt
- = \$5,071 m + 870 m (.0563) = \$ 5,120 million

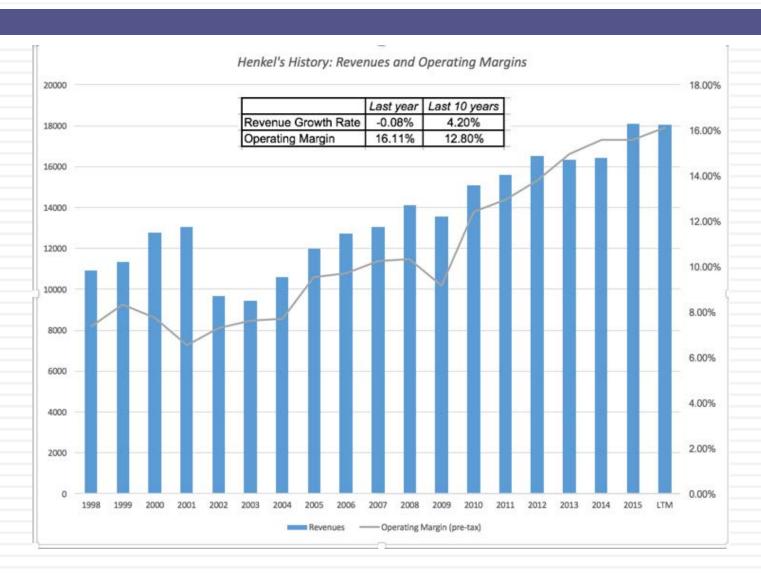
Capitalizing R&D Expenses: Amgen

R & D was assumed to have a 10-year life.

Year	R&D Expense	Unamortiz	ed portion	Amortization this year
Current	3366.00	1.00	3366.00	
-1	2314.00	0.90	2082.60	\$231.40
-2	2028.00	0.80	1622.40	\$202.80
-3	1655.00	0.70	1158.50	\$165.50
-4	1117.00	0.60	670.20	\$111.70
-5	865.00	0.50	432.50	\$86.50
-6	845.00	0.40	338.00	\$84.50
-7	823.00	0.30	246.90	\$82.30
-8	663.00	0.20	132.60	\$66.30
-9	631.00	0.10	63.10	\$63.10
-10	558.00		0.00	\$55.80
Value of Research Ass	et =		\$10,112.80	\$1,149.90
-2 -3 -4 -5 -6 -7 -8 -9	2028.00 1655.00 1117.00 865.00 845.00 823.00 663.00 631.00 558.00	0.80 0.70 0.60 0.50 0.40 0.30 0.20	1622.40 1158.50 670.20 432.50 338.00 246.90 132.60 63.10 0.00	\$202.80 \$165.50 \$111.70 \$86.50 \$84.50 \$82.30 \$66.30 \$63.10 \$55.80

[□] Adjusted Operating Income = \$5,120 + 3,366 - 1,150 = \$7,336 million

Henkel's Operating History



II. Get the big picture (not the accounting one) when it comes to cap ex and working capital

- Capital expenditures should include
 - Research and development expenses, once they have been recategorized as capital expenses.
 - Acquisitions of other firms, whether paid for with cash or stock.
- Working capital should be defined not as the difference between current assets and current liabilities but as the difference between non-cash current assets and nondebt current liabilities.
- On both items, start with what the company did in the most recent year but do look at the company's history and at industry averages.

Amgen's Net Capital Expenditures

The accounting net cap ex at Amgen is small:

Accounting Capital Expenditures = \$1,218 million

- Accounting Depreciation = \$ 963 million

Accounting Net Cap Ex = \$ 255 million

We define capital expenditures broadly to include R&D and acquisitions:

Accounting Net Cap Ex = \$ 255 million

■ Net R&D Cap Ex = (3366-1150) = \$2,216 million

□ Acquisitions in 2006 = \$3,975 million

■ Total Net Capital Expenditures = \$6,443 million

 Acquisitions have been a volatile item. Amgen was quiet on the acquisition front in 2004 and 2005 and had a significant acquisition in 2003.

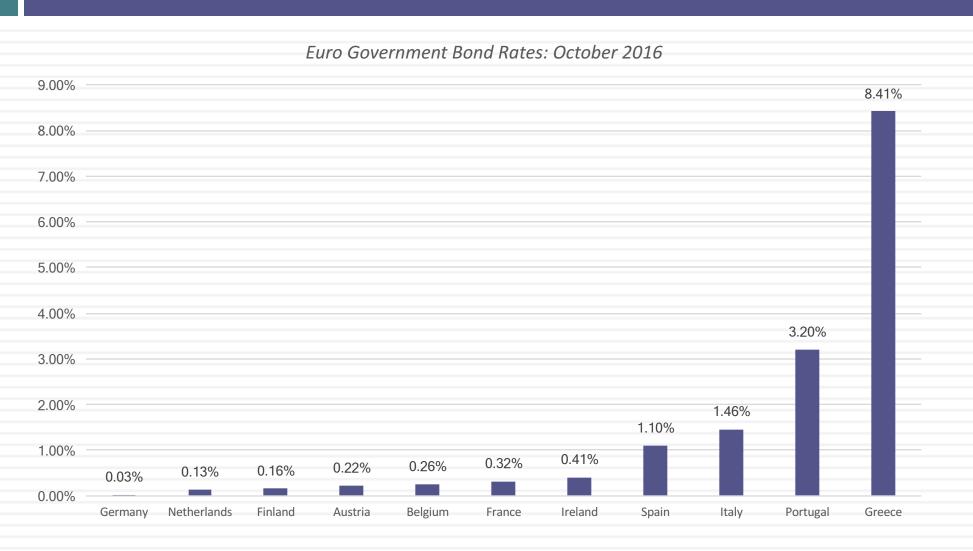
III. The government bond rate is not always the risk free rate

- When valuing Amgen in US dollars, the US\$ ten-year bond rate of 4.78% was used as the risk free rate. We assumed that the US treasury was default free.
- When valuing Tata Motors in Indian rupees in 2010, the Indian government bond rate of 8% was not default free.
 Using the Indian government's local currency rating of Ba2 yielded a default spread of 3% for India and a riskfree rate of 5% in Indian rupees.

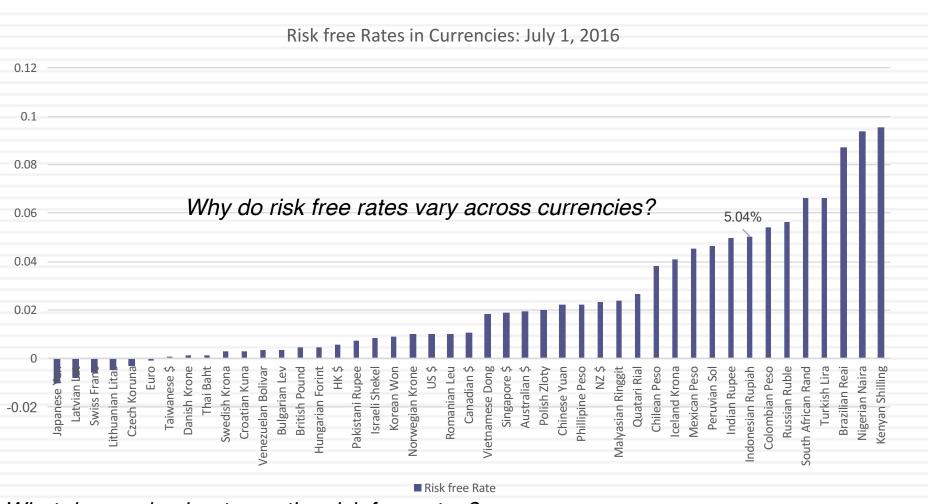
Risk free rate in Indian Rupees = 8% - 3% = 5%

To value Henkel in Euros, you need a risk free rate in Euros. Finding a ten-year government bond denominated in Euros is not the problem. But choosing which one to use might be.

Euro Risk Free Rate?



Risk free rates will vary across currencies!



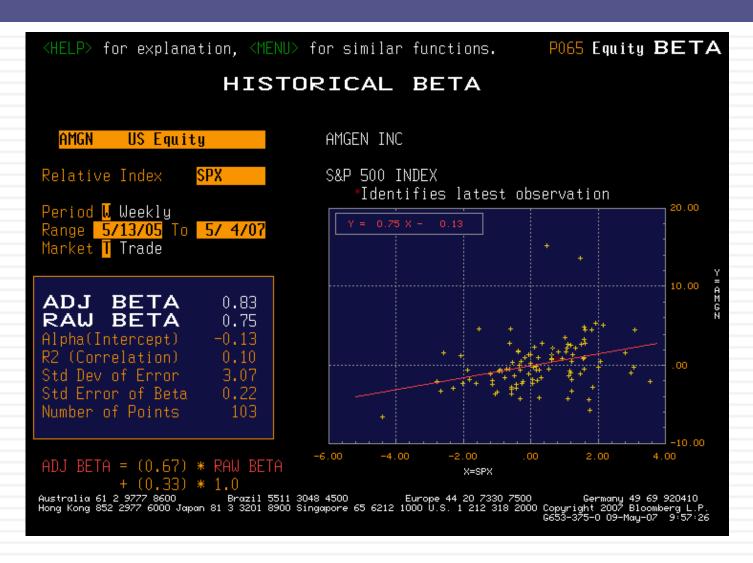
What do you do about negative risk free rates?

Aswath Damodaran

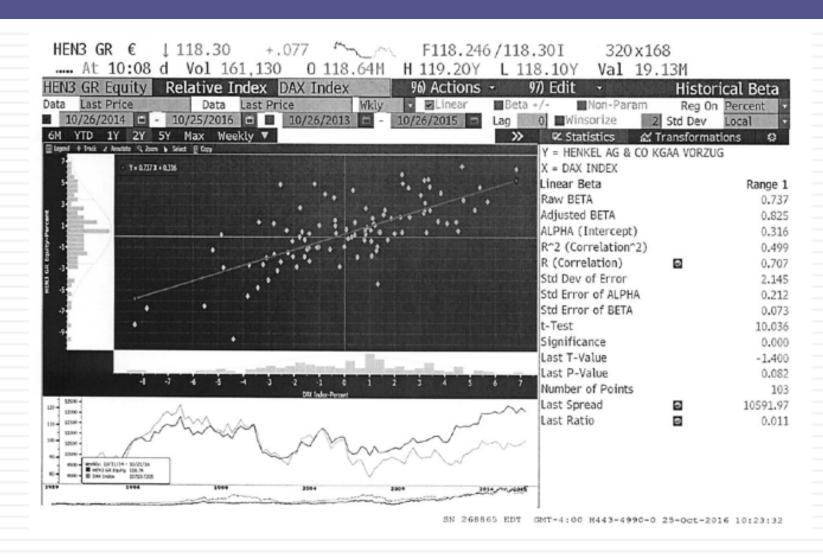
But valuations should not! Valuing Tata Motors

	In Indian Rupees	In US \$
Risk free Rate	5.00%	2.00%
Expected inflation rate	4.00%	1.00%
Cost of capital		
- High Growth	12.50%	9.25%
- Stable Growth	10.39%	7.21%
Expected growth rate		
- High Growth	12.01%	8.78%
- Stable Growth	5.00%	2.00%
Return on Capital		
- High Growth	17.16%	13.78%
- Stable Growth	10.39%	7.21%
Value per share	Rs 614	\$12.79/share (roughly Rs
		614 at current exchange
		rate)

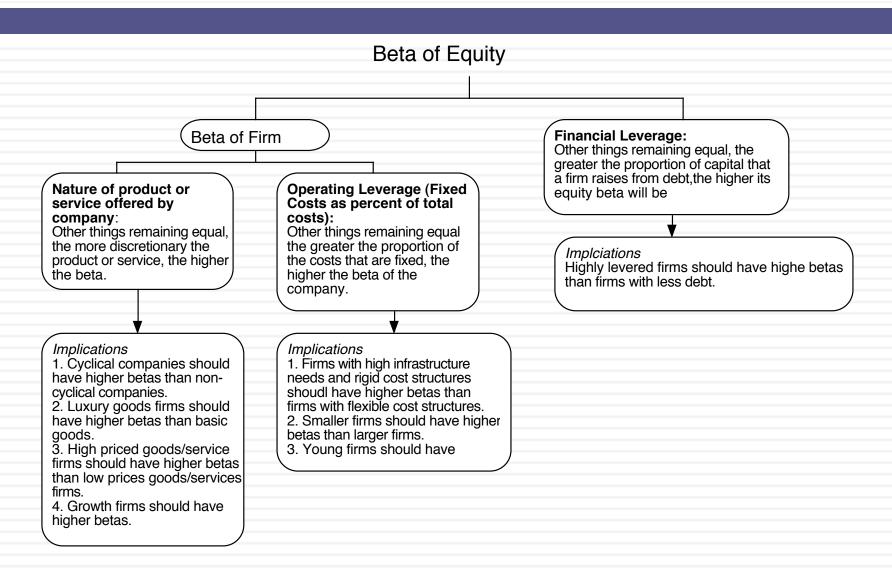
IV. Betas do not come from regressions... and are noisy...



Look better for some companies, but not if run against narrow indices



Determinants of Betas



Bottom-up Betas

Step 1: Find the business or businesses that your firm operates in.

Step 2: Find publicly traded firms in each of these businesses and obtain their regression betas. Compute the simple average across these regression betas to arrive at an average beta for these publicly traded firms. Unlever this average beta using the average debt to equity ratio across the publicly traded firms in the sample. Unlevered beta for business = Average beta across publicly traded firms/ (1 + (1-t) (Average D/E ratio across firms))

Step 3: Estimate how much value your firm derives from each of the different businesses it is in.

Step 4: Compute a weighted average of the unlevered betas of the different businesses (from step 2) using the weights from step 3. Bottom-up Unlevered beta for your firm = Weighted average of the unlevered betas of the individual business

Step 5: Compute a levered beta (equity beta) for your firm, using the market debt to equity ratio for your firm.

Levered beta = Unlevered beta (1+ (1-t) (Debt/Equity))

Possible Refinements

If you can, adjust this beta for differences between your firm and the comparable firms on operating leverage and product characteristics.

While revenues or operating income are often used as weights, it is better to try to estimate the value of each business.

If you expect the business mix of your firm to change over time, you can change the weights on a year-to-year basis.

If you expect your debt to equity ratio to change over time, the levered beta will change over time.

Three examples...

Amgen

- The unlevered beta for pharmaceutical firms is 1.59. Using Amgen's debt to equity ratio of 11%, the bottom up beta for Amgen is
 - Bottom-up Beta = 1.59(1+(1-.35)(.11)) = 1.73

Tata Motors

- The unlevered beta for automobile firms is 0.98. Using Tata Motor's debt to equity ratio of 33.87%, the bottom up beta for Tata Motors is
 - Bottom-up Beta = 0.98 (1+(1-.3399)(.3387)) = 1.20

Henkel

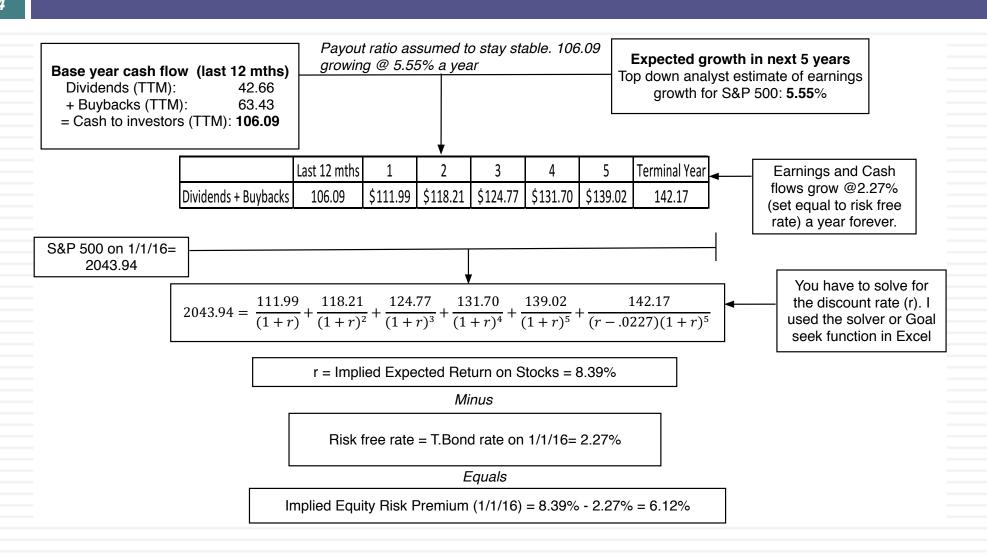
Business	Estimated Value	Weight	Unlevered Beta
Chemical (Specialty)	€ 16,276	35.61%	1.03
Household Products	€ 14,486	31.69%	0.96
Cosmetics/Toileries	€ 14,949	32.70%	0.93
Henkel	€ 45,711		0.98

Levered Beta = 0.98 (1 + (1 - .2965)(.044)) = 1.01

V. And the past is not always a good indicator of the future.

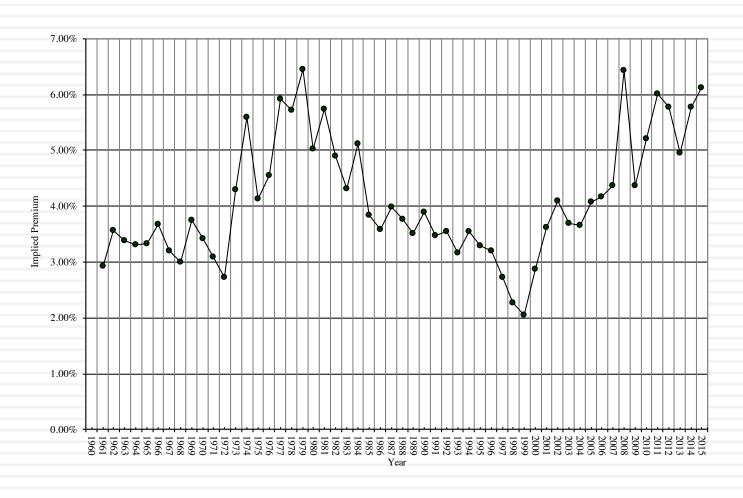
	Arithmetic Average		Geometric Average	
	Stocks - T. Bills	Stocks - T. Bonds	Stocks - T. Bills	Stocks - T. Bonds
1928-2015	7.92%	6.18%	6.05%	4.54%
Std Error	2.15%	2.29%		
1966-2015	6.05%	3.89%	4.69%	2.90%
Std Error	2.42%	2.74%		
2006-2015	7.87%	3.88%	6.11%	2.53%
Std Error	6.06%	8.66%		

- □ If you are going to use a historical risk premium, make it
 - Long term (because of the standard error)
 - Consistent with your risk free rate
 - A "compounded" average
- No matter which estimate you use, recognize that it is backward looking, is noisy and may reflect selection bias.

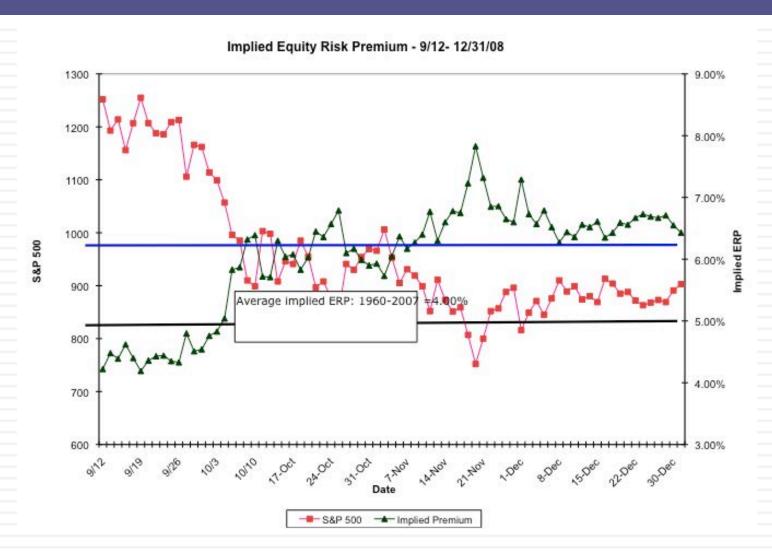


Implied Premiums in the US: 1960-2015

Implied Premium for US Equity Market: 1960-2015



The Anatomy of a Crisis: Implied ERP from September 12, 2008 to January 1, 2009



Implied Premium for India using the Sensex: April 2010

- □ Level of the Index = 17559
- FCFE on the Index = 3.5% (Estimated FCFE for companies in index as % of market value of equity)
- Other parameters
 - Riskfree Rate = 5% (Rupee)
 - Expected Growth (in Rupee)
 - Next 5 years = 20% (Used expected growth rate in Earnings)
 - After year 5 = 5%
- Solving for the expected return:
 - Expected return on Equity = 11.72%
 - Implied Equity premium for India =11.72% 5% = 6.72%

Emerging versus Developed Markets: Implied Equity Risk Premiums

$$PBV = \frac{(Return \ on \ equity - Expected \ growth \ rate)}{(Cost \ of \ equity - Expected \ growth \ rate)}$$

Cost of Equity =
$$\frac{(ROE - Expected growth rate)}{PBV} + Expected growth rate$$

						Growth	Growth	Cost of	Cost of	
	PBV	PBV	ROE	ROE	US T.Bond	Rate	Rate	Equity	Equity	Differential
Start of year	Developed	Emerging	Developed	Emerging	rate	Developed	Emerging	(Developed)	(Emerging)	ERP
2004	2.00	1.19	10.81%	11.65%	4.25%	3.75%	5.25%	7.28%	10.63%	3.35%
2005	2.09	1.27	11.12%	11.93%	4.22%	3.72%	5.22%	7.26%	10.50%	3.24%
2006	2.03	1.44	11.32%	12.18%	4.39%	3.89%	5.39%	7.55%	10.11%	2.56%
2007	1.67	1.67	10.87%	12.88%	4.70%	4.20%	5.70%	8.19%	10.00%	1.81%
2008	0.87	0.83	9.42%	11.12%	4.02%	3.52%	5.02%	10.30%	12.37%	2.07%
2009	1.20	1.34	8.48%	11.02%	2.21%	1.71%	3.21%	7.35%	9.04%	1.69%
2010	1.39	1.43	9.14%	11.22%	3.84%	3.34%	4.84%	7.51%	9.30%	1.79%
2011	1.12	1.08	9.21%	10.04%	3.29%	2.79%	4.29%	8.52%	9.61%	1.09%
2012	1.17	1.18	9.10%	9.33%	1.88%	1.38%	2.88%	7.98%	8.35%	0.37%
2013	1.56	1.63	8.67%	10.48%	1.76%	1.26%	2.76%	6.02%	7.50%	1.48%
2014	1.95	1.50	9.27%	9.64%	3.04%	2.54%	4.04%	6.00%	7.77%	1.77%
2015	1.88	1.56	9.69%	9.75%	2.17%	1.67%	3.17%	5.94%	7.39%	1.45%
2016	1.89	1.59	9.24%	10.16%	2.27%	1.77%	3.27%	5.72%	7.60%	1.88%

VI. The Downside of Globalization: Dealing with Country Risk

The Default Spread: Most practitioners estimate the equity risk premium for riskier markets by starting with a base premium for a mature market and adding the default spread for the government in the risky market.

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ERP for country = ERP for Mature Market + Default spread for country

ERP for Indonesia = ERP for US + Default Spread for Indonesia

= 6\% + 2.44\% = 8.44\%
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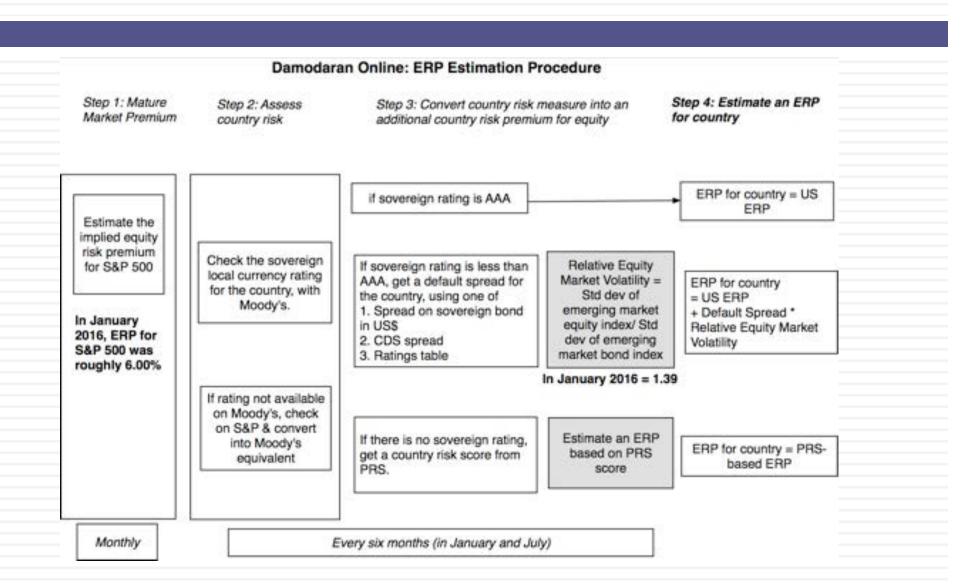
The Melded Default Spread: Equities are riskier than bonds and scaling up the default spread for the higher risk in equities should yield a better estimate of the additional risk for a country:

ERP for country = ERP for Mature Market + Default spread for country *(Std Deviation of Equity_{Country}/ Std Deviation of Govt Bond_{Country})

```
ERP for Indonesia = 6\% + 2.44\% (15.91\%/13.27\%) = 8.93\%
```

(Std Deviation in Indonesian Equities = 15.91%; Indonesian Govt Bond = 13.27%)

A Template for Estimating the ERP



Andorra	9.28%	3.28%	Jersey (States of)	6.59%	0.59%
Austria	6.00%	0.00%	Liechtenstein	6.00%	0.00%
Belgium	6.90%	0.90%	Luxembourg	6.00%	0.00%
Cyprus	12.71%	6.71%	Malta	7.79%	1.79%
Denmark	6.00%	0.00%	Netherlands	6.00%	0.00%
Finland	6.00%	0.00%	Norway	6.00%	0.00%
France	6.74%	0.74%	Portugal	9.72%	3.72%
Germany	6.00%	0.00%	Spain	8.84%	2.84%
Greece	20.90%	14.90%	Sweden	6.00%	0.00%
Guernsey	6.59%	0.59%	Switzerland	6.00%	0.00%
Iceland	8.84%	2.84%	Turkey	9.28%	3.28%
Ireland	8.38%	2.38%	United Kingdom	6.59%	0.59%
Isle of Man	6.59%	0.59%	Western Europe	7.16%	1.16%
Italy	8.84%	2.84%			

North America	6.00%	0.00%
US	6.00%	0.00%
Canada	6.00%	0.00%

Caribbean	14.61	.%	8.619	6	
Argentina	17	.17%	11	.17%	
Belize	19	.42%	13	.42%	
Bolivia	11	37%	5	.37%	
Brazil	9.	28%	3	.28%	
Chile	6.	90%	0	.90%	
Colombia	8	.84%	2	.84%	
Costa Rica	9	.72%	3	.72%	
Ecuador	15	.70%	9	.70%	
El Salvador	11	37%	5	.37%	
Guatemala	9	.72%	3	.72%	
Honduras	15	.70%	9	.70%	
Mexico	7	.79%	1	.79%	
Nicaragua	14	.20%	8	.20%	
Panama	8	.84%	2	.84%	
Paraguay	9	.72%	3	.72%	
Peru	7	.79%	1	.79%	
Suriname	11	37%	5	.37%	
Uruguay	8	.84%	2	.84%	
Venezuela	20).90%	14	1.90%	
Latin America	10	.42%	4	.42%	

10	68	
Country	ERP	CRP
Angola	10.48%	4.48%
Botswana	7.26%	1.26%
Burkina Faso	15.70%	9.70%
Cameroon	14.20%	8.20%
Cape Verde	14.20%	8.20%
Congo (DR	15.70%	9.70%
Congo (Republic)	11.37%	5.37%
Côte d'Ivoire	11.37%	5.37%
Egypt	15.70%	9.70%
Ethiopia	12.71%	6.71%
Gabon	11.37%	5.37%
Ghana	15.70%	9.70%
Kenya	12.71%	6.71%
Morocco	9.72%	3.72%
Mozambique	14.20%	8.20%
Namibia	9.28%	3.28%
Nigeria	11.37%	5.37%
Rwanda	12.71%	6.71%
Senegal	12.71%	6.71%
South Africa	8.84%	2.84%
Tunisia	11.37%	5.37%
Uganda	12.71%	6.71%
Zambia	14.20%	8.20%
Africa	11.76%	5.76%

-	The second second	3.00,0	3.00,0	ı
	Eastern Europe & Russia	9.65%	3.65%	
	Ukraine	20.90%	14.90%	
	Slovenia	9.28%	3.28%	
	Slovakia	7.26%	1.26%	1
	Serbia	12.71%	6.71%	
	Russia	9.72%	3.72%	
4	Romania	9.28%	3.28%	
	Poland	7.26%	1.26%	
)	Montenegro	11.37%	5.37%	
F	Moldova	15.70%	9.70%	
ì	Macedonia	11.37%	5.37%	
	Lithuania	7.79%	1.79%	
	Latvia	7.79%	1.79%	
	Kazakhstan	8.84%	2.84%	
	Hungary	9.72%	3.72%	
	Georgia	11.37%	5.37%	ď.
	Estonia	7.05%	1.05%	
	Czech Republic	7.05%	1.05%	L
	Croatia	9.72%	3.72%	8
	Bulgaria	8.84%	2.84%	
	Bosnia	15.70%	9.70%	
	Belarus	17.17%	11.17%	
	Azerbaijan	9.28%	3.28%	
	Armenia	11.37%	5.37%	

12.71% 6.71%

Albania

Abu Dhabi	6.74%	0.74%
Bahrain	9.28%	3.28%
Israel	7.05%	1.05%
Jordan	12.71%	6.71%
Kuwait	6.74%	0.74%
Lebanon	14.20%	8.20%
Oman	7.05%	1.05%
Qatar	6.74%	0.74%
Ras Al Khaimah	7.26%	1.26%
Saudi Arabia	6.90%	0.90%
Sharjah	7.79%	1.79%
United Arab Emirates	6.74%	0.74%
Middle East	7.11%	1.11%

Black #: Total ERP
Red #: Country risk premium
AVG: GDP weighted average

	Frontier Markets (not rated)							
Algeria	63.0	12.71%	6.71%	Malawi	57.0	17.17%	11.17%	
Brunei	72.8	8.84%	2.84%	Mali	62.5	12.71%	6.71%	
Gambia	62.0	14.20%	8.20%	Myanmar	63.3	12.71%	6.71%	
Guinea	53.8	17.17%	11.17%	Niger	51.0	17.17%	11.17%	
Guinea-Bissau	62.3	12.71%	6.71%	Sierra Leone	56.5	17.17%	11.17%	
Guyana	63.5	12.71%	6.71%	Somalia	42.5	20.90%	14.90%	
Haiti	57.0	17.17%	11.17%	Sudan	48.3	20.90%	14.90%	
Iran	67.8	10.48%	4.48%	Syria	35.8	25.00%	19.00%	
Iraq	56.0	17.17%	11.17%	Tanzania	63.0	12.71%	6.71%	
Korea, D.P.R.	56.0	17.17%	11.17%	Togo	63.8	12.71%	6.71%	
Liberia	50.5	17.17%	11.17%	Yemen, Republic	50.3	17.17%	11.17%	
Libya	52.8	17.17%	11.17%	Zimbabwe	54.5	17.17%	11.17%	
Madagascar	61.3	14.20%	8.20%					

11.37%	5.37%
14.20%	8.20%
6.90%	0.90%
12.719	6.71%
6.59%	0.59%
9.28%	3.28%
9.28%	3.28%
7.05%	1.05%
6.74%	0.74%
6.74%	0.74%
7.79%	1.79%
8.38%	2.38%
14.209	6 8.20%
15.709	6 9.70%
12.719	6.71%
8.84%	2.84%
6.00%	0.00%
12.719	6.71%
6.90%	0.90%
8.38%	2.38%
12.719	6.71%
7.49%	1.49%
6.00%	0.00%
	14.20% 6.90% 12.719 6.59% 9.28% 9.28% 7.05% 6.74% 6.74% 14.209 15.709 12.719 8.84% 6.00% 12.719 8.38% 14.2719 7.49%

12.71%

6.00%

6.00% 0.00%

0.00%

Cook Islands New Zealand

Australia & NZ

VII. And it is not just emerging market companies that are exposed to this risk...

- The "default" approach in valuation has been to assign country risk based upon your country of incorporation. Thus, if you are incorporated in a developed market, the assumption has been that you are not exposed to emerging market risks. If you are incorporated in an emerging market, you are saddled with the entire country risk.
- As companies globalize and look for revenues in foreign markets, this practice will under estimate the costs of equity of developed market companies with significant emerging market risk exposure and over estimate the costs of equity of emerging market companies with significant developed market risk exposure.

One way of dealing with this: Operation-based ERP for Henkel

Region	Revenues in LTM	Weight	ERP
Africa	€ 600	3.34%	11.76%
Asia	€ 3,134	17.45%	7.49%
Central and South America	€ 1,110	6.18%	10.42%
Eastern Europe & Russia	€ 2,695	15.00%	9.65%
Middle East	€ 729	4.06%	7.11%
North America	€ 3,648	20.31%	6.00%
Western Europe	€ 6,045	33.66%	7.16%
Henkel	€ 17,961	100.00%	7.71%

An alternate way: Estimating a company's exposure to country risk (Lambda)

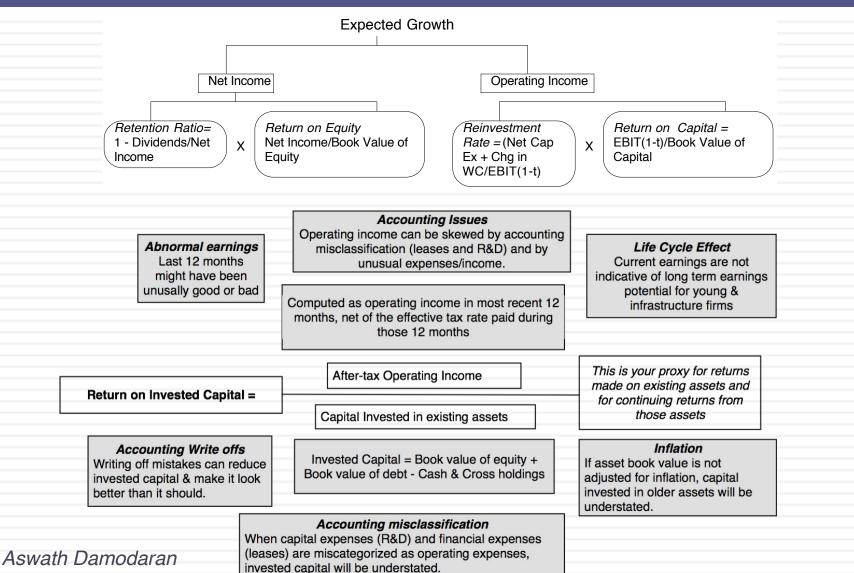
- Just as beta measures exposure to macro economic risk, lambda measures exposure just to country risk. Like beta, it is scaled around one.
- The easiest and most accessible data is on revenues. Most companies break their revenues down by region. One simplistic solution would be to do the following:

Lambda = % of revenues domestically firm/ % of revenues domestically average firm

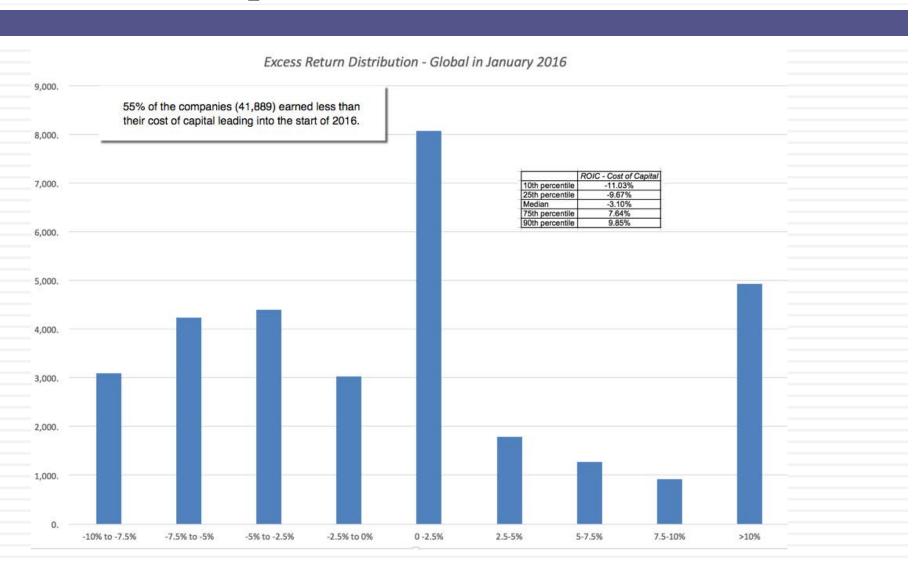
- In 2008-09, Tata Motors got about 91.37% of its revenues in India and TCS got 7.62%. The average Indian firm gets about 80% of its revenues in India:
 - Lambda _{Tata Motors} = 91%/80% = 1.14
 - The danger of focusing just on revenues is that it misses other exposures to risk (production and operations).

	Tata Motors	TCS
% of production/operations in India	High	High
% of revenues in India	91.37% (in 2009) Estimated 70% (in 2010)	7.62%
Lambda	0.80	0.20
Flexibility in moving operations	Low. Significant physical assets.	High. Human capital is mobile.

VIII. Growth has to be earned (not endowed or estimated): Sustainable Growth



Sounds simple, right? But companies seem to have trouble in practice



A More General Way to Estimate Growth: Top Down Growth

- All of the fundamental growth equations assume that the firm has a return on equity or return on capital it can sustain in the long term.
- When operating income is negative or margins are expected to change over time, we use a three step process to estimate growth:
 - Estimate growth rates in revenues over time
 - Determine the total market (given your business model) and estimate the market share that you think your company will earn.
 - Decrease the growth rate as the firm becomes larger
 - Keep track of absolute revenues to make sure that the growth is feasible
 - Estimate expected operating margins each year
 - Set a target margin that the firm will move towards
 - Adjust the current margin towards the target margin
 - Estimate the capital that needs to be invested to generate revenue growth and expected margins
 - Estimate a sales to capital ratio that you will use to generate reinvestment needs each year.

IX. All good things come to an end..And the terminal value is not an ATM...

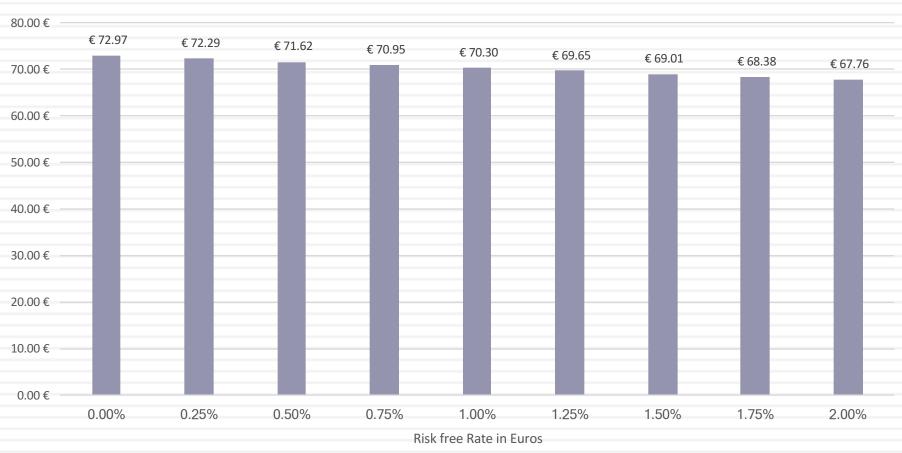
Are you reinvesting enough to sustain your This tax rate locks in stable growth rate? forever. Does it make Reinv Rate = g/ROC sense to use an Is the ROC that of a stable company? effective tax rate? EBIT_{n+1} (1 - tax rate) (1 - Reinvestment Rate)▲ Terminal Value_n = Cost of capital - Expected growth rate This growth rate should be This is a mature company. less than the nominal It's cost of capital should growth rate of the economy reflect that.

Terminal Value and Growth

Stable Growth Rate	Amgen	Tata Motors	Henkel
0%	\$150,652	₹ 435,686	€33,214
1%	\$154,479	₹ 435,686	€33,214
2%	\$160,194	₹ 435,686	
3%	\$167,784	₹ 435,686	
4%	\$179,099	₹ 435,686	
5%		₹ 435,686	
Risk free Rate	4.78%	5.00%	0.10%
Cost of capital	8.08%	10.39%	7.00%
Return on capital	10.00%	10.39%	7.00%

Just an aside: Don't blame the risk free rate



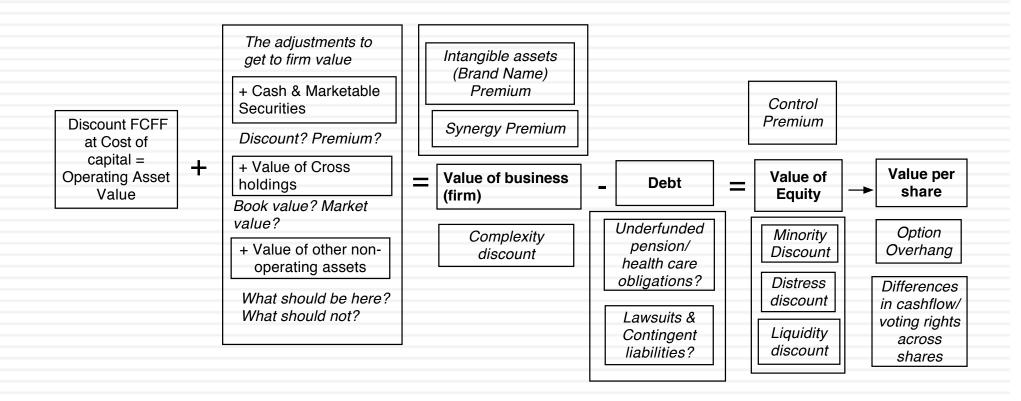


Aswath Damodaran

THE LOOSE ENDS IN VALUATION...

Aswath Damodaran

Getting from DCF to value per share: The Loose Ends



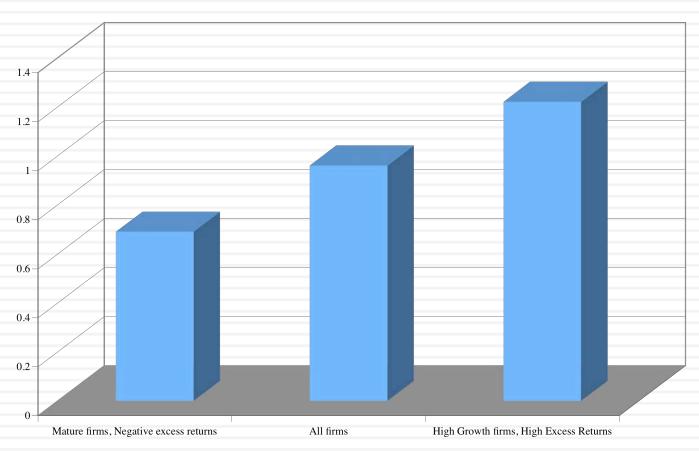
1. The Value of Cash An Exercise in Cash Valuation

	Company A	Company B	Company C
Enterprise Value	\$ 1 billion	\$ 1 billion	\$ 1 billion
Cash	\$ 100 mil	\$ 100 mil	\$ 100 mil
Return on Capital	10%	5%	22%
Cost of Capital	10%	10%	12%
Trades in	US	US	Argentina

In which of these companies is cash most likely to trade at face value, at a discount and at a premium?

Cash: Discount or Premium?

Market Value of \$ 1 in cash: Estimates obtained by regressing Enterprise Value against Cash Balances



2. Dealing with Holdings in Other firms

- Holdings in other firms can be categorized into
 - Minority passive holdings, in which case only the dividend from the holdings is shown in the balance sheet
 - Minority active holdings, in which case the share of equity income is shown in the income statements
 - Majority active holdings, in which case the financial statements are consolidated.
- We tend to be sloppy in practice in dealing with cross holdings. After valuing the operating assets of a firm, using consolidated statements, it is common to add on the balance sheet value of minority holdings (which are in book value terms) and subtract out the minority interests (again in book value terms), representing the portion of the consolidated company that does not belong to the parent company.

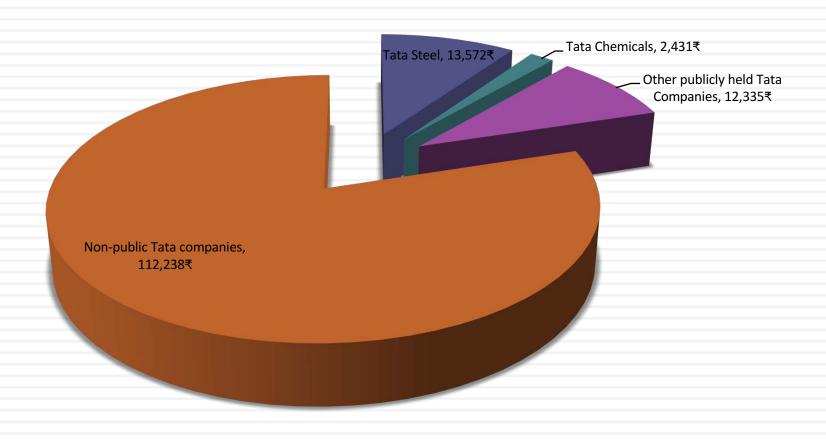
How to value holdings in other firms.. In a perfect world..

- In a perfect world, we would strip the parent company from its subsidiaries and value each one separately. The value of the combined firm will be
 - Value of parent company + Proportion of value of each subsidiary
- To do this right, you will need to be provided detailed information on each subsidiary to estimate cash flows and discount rates.

Two compromise solutions...

- The market value solution: When the subsidiaries are publicly traded, you could use their traded market capitalizations to estimate the values of the cross holdings. You do risk carrying into your valuation any mistakes that the market may be making in valuation.
- The relative value solution: When there are too many cross holdings to value separately or when there is insufficient information provided on cross holdings, you can convert the book values of holdings that you have on the balance sheet (for both minority holdings and minority interests in majority holdings) by using the average price to book value ratio of the sector in which the subsidiaries operate.

Tata Motor's Cross Holdings



3. Other Assets that have not been counted yet..

- Unutilized assets: If you have assets or property that are not being utilized (vacant land, for example), you have not valued it yet. You can assess a market value for these assets and add them on to the value of the firm.
- Overfunded pension plans: If you have a defined benefit plan and your assets exceed your expected liabilities, you could consider the over funding with two caveats:
 - Collective bargaining agreements may prevent you from laying claim to these excess assets.
 - There are tax consequences. Often, withdrawals from pension plans get taxed at much higher rates.
- Do not double count an asset. If you count the income from an asset in your cash flows, you cannot count the market value of the asset in your value.



The longtime home of Playboy magazine founder Hugh Hefner is to be sold to Daren Metropoulos, a principal at private-equity firm Metropoulos & Co. PHOTO: GETTY IMAGES

4. A Discount for Complexity: An Experiment

	Company A	Company B
Operating Income	\$ 1 billion	\$ 1 billion
Tax rate	40%	40%
ROIC	10%	10%
Expected Growth	5%	5%
Cost of capital	8%	8%
Business Mix	Single	Multiple Businesses
Holdings	Simple	Complex
Accounting	Transparent	Opaque
Which firm would	d you value m	ore highly?

Measuring Complexity: Volume of Data in Financial Statements

Company	Number of pages in last 10Q	Number of pages in last 10K
General Electric	65	410
Microsoft	63	218
Wal-mart	38	244
Exxon Mobil	86	332
Pfizer	171	460
Citigroup	252	1026
Intel	69	215
AIG	164	720
Johnson & Johnson	63	218
IBM	85	353

Measuring Complexity: A Complexity Score

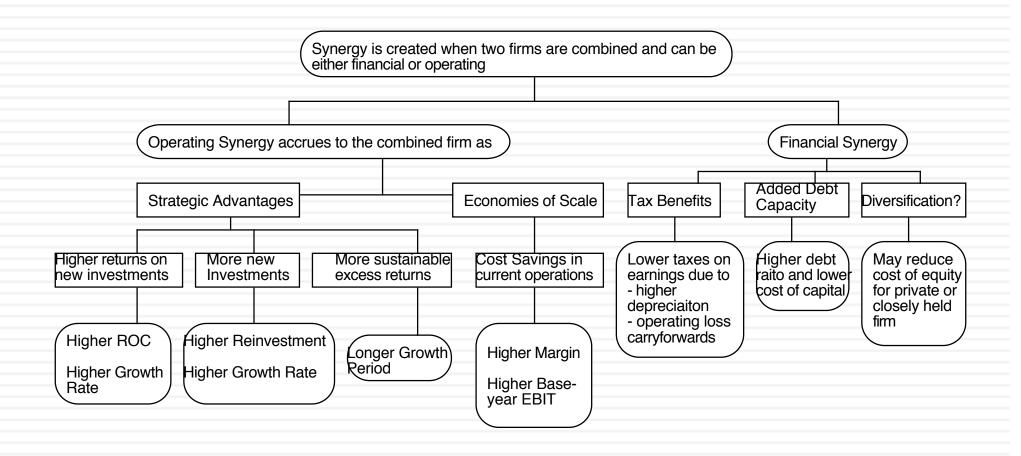
tem	Factors	Follow-up Question	Answer	Weighting factor	Gerdau Score	GE Score
Operating Income	1. Multiple Businesses	Number of businesses (with more than 10% of				
		revenues) =	1	2.00	2	30
		Percent of operating income =	10%	10.00	1	0.8
	3. Income from unspecified sources	Percent of operating income =	0%	10.00	0	1.2
	4. Items in income statement that are volatile	Percent of operating income =	15%	5.00	0.75	1
ax Rate	1. Income from multiple locales	Percent of revenues from non-domestic locales =	70%	3.00	2.1	1.8
	2. Different tax and reporting books	Yes or No	No	Yes=3	0	3
	3. Headquarters in tax havens	Yes or No	No	Yes=3	0	0
	4. Volatile effective tax rate	Yes or No	Yes	Yes=2	2	0
Capital Expenditures	1. Volatile capital expenditures	Yes or No	Yes	Yes=2	2	2
	2. Frequent and large acquisitions	Yes or No	Yes	Yes=4	4	4
	3. Stock payment for acquisitions and					
		Yes or No	No	Yes=4	0	4
Vorking capital	Unspecified current assets and current					
	liabilities	Yes or No	No	Yes=3	0	0
	2. Volatile working capital items	Yes or No	Yes	Yes=2	2	2
Expected Growth rate	1. Off-balance sheet assets and liabilities					
	(operating leases and R&D)	Yes or No	No	Yes=3	0	3
	Substantial stock buybacks	Yes or No	No	Yes=3	0	3
	3. Changing return on capital over time	Is your return on capital volatile?	Yes	Yes=5	5	5
	4. Unsustainably high return	Is your firm's ROC much higher than industry average?	No	Yes=5	0	0
Cost of capital	1. Multiple businesses	Number of businesses (more than 10% of revenues) =	1	1.00	1	20
	2. Operations in emerging markets	Percent of revenues=	50%	5.00	2.5	2.5
	3. Is the debt market traded?	Yes or No	No	No=2	2	0
	4. Does the company have a rating?	Yes or No	Yes	No=2	0	0
	5. Does the company have off-balance sheet				-	-
	debt?	Yes or No	No	Yes=5	0	5
lo-operating assets	Minority holdings as percent of book assets	Minority holdings as percent of book assets	0%	20.00	0	0.8
irm to Equity value	Consolidation of subsidiaries	Minority interest as percent of book value of equity	63%	20.00	12.6	1.2
er share value Dan	Shares with different voting rights	Does the firm have shares with different voting rights?	Yes	Yes = 10	10	0
nowalli Dall	Shares with different voting rights LOCATOR Equity options outstanding	Options outstanding as percent of shares	0%	10.00	0	0.26.
		Complexity Score =			48.95	90.55

Dealing with Complexity

- In Discounted Cashflow Valuation
 - The Aggressive Analyst: Trust the firm to tell the truth and value the firm based upon the firm's statements about their value.
 - The Conservative Analyst: Don't value what you cannot see.
 - The Compromise: Adjust the value for complexity
 - Adjust cash flows for complexity
 - Adjust the discount rate for complexity
 - Adjust the expected growth rate/length of growth period
 - Value the firm and then discount value for complexity
- In relative valuation
 - In a relative valuation, you may be able to assess the price that the market is charging for complexity:
 - With the hundred largest market cap firms, for instance:

PBV = 0.65 + 15.31 ROE - 0.55 Beta + 3.04 Expected growth rate - 0.003 # Pages in 10K

5. The Value of Synergy



Valuing Synergy

- (1) the firms involved in the merger are valued independently, by discounting expected cash flows to each firm at the weighted average cost of capital for that firm.
- (2) the value of the combined firm, with no synergy, is obtained by adding the values obtained for each firm in the first step.
- (3) The effects of synergy are built into expected growth rates and cashflows, and the combined firm is re-valued with synergy.

Value of Synergy = Value of the combined firm, with synergy - Value of the combined firm, without synergy

Inbev + SAB Miller: Where's the synergy?

	Inbev	SABMiller	Combined firm (status quo)	Combined firm (synergy)
Levered Beta	0.85	0.8289	0.84641	0.84641
Pre-tax cost of debt	3.0000%	3.2000%	3.00%	3.00%
Effective tax rate	18.00%	26.36%	19.92%	19.92%
Debt to Equity Ratio	30.51%	23.18%	29.71%	29.71%
Revenues	\$45,762.00	\$22,130.00	\$67,892.00	\$67,892.00
Operating Margin	32.28%	19.97%	28.27%	30.00%
Operating Income (EBIT)	\$14,771.97	\$4,419.36	\$19,191.33	\$20.368
After-tax return on capital	12.10%	12.64%	11.68%	12.00%
Reinvestment Rate =	50.99%	33.29%	43.58%	50.00%
Expected Growth Rate	6.17%	4.21%	5.09%	6.00%

The value of synergy

			Combined	
			firm (status	Combined firm
	Inbev	SABMiller	quo)	(synergy)
Cost of Equity =	8.93%	9.37%	9.12%	9.12%
After-tax cost of debt =	2.10%	2.24%	2.10%	2.10%
Cost of capital =	7.33%	8.03%	7.51%	7.51%
After-tax return on capital =	12.10%	12.64%	11.68%	12.00%
Reinvestment Rate =	50.99%	33.29%	43.58%	50.00%
Expected growth rate=	6.17%	4.21%	5.09%	6.00%
	1/1/	C. C'		
	Value o	t firm	I	
PV of FCFF in high growth =	\$28,733	\$9,806	\$38,539	\$39,151
Terminal value =	\$260,982	\$58,736	\$319,717	\$340,175
Value of operating assets =	\$211,953	\$50,065	\$262,018	\$276,610

Value of synergy = 276,610 - 262,018 = 14,592 million ₆₈

6. Brand name, great management, superb product ...Are we short changing intangibles?

- There is often a temptation to add on premiums for intangibles. Here are a few examples.
 - Brand name
 - Great management
 - Loyal workforce
 - Technological prowess
- There are two potential dangers:
 - For some assets, the value may already be in your value and adding a premium will be double counting.
 - For other assets, the value may be ignored but incorporating it will not be easy.

Valuing Brand Name

	Coca Cola	With Cott Margins
Current Revenues =	\$21,962.00	\$21,962.00
Length of high-growth period	10	10
Reinvestment Rate =	50%	50%
Operating Margin (after-tax)	15.57%	5.28%
Sales/Capital (Turnover ratio)	1.34	1.34
Return on capital (after-tax)	20.84%	7.06%
Growth rate during period (g) =	10.42%	3.53%
Cost of Capital during period =	7.65%	7.65%
Stable Growth Period		
Growth rate in steady state =	4.00%	4.00%
Return on capital =	7.65%	7.65%
Reinvestment Rate =	52.28%	52.28%
Cost of Capital =	7.65%	7.65%
Value of Firm =	\$79,611.25	\$15,371.24

Valuing a Franchise: Star Wars

		Add-on \$ per Box Office \$	tar Wars Fra	anchise Valu	uation: Dec	cen	nber 20	15			
Stream	ing/Video	\$1.20									
Toys &	Merchandise	\$2.00									
Books/	eBooks	\$0.20		Main Movies			9	nin O	off Movie	26	
Gaming	3	\$0.50	Main Movies Spin Off Movies World Box office of \$1.5 billion, World Box office is 509			of					
Other		\$0.50		sted for 2% infl			1	nain	movies		
	Add on \$		Mai	n Star Wars Mo	vies	1	Sto	ır Wa	rs Spin o	offs	
	per box office \$		Star Wars VII	Star Wars VIII	Star Wars IX	Ro	gue One	Hans	s Solo?	Bob	a Fett?
	Office \$	Years from now	0.0	2.0	4.0		1.0	3.0 \$1,061		5.0 \$1,104	
		Movies - Revenues	\$2,000	\$2,081	\$2,165		\$1,020				
		Streaming/Video - Revenues	\$2,400	\$2,497	\$2,598		\$1,224	\$:	1,273	\$	1,325
		Toys & Merchandise - Revenues	\$4,000	\$4,162	\$4,330		\$2,040	\$2	2,122	\$	2,208
	-	Books/eBooks - Revenues	\$400	\$416	\$433		\$204	5	212		\$221
		Gaming - Revenues	\$1,000	\$1,040	\$1,082		\$510	5	531		\$552
		Other - Revenues	\$1,000	\$1,040	\$1,082		\$510	5	531		\$552
Opera	ting Margin	Total - Revenues	\$10,800	\$11,236	\$11,690		\$5,508	\$5	5,731	\$	5,962
-	for movies										
- ,	non-movies	After-tax Operating Income (movies)	\$ 282	\$ 293	\$ 305	\$	144	\$	150	\$	156
30%	tax rate	After-tax Operating Income (non-movies)	\$ 924	\$ 961	\$ 1,000	\$	471	\$	490	\$	510
	—	Present Value	\$ 1,206	\$ 1,083	\$ 973	\$	572	\$	514	\$	461
Diag		Value of new Star Wars movies =	\$4,809			H					
1	ounted back 61% cost of	Value of continuing income =	\$5,163	···							
_	apital of	Value of Star Wars =	\$9,972								
ent	ertainment ompanies			continue a	es that revent after 2020, gr th 15% opera	owi	ng at 2%				

7. Be circumspect about defining debt for cost of capital purposes...

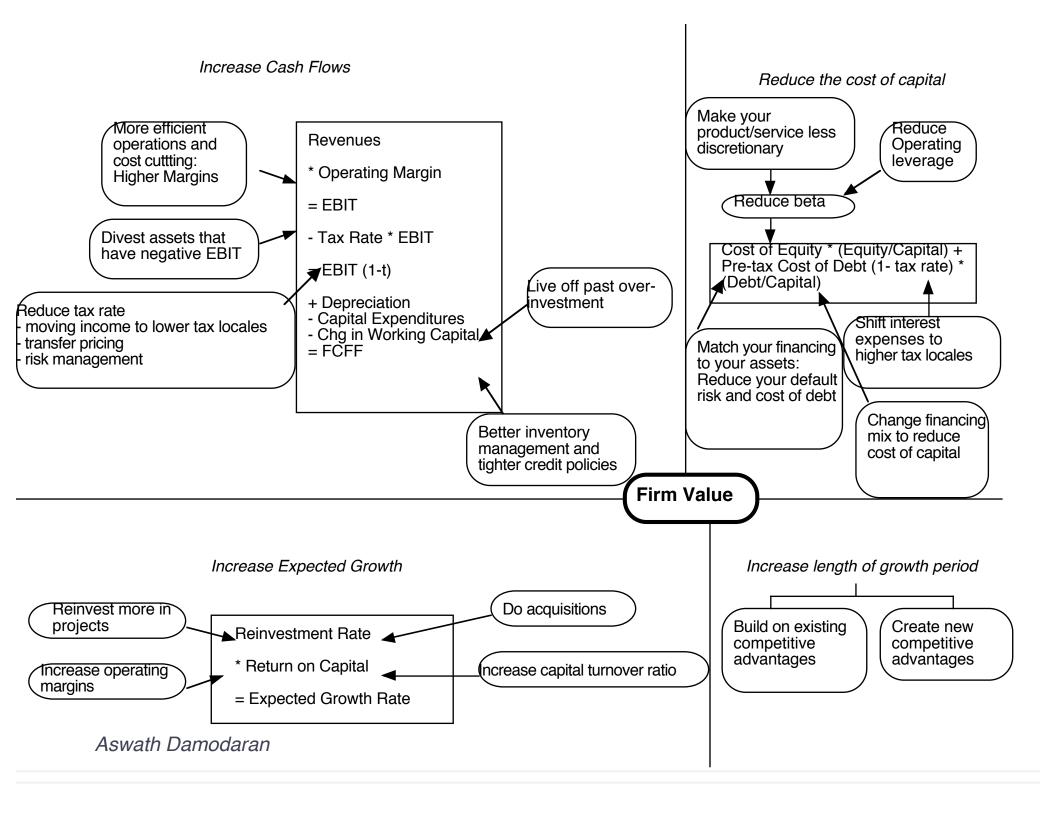
- General Rule: Debt generally has the following characteristics:
 - Commitment to make fixed payments in the future
 - The fixed payments are tax deductible
 - Failure to make the payments can lead to either default or loss of control of the firm to the party to whom payments are due.
- Defined as such, debt should include
 - All interest bearing liabilities, short term as well as long term
 - All leases, operating as well as capital
- Debt should not include
 - Accounts payable or supplier credit

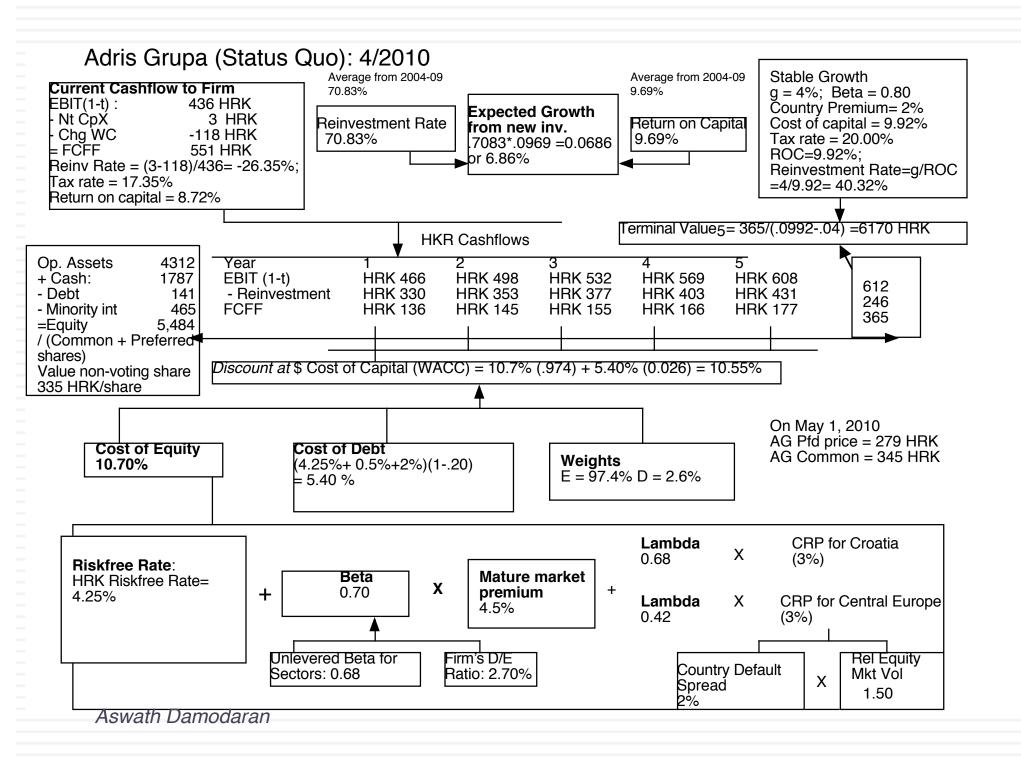
But should consider other potential liabilities when getting to equity value...

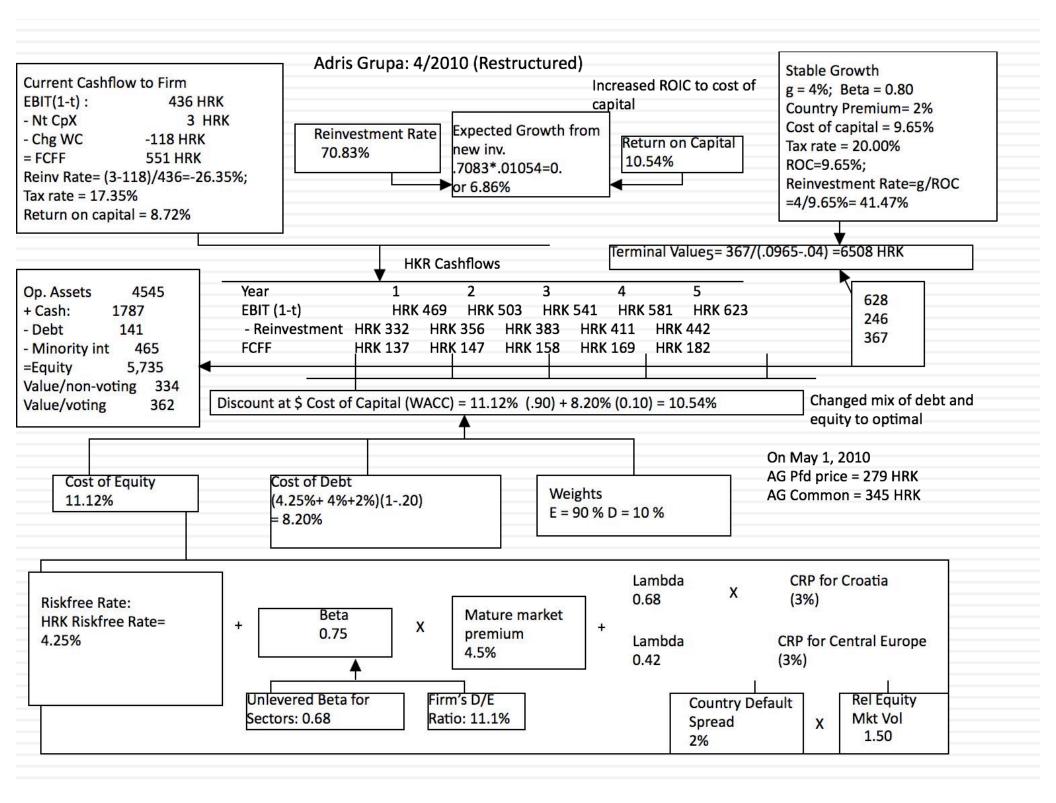
- If you have under funded pension fund or health care plans, you should consider the under funding at this stage in getting to the value of equity.
 - If you do so, you should not double count by also including a cash flow line item reflecting cash you would need to set aside to meet the unfunded obligation.
 - You should not be counting these items as debt in your cost of capital calculations....
- If you have contingent liabilities for example, a potential liability from a lawsuit that has not been decided - you should consider the expected value of these contingent liabilities
 - Value of contingent liability = Probability that the liability will occur * Expected value of liability

8. The Value of Control

- The value of the control premium that will be paid to acquire a block of equity will depend upon two factors -
 - Probability that control of firm will change: This refers to the probability that incumbent management will be replaced. this can be either through acquisition or through existing stockholders exercising their muscle.
 - Value of Gaining Control of the Company: The value of gaining control of a company arises from two sources the increase in value that can be wrought by changes in the way the company is managed and run, and the side benefits and perquisites of being in control
 - <u>Value of Gaining Control</u> = <u>Present Value (Value of Company with change in control Value of company without change in control) + Side Benefits of Control</u>







Value of Control and the Value of Voting Rights

- Adris Grupa has two classes of shares outstanding: 9.616 million voting shares and 6.748 million non-voting shares.
- To value a non-voting share, we assume that all non-voting shares essentially have to settle for status quo value. All shareholders, common and preferred, get an equal share of the status quo value.

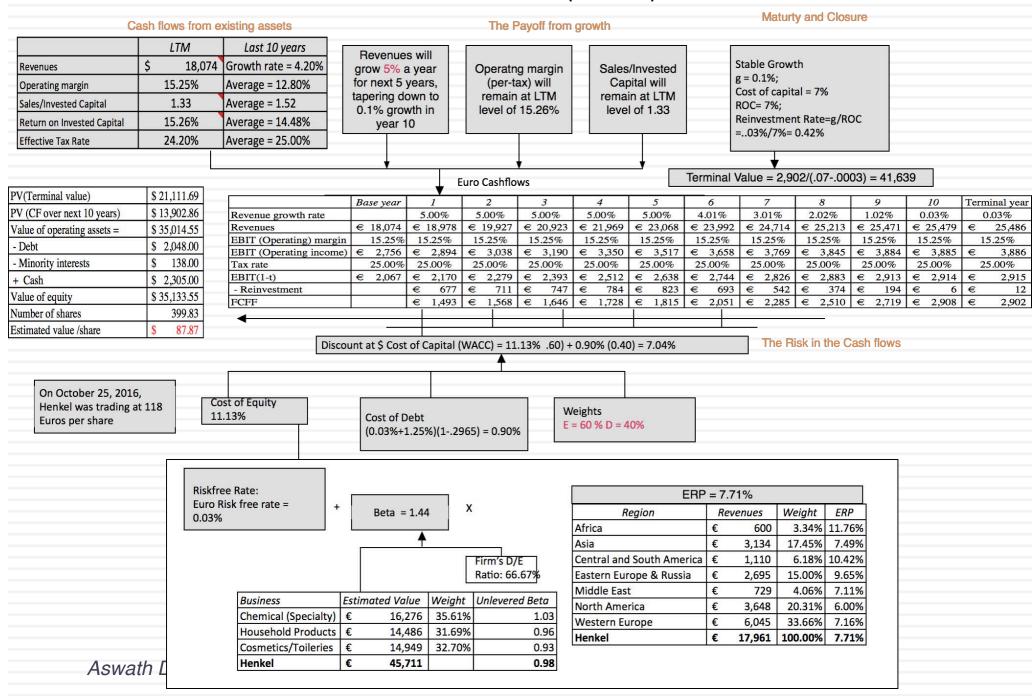
Status Quo Value of Equity = 5,484 million HKR Value for a non-voting share = 5484/(9.616+6.748) = 334 HKR/share

- To value a voting share, we first value control in Adris Grup as the difference between the optimal and the status quo value:
 - Value of control at Adris Grupa = 5,735 5484 = 249 million HKR
- □ If you assume a 100% probability of change occurring, the value per voting share can be written as:
 - Value per voting share =334 HKR + 249/9.616 = 362 HKR
- ☐ If the probability of control changing is only 40%, the expected value of control and value per voting share can be written as follows:
 - Expected value of control = 249 (.4) = 99.6 million HKR
 - Value per voting share = 334 HKR + 99.6/9.616 = 344 HKR

Henkel: Debt Capacity?

		Cost of	Bond	Interest rate on		Cost of Debt (after-	
Debt Ratio	Beta	Equity	Rating	debt	Tax Rate	tax)	WACC
0%	0.9751	7.55%	Aaa/AAA	0.43%	29.65%	0.30%	7.55%
4.2%	1.0052	7.78%	A2	1.03%	29.65%	0.72%	7.48%
10%	1.0565	8.17%	A2	1.03%	29.65%	0.72%	7.43%
20%	1.1522	8.91%	A2	1.03%	29.65%	0.72%	7.27%
30%	1.2753	9.86%	A3	1.28%	29.65%	0.90%	7.17%
40%	1.4395	11.13%	A3	1.28%	29.65%	0.90%	7.04%
50%	1.6692	12.90%	Ba1	2.78%	29.65%	1.96%	7.43%
60%	2.1966	16.96%	B1	4.03%	29.65%	2.84%	8.49%
70%	2.9288	22.61%	C2	7.03%	21.33%	5.53%	10.65%
80%	4.3932	33.89%	Ca2	8.03%	18.55%	6.54%	12.01%
90%	8.7863	67.75%	Ca3	10.03%	11.48%	8.88%	14.77%

Henkel Restructured: October 2016 (in Euros)



THE DARK SIDE OF VALUATION: VALUING DIFFICULT-TO-VALUE COMPANIES

The fundamental determinants of value...

What are the cashflows from existing assets?

- Equity: Cashflows after debt payments
- Firm: Cashflows before debt payments

What is the **value added** by growth assets? Equity: Growth in equity earnings/ cashflows Firm: Growth in operating earnings/ cashflows

How **risky are the cash flows** from both existing assets and growth assets? Equity: Risk in equity in the company Firm: Risk in the firm's operations

When will the firm become a **mature firm**, and what are the potential roadblocks?

The Dark Side of Valuation...

- Valuing stable, money making companies with consistent and clear accounting statements, a long and stable history and lots of comparable firms is easy to do.
- The true test of your valuation skills is when you have to value "difficult" companies. In particular, the challenges are greatest when valuing:
 - Young companies, early in the life cycle, in young businesses
 - Companies that don't fit the accounting mold
 - Companies that face substantial truncation risk (default or nationalization risk)

Difficult to value companies...

Across the life cycle:

- Young, growth firms: Limited history, small revenues in conjunction with big operating losses and a propensity for failure make these companies tough to value.
- Mature companies in transition: When mature companies change or are forced to change, history may have to be abandoned and parameters have to be reestimated.
- Declining and Distressed firms: A long but irrelevant history, declining markets, high debt loads and the likelihood of distress make them troublesome.

Across sectors

- Financial service firms: Opacity of financial statements and difficulties in estimating basic inputs leave us trusting managers to tell us what's going on.
- Commodity and cyclical firms: Dependence of the underlying commodity prices or overall economic growth make these valuations susceptible to macro factors.
- Firms with intangible assets: Accounting principles are left to the wayside on these firms.

Across the ownership cycle

- Privately owned businesses: Exposure to firm specific risk and illiquidity bedevil valuations.
- Venture Capital (VC) and private equity: Different equity investors, with different perceptions of risk.
- Closely held public firms: Part private and part public, sharing the troubles of both.

I. The challenge with young companies...

Figure 5.2: Estimation Issues - Young and Start-up Companies

Making judgments on revenues/ profits difficult becaue you cannot draw on history. If you have no product/ service, it is difficult to gauge market potential or profitability. The company's entire value lies in future growth but you have little to base your estimate on.

Cash flows from existing assets non-existent or negative.

What is the value added by growth assets?

What are the cashflows from existing assets?

Different claims or cash flows can affect value of equity at each stage.

What is the value of equity in the firm?

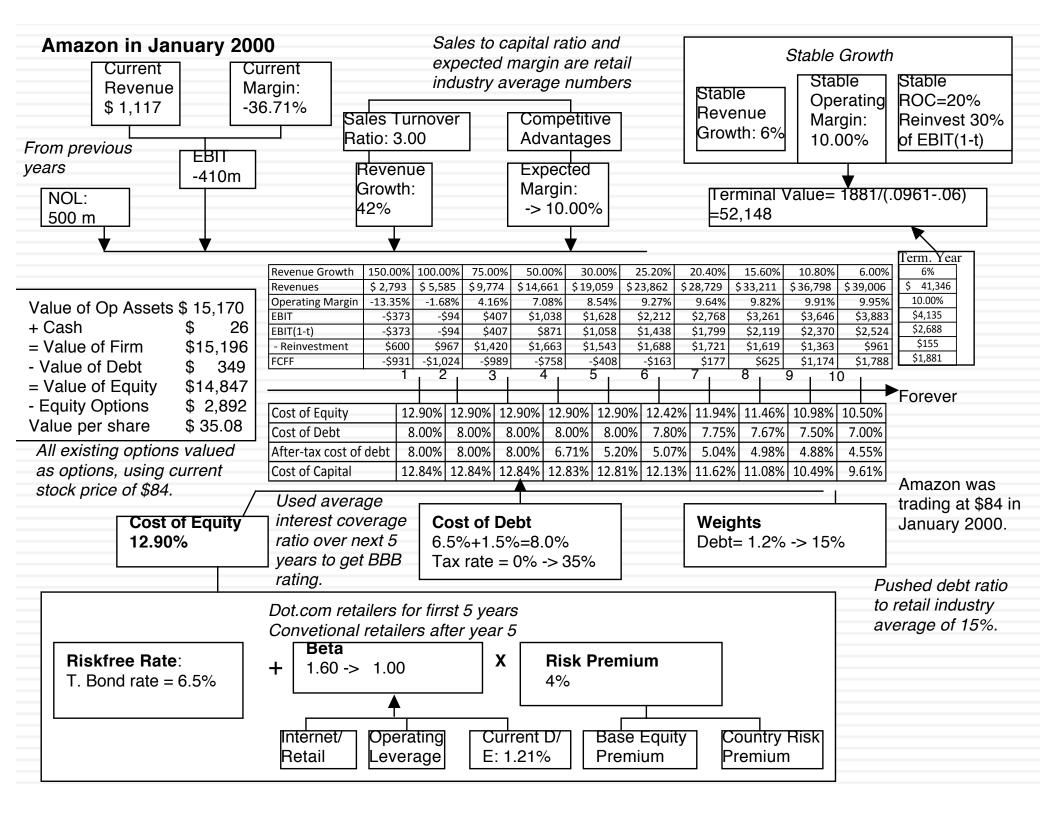
How risky are the cash flows from both existing assets and growth assets?

Limited historical data on earnings, and no market prices for securities makes it difficult to assess risk. When will the firm become a mature fiirm, and what are the potential roadblocks?

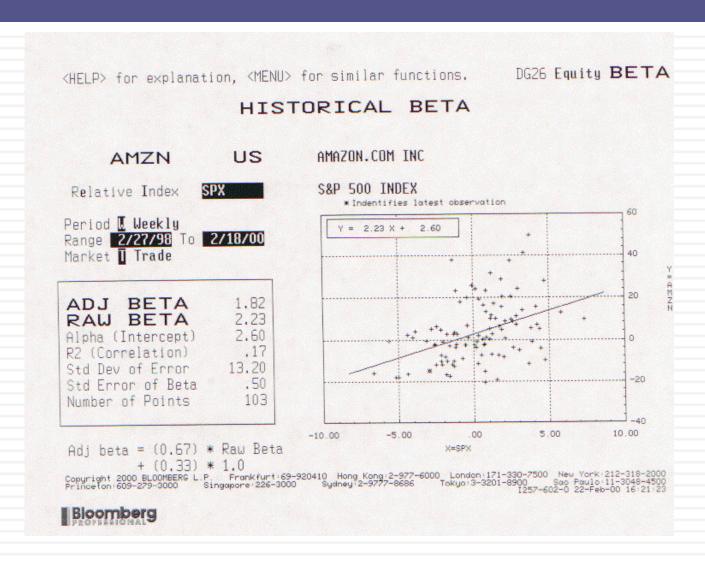
Will the firm make it through the gauntlet of market demand and competition? Even if it does, assessing when it will become mature is difficult because there is so little to go on.

Upping the ante.. Young companies in young businesses...

- □ When valuing a business, we generally draw on three sources of information
 - The firm's current financial statement
 - How much did the firm sell?
 - How much did it earn?
 - The firm's financial history, usually summarized in its financial statements.
 - How fast have the firm's revenues and earnings grown over time?
 - What can we learn about cost structure and profitability from these trends?
 - Susceptibility to macro-economic factors (recessions and cyclical firms)
 - The industry and comparable firm data
 - What happens to firms as they mature? (Margins.. Revenue growth... Reinvestment needs... Risk)
- It is when valuing these companies that you find yourself tempted by the dark side, where
 - "Paradigm shifts" happen...
 - New metrics are invented ...
 - The story dominates and the numbers lag...



Lesson 1: Don't trust regression betas....

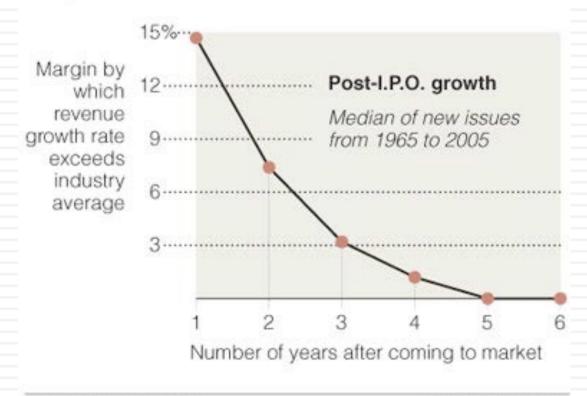


Lesson 2: Work backwards and keep it simple...

Year	Revenue Growth	Sales	Operating Margin	EBIT	EBIT (1-t)
Tr 12 mths		\$1,117	-36.71%	-\$410	-\$410
1	150.00%	\$2,793	-13.35%	-\$373	-\$373
2	100.00%	\$5,585	-1.68%	-\$94	-\$94
3	75.00%	\$9,774	4.16%	\$407	\$407
4	50.00%	\$14,661	7.08%	\$1,038	\$871
5	30.00%	\$19,059	8.54%	\$1,628	\$1,058
6	25.20%	\$23,862	9.27%	\$2,212	\$1,438
7	20.40%	\$28,729	9.64%	\$2,768	\$1,799
8	15.60%	\$33,211	9.82%	\$3,261	\$2,119
9	10.80%	\$36,798	9.91%	\$3,646	\$2,370
10	6.00%	\$39,006	9.95%	\$3,883	\$2,524
TY	6.00%	\$41,346	10.00%	\$4,135	\$2,688

Lesson 3: Scaling up is hard to do...

Typically, the revenue growth rate of a newly public company outpaces its industry average for only about five years.



Source: Andrew Metrick

The New York Times

Lesson 4: Don't forget to pay for growth...

Year	Revenues	Δ Revenue	Sales/Cap	∆ Investment	Invested Capital		Invested Capital EBIT (1-t)	
Tr 12 mths	\$1,117				\$	487	-\$410	
1	\$2,793	\$1,676	3.00	\$559	\$	1,045	-\$373	-76.62%
2	\$5,585	\$2,793	3.00	\$931	\$	1,976	-\$94	-8.96%
3	\$9,774	\$4,189	3.00	\$1,396	\$	3,372	\$407	20.59%
4	\$14,661	\$4,887	3.00	\$1,629	\$	5,001	\$871	25.82%
5	\$19,059	\$4,398	3.00	\$1,466	\$	6,467	\$1,058	21.16%
6	\$23,862	\$4,803	3.00	\$1,601	\$	8,068	\$1,438	22.23%
7	\$28,729	\$4,868	3.00	\$1,623	\$	9,691	\$1,799	22.30%
8	\$33,211	\$4,482	3.00	\$1,494	\$	11,185	\$2,119	21.87%
9	\$36,798	\$3,587	3.00	\$1,196	\$	12,380	\$2,370	21.19%
10	\$39,006	\$2,208	3.00	\$736	\$	13,116	\$2,524	20.39%
TY	\$41,346	\$2,340	NA			Assumed to	be =	20.00%

Lesson 5: There are always scenarios where the market price can be justified...

	_	Target pre-tax Operating Margin									
Φ			6%	8%		10%		12%		14%	
annual vth rate	30%	\$	(1.94)	\$	2.95	\$	7.84	\$	12.71	\$	17.57
X	35%	\$	1.41	\$	8.37	\$	15.33	\$	22.27	\$	29.21
ded anr Growth	40%	\$	6.10	\$	15.93	\$	25.74	\$	35.54	\$	45.34
	45%	\$	12.59	\$	26.34	\$	40.05	\$	53.77	\$	67.48
οοι	50%	\$	21.47	\$	40.50	\$	59.52	\$	78.53	\$	97.54
Compoui	55%	\$	33.47	\$	59.60	\$	85.72	\$	111.84	\$	137.95
Cc	60%	\$	49.53	\$	85.10	\$	120.66	\$	156.22	\$	191.77

Lesson 6: Don't forget to mop up...

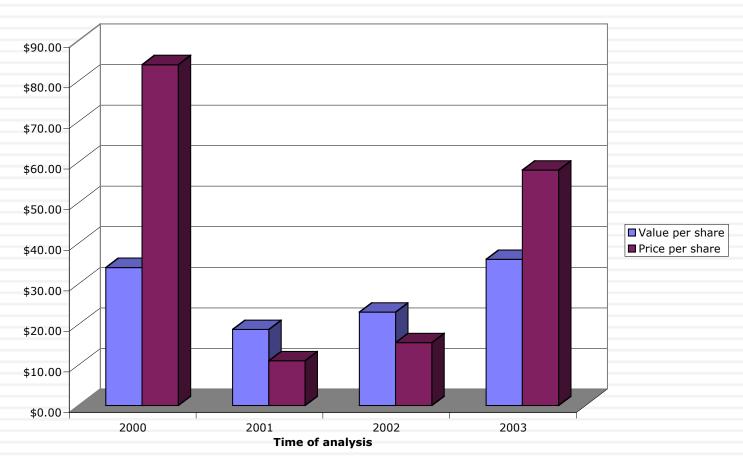
- Watch out for "other" equity claims: If you buy equity in a young, growth company, watch out for other (often hidden) claims on the equity that don't take the form of common shares. In particular, watch for options granted to managers, employees, venture capitalists and others (you will be surprised...).
 - Value these options as options (not at exercise value)
 - Take into consideration expectations of future option grants when computing expected future earnings/cash flows.
- Not all shares are equal: If there are differences in cash flow claims (dividends or liquidation) or voting rights across shares, value these differences.
 - Voting rights matter even at well run companies

Lesson 7: You will be wrong 100% of the time... and it really is not (always) your fault...

- No matter how careful you are in getting your inputs and how well structured your model is, your estimate of value will change both as new information comes out about the company, the business and the economy.
- As information comes out, you will have to adjust and adapt your model to reflect the information. Rather than be defensive about the resulting changes in value, recognize that this is the essence of risk.
- A test: If your valuations are unbiased, you should find yourself increasing estimated values as often as you are decreasing values. In other words, there should be equal doses of good and bad news affecting valuations (at least over time).

And the market is often "more wrong"....





Valuing an IPO

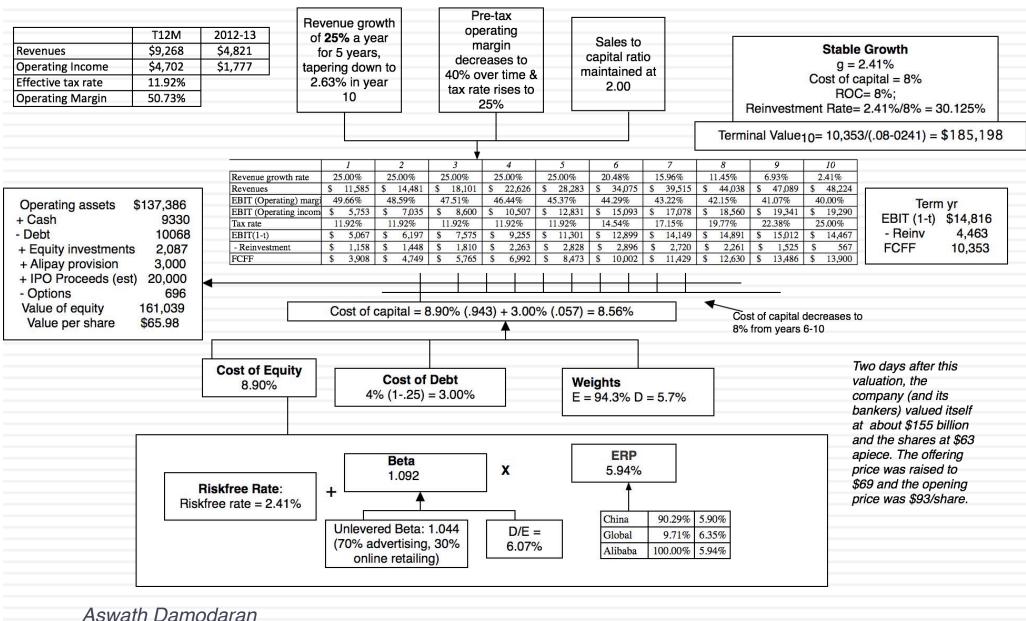
Valuation issues:

- Use of the proceeds from the offering: The proceeds from the offering can be held as cash by the firm to cover future investment needs, paid to existing equity investors who want to cash out or used to pay down debt.
- Warrants/ Special deals with prior equity investors: If venture capitalists and other equity investors from earlier iterations of fund raising have rights to buy or sell their equity at pre-specified prices, it can affect the value per share offered to the public.

Pricing issues:

- Institutional set-up: Most IPOs are backed by investment banking guarantees on the price, which can affect how they are priced.
- Follow-up offerings: The proportion of equity being offered at initial offering and subsequent offering plans can affect pricing.

Alibaba: Pre-IPO valuation - September 2, 2014 (in US \$)



II. Mature Companies in transition...

- Mature companies are generally the easiest group to value. They have long, established histories that can be mined for inputs. They have investment policies that are set and capital structures that are stable, thus making valuation more grounded in past data.
- However, this stability in the numbers can mask real problems at the company. The company may be set in a process, where it invests more or less than it should and does not have the right financing mix. In effect, the policies are consistent, stable and bad.
- If you expect these companies to change or as is more often the case to have change thrust upon them,

The perils of valuing mature companies...

Figure 7.1: Estimation Issues - Mature Companies

Lots of historical data on earnings and cashflows. Key questions remain if these numbers are volatile over time or if the existing assets are not being efficiently utilized.

Growth is usually not very high, but firms may still be generating healthy returns on investments, relative to cost of funding. Questions include how long they can generate these excess returns and with what growth rate in operations. Restructuring can change both inputs dramatically and some firms maintain high growth through acquisitions.

What is the value added by growth assets?

What are the cashflows from existing assets?

> How risky are the cash flows from both existing assets and growth assets?

Equity claims can vary in voting rights and dividends.

What is the value of

the firm can change its financial leverage This can affect both the cost of equtiv and capital.

Operating risk should be stable, but

When will the firm become a mature fiirm, and what are the potential roadblocks?

Maintaining excess returns or high growth for any length of time is difficult to do for a mature firm.

Aswath Damodaran

Hormel Foods: The Value of Control Changing

Hormel Foods sells packaged meat and other food products and has been in existence as a publicly traded company for almost 80 years. In 2008, the firm reported after-tax operating income of \$315 million, reflecting a compounded growth of 5% over the previous 5 years.

The Status Quo

Run by existing management, with conservative reinvestment policies (reinvestment rate = 14.34% and debt ratio = 10.4%.

Anemic growth rate and short growth period, due to reinvestment policy

Low debt ratio affects cost of capital

							>	
Year	Operating income after taxes	Expected growth rate	ROC	Reinvestment Rate	Reinvestment	FCFF	Cost of capital	Present Value
Trailing 12 months	\$315							
1	\$324	2.75%	14.34%	19.14%	\$62	\$262	6.79%	\$245
2	\$333	2.75%	14.34%	19.14%	\$64	\$269	6.79%	\$236
3	\$342	2.75%	14.34%	19.14%	\$65	\$276	6.79%	\$227
Beyond	\$350	2.35%	7.23%	32.52%	\$114	\$4,840	7.23%	\$3,974
Value of operating a	ssets							\$4,682
(Add) Cash								\$155
(Subtract) Debt								\$491
(Subtract) Managen	nent Options							\$53
Value of equity in common stock								\$4,293
Value per share								\$31.91

New and better management

More aggressive reinvestment which increases the reinvestment rate (to 40%) and tlength of growth (to 5 years), and higher debt ratio (20%).

Operating Restructuring (1)

Expected growth rate = ROC* Reinvestment Rate

Expected growth rae (status quo) = 14.34% * 19.14% = 2.75%

Expected growth rate (optimal) = 14.00% * 40% = 5.60%

ROC drops, reinvestment rises and growth goes up.

Financial restructuring 📵

Cost of capital = Cost of equity (1-Debt ratio) + Cost of debt (Debt ratio)

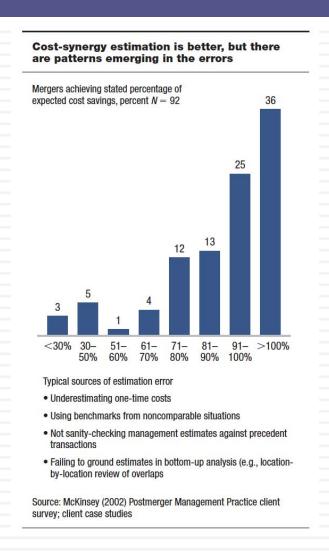
Status quo = 7.33% (1-.104) + 3.60% (1-.40) (.104) = 6.79%

Optimal = 7.75% (1-.20) + 3.60% (1-.40) (.20) = 6.63%

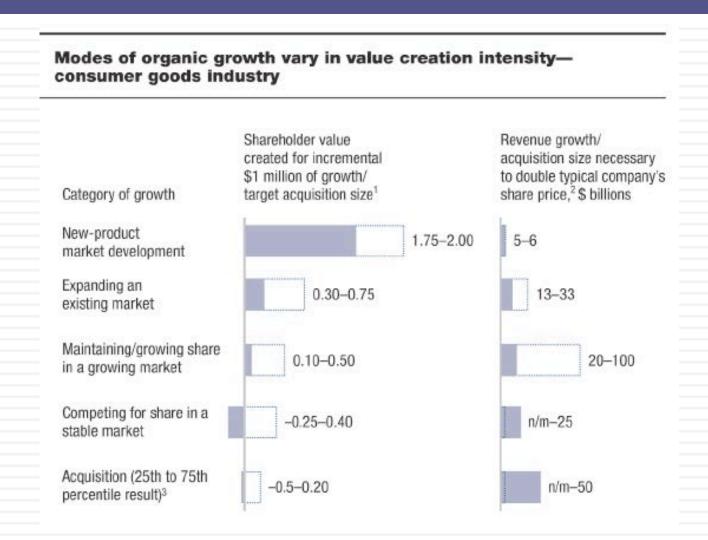
Cost of equity rises but cost of capital drops.

Year	Operating income after taxes	Expected growth rate	ROC	Reinvestment Rate	Reinvestment	FCFF	Cost of capital	Present Value
Trailing 12 months	\$315							
1	\$333	5.60%	14.00%	40.00%	\$133	\$200	6.63%	\$187
2	\$351	5.60%	14.00%	40.00%	\$141	\$211	6.63%	\$185
3	\$371	5.60%	14.00%	40.00%	\$148	\$223	6.63%	\$184
4	\$392	5.60%	14.00%	40.00%	\$260	\$235	6.63%	\$182
5	\$414	5.60%	14.00%	40.00%	\$223	\$248	6.63%	\$180
Beyond	\$423	2.35%	6.74%	34.87%	\$148	\$6,282	6.74%	\$4,557
Value of operating a	ssets							\$5,475
(Add) Cash								\$155
(Subtract) Debt								\$491
(Subtract) Managen	nent Options							\$53
Value of equity in c								\$5,085
Value per Algrivat	n Damodaran							\$37.80

Lesson 1: Cost cutting and increased efficiency are easier accomplished on paper than in practice...

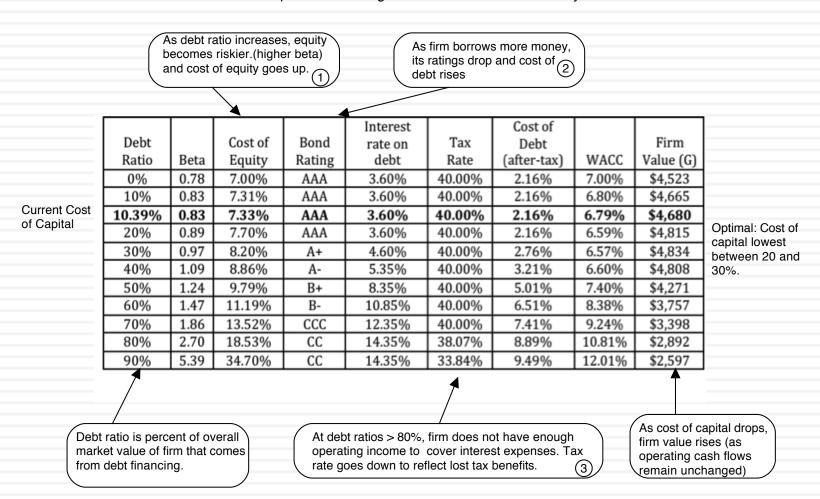


Lesson 2: Increasing growth is not always an option (or at least not a good option)



Lesson 3: Financial leverage is a double-edged sword..

Exhibit 7.1: Optimal Financing Mix: Hormel Foods in January 2009



III. Dealing with decline and distress...

Historial data often reflects flat or declining revenues and falling margins. Investments often earn less than the cost of capital.

Growth can be negative, as firm sheds assets and shrinks. As less profitable assets are shed, the firm's remaining assets may improve in quality.

What is the value added by growth assets?

What are the cashflows from existing assets?

Underfunded pension obligations and litigation claims can lower value of equity. Liquidation preferences can affect value of equity

What is the value of equity in the firm?

How risky are the cash flows from both existing assets and growth assets?

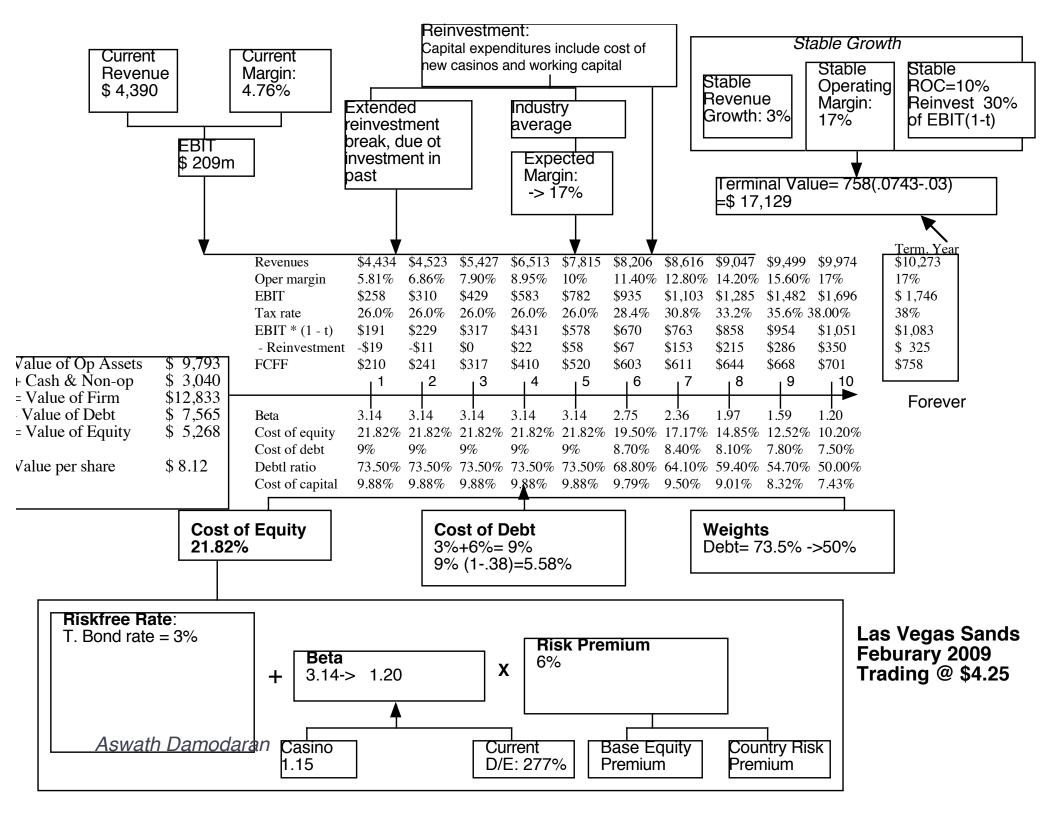
Depending upon the risk of the assets being divested and the use of the proceeds from the divestuture (to pay dividends or retire debt), the risk in both the firm and its equity can change.

When will the firm become a mature fiirm, and what are the potential roadblocks?

There is a real chance, especially with high financial leverage, that the firm will not make it. If it is expected to survive as a going concern, it will be as a much smaller entity.

Dealing with the "downside" of Distress

- A DCF valuation values a firm as a going concern. If there is a significant likelihood of the firm failing before it reaches stable growth and if the assets will then be sold for a value less than the present value of the expected cashflows (a distress sale value), DCF valuations will understate the value of the firm.
- □ Value of Equity= DCF value of equity (1 Probability of distress) + Distress sale value of equity (Probability of distress)
- ☐ There are three ways in which we can estimate the probability of distress:
 - Use the bond rating to estimate the cumulative probability of distress over 10 years
 - Estimate the probability of distress with a probit
 - Estimate the probability of distress by looking at market value of bonds...
- The distress sale value of equity is usually best estimated as a percent of book value (and this value will be lower if the economy is doing badly and there are other firms in the same business also in distress).



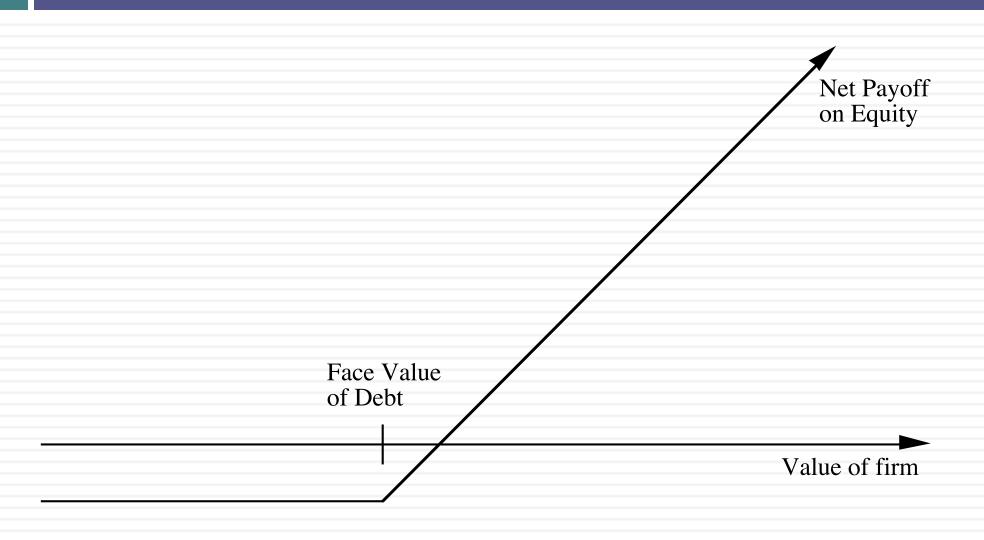
Adjusting the value of LVS for distress...

In February 2009, LVS was rated B+ by S&P. Historically, 28.25% of B+ rated bonds default within 10 years. LVS has a 6.375% bond, maturing in February 2015 (7 years), trading at \$529. If we discount the expected cash flows on the bond at the riskfree rate, we can back out the probability of distress from the bond price:

$$529 = \sum_{t=1}^{t=7} \frac{63.75(1 - \Pi_{\text{Distress}})^t}{(1.03)^t} + \frac{1000(1 - \Pi_{\text{Distress}})^7}{(1.03)^7}$$

- Solving for the probability of bankruptcy, we get:
- \square π_{Distress} = Annual probability of default = 13.54%
 - □ Cumulative probability of surviving 10 years = (1 .1354)10 = 23.34%
 - □ Cumulative probability of distress over 10 years = 1 .2334 = .7666 or 76.66%
- If LVS is becomes distressed:
 - Expected distress sale proceeds = \$2,769 million < Face value of debt
 - Expected equity value/share = \$0.00
- \square Expected value per share = \$8.12 (1 .7666) + \$0.00 (.7666) = \$1.92

The "sunny" side of distress: Equity as a call option to liquidate the firm



Application to valuation: A simple example

- Assume that you have a firm whose assets are currently valued at \$100 million and that the standard deviation in this asset value is 40%.
- Further, assume that the face value of debt is \$80 million (It is zero coupon debt with 10 years left to maturity).
- □ If the ten-year treasury bond rate is 10%,
 - how much is the equity worth?
 - What should the interest rate on debt be?

Model Parameters & Valuation

The inputs

- Value of the underlying asset = S = Value of the firm = \$ 100 million
- Exercise price = K = Face Value of outstanding debt = \$80 million
- Life of the option = t = Life of zero-coupon debt = 10 years
- Variance in the value of the underlying asset = σ^2 = Variance in firm value = 0.16
- Riskless rate = r = Treasury bond rate corresponding to option life = 10%

The output

■ The Black-Scholes model provides the following value for the call:

$$N(d1) = 0.9451$$

$$d2 = 0.3345$$

$$N(d2) = 0.6310$$

- Value of the call = $100 (0.9451) 80 \exp^{(-0.10)(10)} (0.6310) = $75.94 million$
- □ Value of the outstanding debt = \$100 \$75.94 = \$24.06 million
- Interest rate on debt = $($80 / $24.06)^{1/10} 1 = 12.77\%$

Firm value drops...

- Assume now that a catastrophe wipes out half the value of this firm (the value drops to \$ 50 million), while the face value of the debt remains at \$ 80 million.
- The inputs
 - Value of the underlying asset = S = Value of the firm = \$ 50 million
 - All the other inputs remain unchanged
- The output
 - Based upon these inputs, the Black-Scholes model provides the following value for the call:

$$N(d1) = 0.8534$$

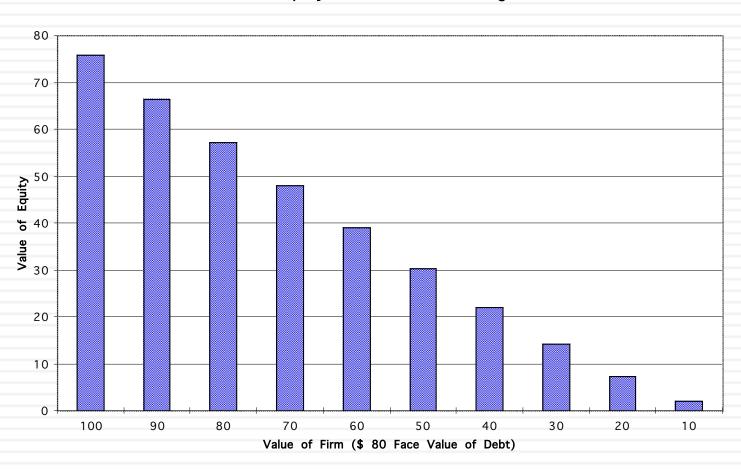
$$d2 = -0.2135$$

$$N(d2) = 0.4155$$

- Value of the call = $50 (0.8534) 80 \exp^{(-0.10)(10)} (0.4155) = $30.44 million$
- Value of the bond= \$50 \$30.44 = \$19.56 million

Equity value persists .. As firm value declines..

Value of Equity as Firm Value Changes



IV. Valuing Financial Service Companies

Existing assets are usually financial assets or loans, often marked to market.
Earnings do not provide much information on underlying risk.

Defining capital expenditures and working capital is a challenge. Growth can be strongly influenced by regulatory limits and constraints. Both the amount of new investments and the returns on these investments can change with regulatory changes.

What is the value added by growth assets?

What are the cashflows from existing assets?

Preferred stock is a significant source of capital.

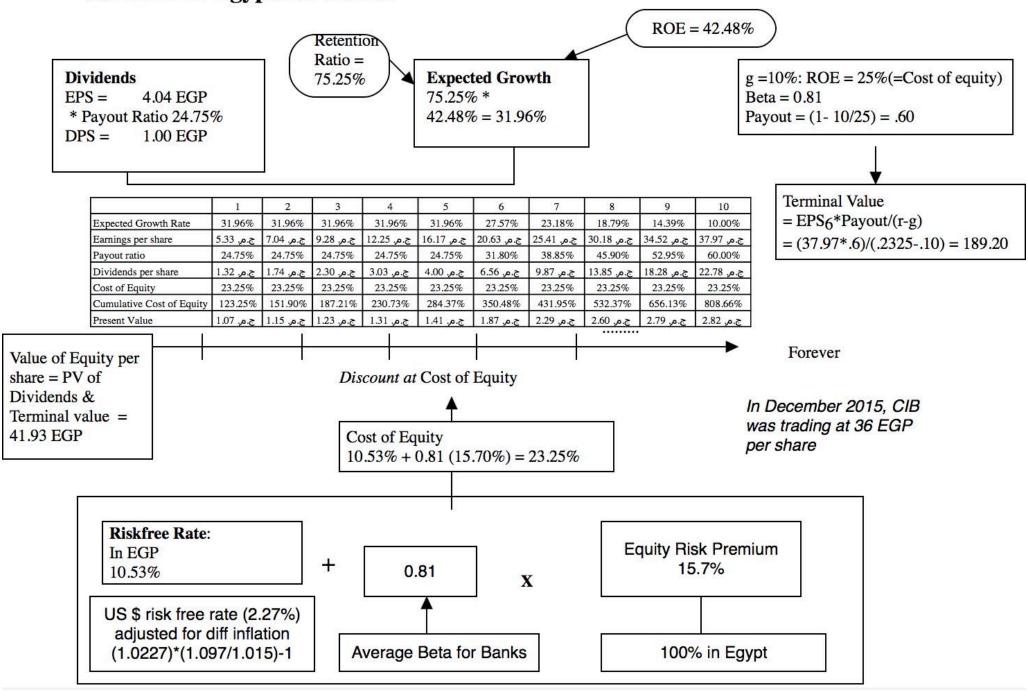
What is the value of equity in the firm?

How risky are the cash flows from both existing assets and growth assets?

For financial service firms, debt is raw material rather than a source of capital. It is not only tough to define but if defined broadly can result in high financial leverage, magnifying the impact of small operating risk changes on equity risk. When will the firm become a mature fiirm, and what are the potential roadblocks?

In addition to all the normal constraints, financial service firms also have to worry about maintaining capital ratios that are acceptable of regulators. If they do not, they can be taken over and shut down.

CIB Egypt in December 2015 Valuation in Egyptian Pounds



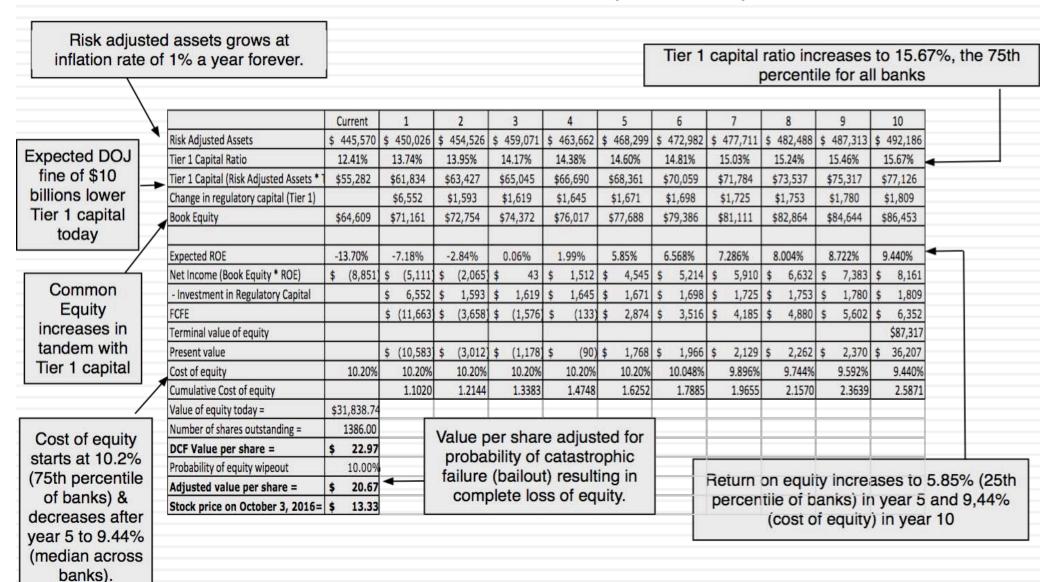
Lesson 1: Financial service companies are opaque...

- □ With financial service firms, we enter into a Faustian bargain. They tell us very little about the quality of their assets (loans, for a bank, for instance are not broken down by default risk status) but we accept that in return for assets being marked to market (by accountants who presumably have access to the information that we don't have).
- In addition, estimating cash flows for a financial service firm is difficult to do. So, we trust financial service firms to pay out their cash flows as dividends. Hence, the use of the dividend discount model.

Lesson 2: For financial service companies, book value matters...

- The book value of assets and equity is mostly irrelevant when valuing non-financial service companies. After all, the book value of equity is a historical figure and can be nonsensical. (The book value of equity can be negative and is so for more than a 1000 publicly traded US companies)
- With financial service firms, book value of equity is relevant for two reasons:
 - Since financial service firms mark to market, the book value is more likely to reflect what the firms own right now (rather than a historical value)
 - The regulatory capital ratios are based on book equity. Thus, a bank with negative or even low book equity will be shut down by the regulators.
- From a valuation perspective, it therefore makes sense to pay heed to book value. In fact, you can argue that reinvestment for a bank is the amount that it needs to add to book equity to sustain its growth ambitions and safety requirements:
 - FCFE = Net Income Reinvestment in regulatory capital (book equity)

Deutsche Bank: A Crisis Valuation (October 2016)



Aswath Damodaran

V. Valuing cyclical and commodity companies

Company growth often comes from movements in the economic cycle, for cyclical firms, or commodity prices, for commodity companies.

What is the value added by growth assets?

What are the cashflows from existing assets?

Historial revenue and earnings data are volatile, as the economic cycle and commodity prices change.

How risky are the cash flows from both existing assets and growth assets?

Primary risk is from the economy for cyclical firms and from commodity price movements for commodity companies. These risks can stay dormant for long periods of apparent prosperity.

When will the firm become a mature fiirm, and what are the potential roadblocks?

For commodity companies, the fact that there are only finite amounts of the commodity may put a limit on growth forever. For cyclical firms, there is the peril that the next recession may put an end to the firm.

Valuing a Cyclical Company - Toyota in Early 2009

	Year	Revenues	Operating Inco	EBITDA	Operating Març
	FY1 1992	¥10,163,380	¥218,511	¥218,511	2.15%
	FY1 1993	¥10,210,750	¥181,897	¥181,897	1.78%
	FY1 1994	¥9,362,732	¥136,226	¥136,226	1.45%
	FY1 1995	¥8,120,975	¥255,719	¥255,719	3.15%
	FY1 1996	¥10,718,740	¥348,069	¥348,069	3.25%
	FY1 1997	¥12,243,830	¥665,110	¥665,110	5.43%
	FY1 1998	¥11,678,400	¥779,800	¥1,382,950	6.68%
	FY1 1999	¥12,749,010	¥774,947	¥1,415,997	6.08%
	FY1 2000	¥12,879,560	¥775,982	¥1,430,982	6.02%
	FY1 2001	¥13,424,420	¥870,131	¥1,542,631	6.48%
	FY1 2002	¥15,106,300	¥1,123,475	¥1,822,975	7.44%
	FY1 2003	¥16,054,290	¥1,363,680	¥2,101,780	8.49%
	FY1 2004	¥17,294,760	¥1,666,894	¥2,454,994	9.64%
	FY1 2005	¥18,551,530	¥1,672,187	¥2,447,987	9.01%
	FY1 2006	¥21,036,910	¥1,878,342	¥2,769,742	8.93%
	FY1 2007	¥23,948,090	¥2,238,683	¥3,185,683	9.35%
	FY1 2008	¥26,289,240	¥2,270,375	¥3,312,775	8.64%
	FY 2009 (Estin	¥22,661,325	¥267,904	¥1,310,304	1.18%
rni	ings (1)		¥1,306,867		7.33%

Normalized Earnings (1)

As a cyclical company, Toyota's earnings have been volatile and 2009 earnings reflect the troubled global economy. We will assume that when economic growth returns, the operating margin for Toyota will revert back to the historical average.

Normalized Operating Income = Revenues in 2009 * Average Operating Margin (98--09)

= 22661 * .0733 = 1660.7 billion ven

In early 2009, Toyota Motors had the highest market share in the sector. However, the global economic recession in 2008-09 had pulled earnings down.

Normalized Return on capital and Reinvestment

Once earnings bounce back to normal, we assume that Toyota will be able to earn a return on capital equal to its cost of capital (5.09%). This is a sector, where earning excess returns has proved to be difficult even for the best of firms.

To sustain a 1.5% growth rate, the reinvestment rate has to be: Reinvestment rate = 1.5%/5.09%

= 29.46%

	/		
	Operating Assets	19,640	_
	+ Cash	2,288	
	+ Non-operating assets	6,845	
	- Debt	11,862	
	- Minority Interests	583	
•	Value of Equity		
	/ No of shares	/3,448	
	Value per share	¥4735	

1660.7 (1.015) (1 - .407) (1 - .2946) = 19,640 billion Value of operating assets = (.0509 - .015)

Normalized Cost of capital (3)

The cost of capital is computed using the average beta of automobile companies (1.10), and Toyota's cost of debt (3.25%) and debt ratio (52.9% debt ratio. We use the Japanese marginal tax rate of 40.7% for computing both the after-tax cost of debt and the after-tax operating income

Cost of capital = 8.65% (.471) + 3.25% (1-.407) (.529) = 5.09%Aswath Damodaran

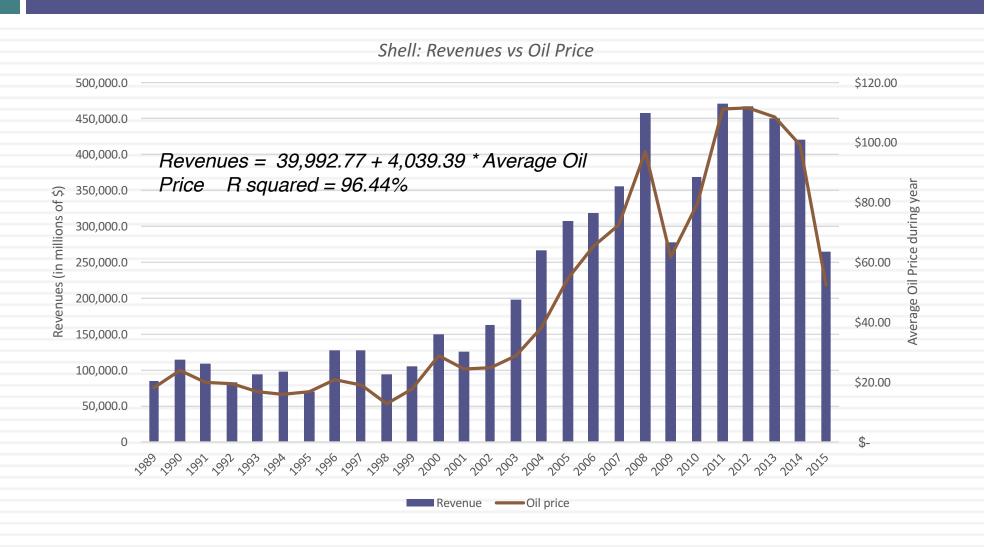
Stable Growth (4)

Once earnings are normalized, we assume that Toyota, as the largest market-share company, will be able to maintain only stable growth (1.5% in Yen terms)

Lesson 1: With "macro" companies, it is easy to get lost in "macro" assumptions...

- With cyclical and commodity companies, it is undeniable that the value you arrive at will be affected by your views on the economy or the price of the commodity.
- Consequently, you will feel the urge to take a stand on these macro variables and build them into your valuation. Doing so, though, will create valuations that are jointly impacted by your views on macro variables and your views on the company, and it is difficult to separate the two.
- The best (though not easiest) thing to do is to separate your macro views from your micro views. Use current market based numbers for your valuation, but then provide a separate assessment of what you think about those market numbers.

Shell's Revenues & Oil Prices



Revenue calculated from prevailing oil price of \$40/barrel in March 2016
Revenue = 39992.77+4039.40*\$40
= \$201,569

Shell: A "Oil Price" Neutral Valuation: March 2016

Compounded revenue growth of 3.91% a year, based on Shell's historical revenue growth rate from 2000 to 2015

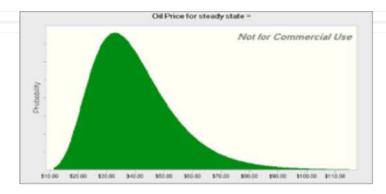
	Base Year	1		2		3		4		5	Те	rminal Year
Revenues	\$ 201,569	\$ 209,450	\$	217,639	\$	226,149	\$	234,991	\$	244,180	\$	249,063
Operating Margin	3.01%	6.18%		7.76%		8.56%		8.95%		9.35%		9.35%
Operating Income	\$ 6,065.00	\$ 12,942.85	\$	16,899.10	\$	19,352.39	\$	21,040.39	\$	22,830.80	\$	23,287.41
Effective tax rate	30.00%	30.00%		30.00%		30.00%		30.00%		30.00%		30.00%
AT Operating Income	\$ 4,245.50	\$ 9,060.00	\$	11,829.37	\$	13,546.68	\$	14,728.27	\$	15,981.56	\$	16,301.19
+ Depreciation	\$ 26,714.00	\$ 27,759	\$	28,844	\$	29,972	\$	31,144	\$	32,361		
- Cap Ex	\$ 31,854.00	\$ 33,099	\$	34,394	\$	35,738	\$	37,136	\$	38,588		
- Chg in WC		\$ 472.88	\$	491.37	\$	510.58	\$	530.55	\$	551.29		
FCFF		\$ 3,246.14	\$	5,788.19	\$	7,269.29	\$	8,205.44	\$	9,203.68	\$	13,011.34
Terminal Value									\$	216,855.71		
Return on capital												12.37%
Cost of Capital		9.91%		9.91%		9.91%		9.91%		9.91%		8.00%
Cumulated Discount Factor		1.0991		1.2080		1.3277		1.4593		1.6039		
Present Value		\$ 2,953.45	\$	4,791.47	\$	5,474.95	\$	5,622.81	\$	140,940.73		
Value of Operating Assets	\$ 159,783.41											
+ Cash	\$ 31,752.00	2 1000	100	141				2 727	1			
+ Cross Holdings	\$ 33,566.00					stments in						
- Debt	\$ 58,379.00	subti	rac	ted out mi		rity interes	tin	consolida	atec	d		
- Minority Interets	\$ 1,245.00				h	oldings.						
Value of Equity	\$ 165,477.41											
Number of shares	4209.7											
Value per share	\$ 39.31											

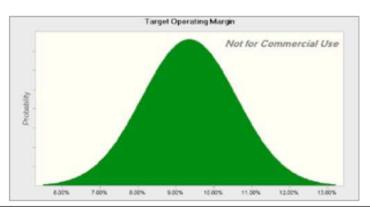
Operating margin converges on Shell's historical average margin of 9.35% from 200-2015

Return on capital reverts and stays at Shell's historic average of 12.37% from 200-2015

Lesson 2: Use probabilistic tools to assess value as a function of macro variables...

- If there is a key macro variable affecting the value of your company that you are uncertain about (and who is not), why not quantify the uncertainty in a distribution (rather than a single price) and use that distribution in your valuation.
- That is exactly what you do in a Monte Carlo simulation, where you allow one or more variables to be distributions and compute a distribution of values for the company.
- With a simulation, you get not only everything you would get in a standard valuation (an estimated value for your company) but you will get additional output (on the variation in that value and the likelihood that your firm is under or over valued)





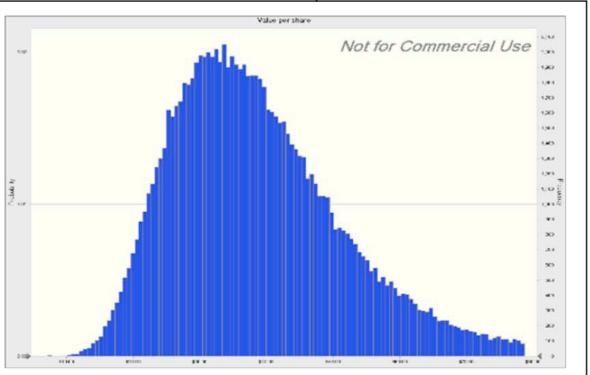
Revenue calculated from the oil price drawn from distribution Revenue = 39992.77+4039.40*Oil Price/Barrel

Pre-tax Operating Income based on revenue & selected margin
Pre-tax Operating Income = Revenues * Operating Margin

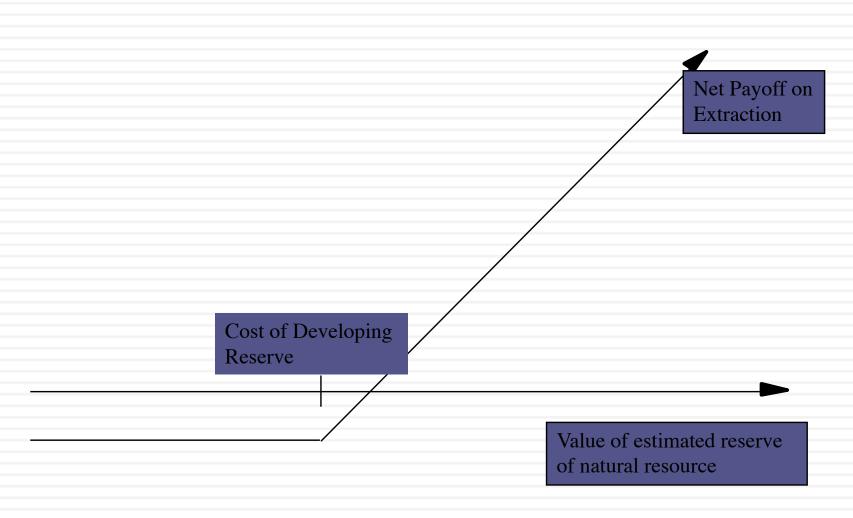
Value Shell based on operating income, assuming other assumptions (tax rate, revenue growth, cost of capital

Percentiles:	Forecast values
0%	\$6.55
10%	\$23.90
20%	\$27.73
30%	\$30.89
40%	\$33.88
50%	\$36.99
60%	\$40.28
70%	\$44.22
80%	\$49.24
90%	\$57.49
100%	\$197.11

124 Aswath Damodaran



The optionality in commodities: Undeveloped reserves as an option



Valuing Gulf Oil

- Gulf Oil was the target of a takeover in early 1984 at \$70 per share (It had 165.30 million shares outstanding, and total debt of \$9.9 billion).
 - It had estimated reserves of 3038 million barrels of oil and the average cost of developing these reserves was estimated to be \$10 a barrel in present value dollars (The development lag is approximately two years).
 - The average relinquishment life of the reserves is 12 years.
 - The price of oil was \$22.38 per barrel, and the production cost, taxes and royalties were estimated at \$7 per barrel.
 - The bond rate at the time of the analysis was 9.00%.
 - Gulf was expected to have net production revenues each year of approximately 5% of the value of the developed reserves. The variance in oil prices is 0.03.

Valuing Undeveloped Reserves

- Inputs for valuing undeveloped reserves
 - Value of underlying asset = Value of estimated reserves discounted back for period of development lag= 3038 * (\$ 22.38 \$7) / 1.05² = \$42,380.44
 - Exercise price = Estimated development cost of reserves = 3038 * \$10 = \$30,380 million
 - Time to expiration = Average length of relinquishment option = 12 years
 - Variance in value of asset = Variance in oil prices = 0.03
 - Riskless interest rate = 9%
 - Dividend yield = Net production revenue/ Value of developed reserves = 5%
- Based upon these inputs, the Black-Scholes model provides the following value for the call:
 - □ d1 = 1.6548 N(d1) = 0.9510
 - d2 = 1.0548 N(d2) = 0.8542
- Call Value= $42,380.44 \exp^{(-0.05)(12)} (0.9510) -30,380 (\exp^{(-0.09)(12)} (0.8542) = $13,306 million$

The composite value...

- In addition, Gulf Oil had free cashflows to the firm from its oil and gas production of \$915 million from already developed reserves and these cashflows are likely to continue for ten years (the remaining lifetime of developed reserves).
- □ The present value of these developed reserves, discounted at the weighted average cost of capital of 12.5%, yields:
 - □ Value of already developed reserves = $915 (1 1.125^{-10})/.125 = 5065.83
- Adding the value of the developed and undeveloped reserves
 - Value of undeveloped reserves = \$ 13,306 million
 - Value of production in place = \$ 5,066 million
 - Total value of firm = \$ 18,372 million
 - Less Outstanding Debt = \$ 9,900 million
 - Value of Equity = \$ 8,472 million
 - □ Value per share = \$8,472/165.3 = \$51.25

VII. Valuing Companies across the ownership cycle

Reported income and balance sheet are heavily affected by tax considerations rather than information disclosure requirements. The line between the personal and business expenses is a fine one.

What is the **value added** by growth assets? Equity: Growth in equity earnings/ cashflows Firm: Growth in operating earnings/ cashflows

What are the cashflows from existing assets?

Equity: Cashflows after debt paymentsFirm: Cashflows before debt payments

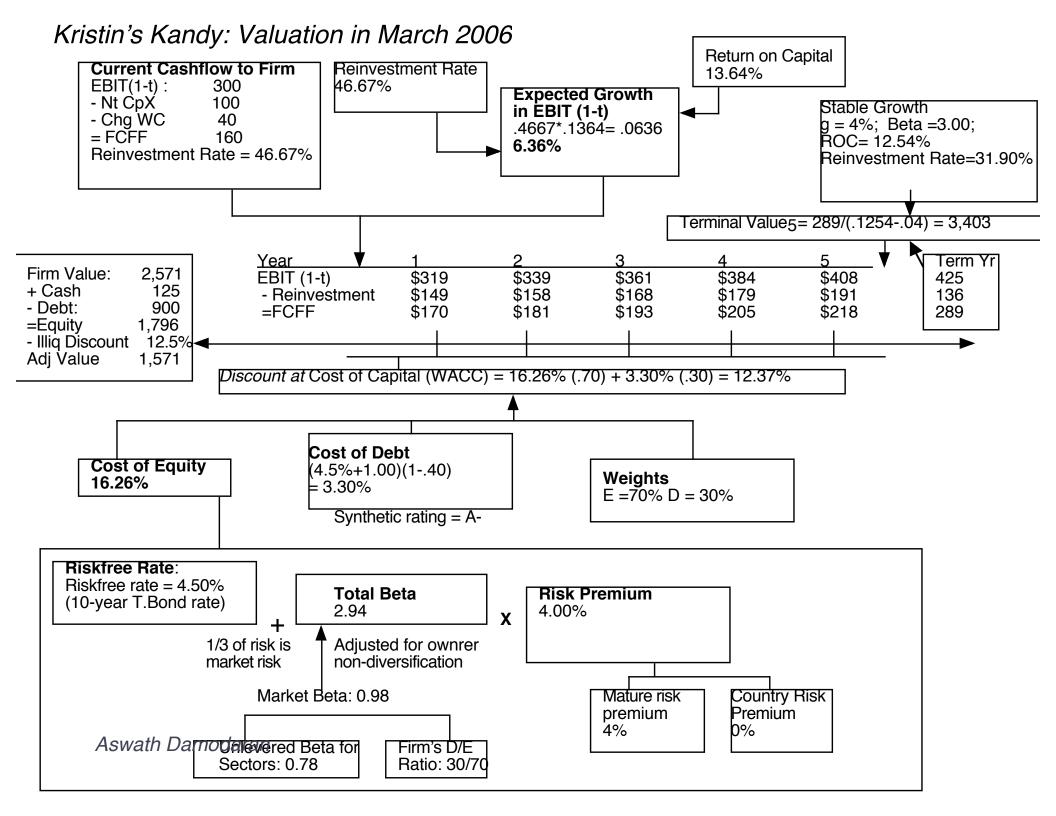
Reversing investment mistakes is difficult to do. The need for and the cost of illiquidity has to be incorporated into current value.

How **risky are the cash flows** from both existing assets and growth assets? Equity: Risk in equity in the company Firm: Risk in the firm's operations

Different buyers can perceive risk differently in the same private business, largely because what they see as risk will be a function of how diversified they are. The fall back positions of using market prices to extract risk measures does not work.

When will the firm become a mature fiirm, and what are the potential roadblocks?

Many private businesses are finite life enterprises, not expected to last into perpetuity



Lesson 1: In private businesses, risk in the eyes of the "beholder" (buyer)

Private business owner with entire wealth invested in the business

Venture capitalist, with multiple holdings in the sector.

Public company investor with diversified portfolio

Exposed to all risk in the company. Total beta measures exposure to total risk. Total Beta = Market Beta/ Correlation of firm with market

Partially diversified.
Diversify away some firm specific risk but not all. Beta will fall berbetween total and market beta.

Firm-specific risk is diversified away.
Market or macro risk exposure captured in a market beta or betas.

Private Owner versus Publicly Traded Company Perceptions of Risk in an Investment

Total Beta measures all risk = Market Beta/ (Portion of the total risk that is market risk)

invested in the business

Demands a cost of equity that reflects this risk

Is exposed

to all the risk

80 units of firm specific risk

Market Beta measures just market risk

Eliminates firmspecific risk in portfolio

20 units of market risk

Publicly traded company with investors who are diversified

Demands a cost of equity that reflects only market risk

Total Risk versus Market Risk

- Adjust the beta to reflect total risk rather than market risk.
 This adjustment is a relatively simple one, since the R squared of the regression measures the proportion of the risk that is market risk.
 - Total Beta = Market Beta / Correlation of the sector with the market
- To estimate the beta for Kristin Kandy, we begin with the bottom-up unlevered beta of food processing companies:
 - Unlevered beta for publicly traded food processing companies = 0.78
 - Average correlation of food processing companies with market = 0.333
 - Unlevered total beta for Kristin Kandy = 0.78/0.333 = 2.34
 - Debt to equity ratio for Kristin Kandy = 0.3/0.7 (assumed industry average)
 - \blacksquare Total Beta = 2.34 (1- (1-.40)(30/70)) = 2.94
 - Total Cost of Equity = 4.50% + 2.94 (4%) = 16.26%

Lesson 2: With financials, trust but verify...

- Different Accounting Standards: The accounting statements for private firms are often based upon different accounting standards than public firms, which operate under much tighter constraints on what to report and when to report.
- Intermingling of personal and business expenses: In the case of private firms, some personal expenses may be reported as business expenses.
- Separating "Salaries" from "Dividends": It is difficult to tell where salaries end and dividends begin in a private firm, since they both end up with the owner.
- The Key Person issue: In some private businesses, with a personal component, the cashflows may be intertwined with the owner being part of the business.

Lesson 3: Illiquidity is a clear and present danger..

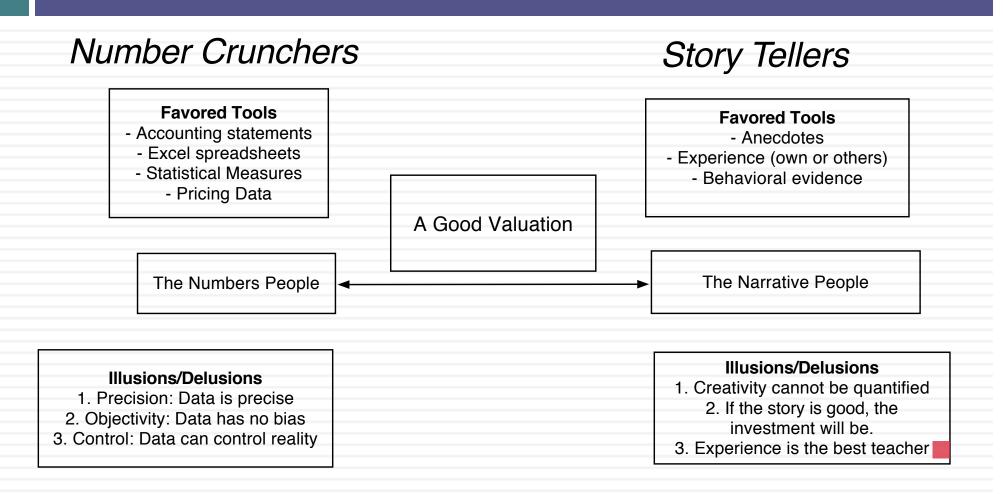
- In private company valuation, illiquidity is a constant theme. All the talk, though, seems to lead to a rule of thumb. The illiquidity discount for a private firm is between 20-30% and does not vary across private firms.
- But illiquidity should vary across:
 - Companies: Healthier and larger companies, with more liquid assets, should have smaller discounts than money-losing smaller businesses with more illiquid assets.
 - Time: Liquidity is worth more when the economy is doing badly and credit is tough to come by than when markets are booming.
 - Buyers: Liquidity is worth more to buyers who have shorter time horizons and greater cash needs than for longer term investors who don't need the cash and are willing to hold the investment.

And it is not just in private businesses...

- Almarai is a publicly traded company with 600 million shares outstanding but only 175 million of these shares are traded (float). One reason is that Almarai, like most Middle Eastern companies, is controlled by family holdings (Savola Group and Al Saud Sultan Mohamed).
- In addition, the Saudi market is not a very liquid market, with little trading volume and not much non-Saudi investor interests in Saudi stocks.
- □ Will the lack of liquidity affect your valuation of Almarai?
- a. Yes
- b. No

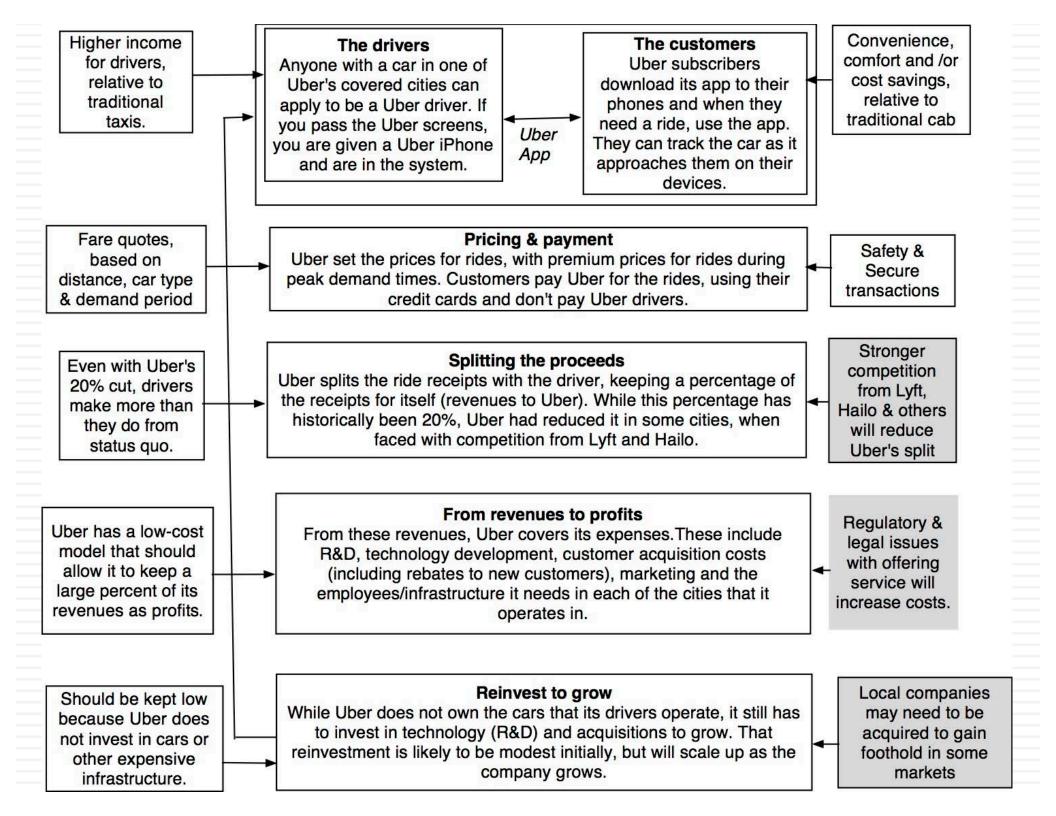
NARRATIVE AND NUMBERS: VALUATION AS A BRIDGE

Valuation as a bridge



Step 1: Survey the landscape

- Every valuation starts with a narrative, a story that you see unfolding for your company in the future.
- In developing this narrative, you will be making assessments of
 - Your company (its products, its management and its history.
 - The market or markets that you see it growing in.
 - The competition it faces and will face.
 - The macro environment in which it operates.



Low Growth

The Auto Business

+

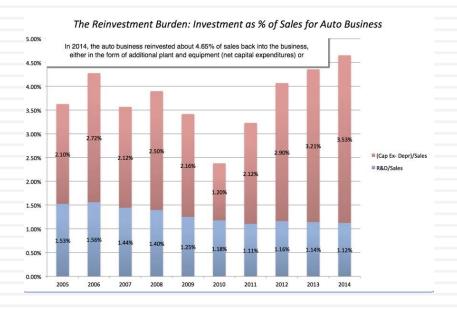
Low Margins

The Automobile Business: Pre-tax Operating Margins in 2015

Year 🔻	Revenues (\$) ▼	% Growth Rate 🔻
2005	1,274,716.60	
2006	1,421,804.20	11.54%
2007	1,854,576.40	30.44%
2008	1,818,533.00	-1.94%
2009	1,572,890.10	-13.51%
2010	1,816,269.40	15.47%
2011	1,962,630.40	8.06%
2012	2,110,572.20	7.54%
2013	2,158,603.00	2.28%
2014	2,086,124.80	-3.36%
ounded Avera	age =	5.63%

30.00% Auto Business- 2015 27.62% Average -2.11% Median 4.46% 10th percentile -13.26% 25.00% 25th percentile 75th percentile 7.99% 90th percentille 20.00% 17.14% 14.29% 10.00% 7.62%

High & Increasing Reinvestment



Bad Business

	ROIC	Cost of capital	ROiC - Cost of capital
2004	6.82%	7.93%	-1.11%
2005	10.47%	7.02%	3.45%
2006	4.60%	7.97%	-3.37%
2007	7.62%	8.50%	-0.88%
2008	3.48%	8.03%	-4.55%
2009	-4.97%	8.58%	-13.55%
2010	5.16%	8.03%	-2.87%
2011	7.55%	8.15%	-0.60%
2012	7.80%	8.55%	-0.75%
2013	7.83%	8.47%	-0.64%
2014	6.47%	7.53%	-1.06%

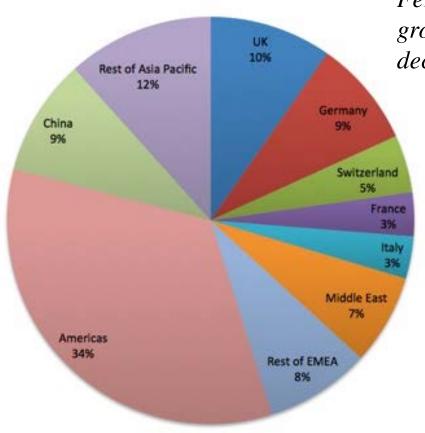
Only once in the last 10 years have auto companies collectively earned more than their cost of capital

What makes Ferrari different?

Ferrari sold only 7,255 cars in all of 2014

Ferrari had a profit margin of 18.2%, in the 95th percentile, partly because of its high prices and partly because it spends little on advertising.

Ferrari: Geographical Sales (2014)



Ferrari sales (in units) have grown very little in the last decade & have been stable

Ferrari has not invested in new plants.

Step 2: Create a narrative for the future

- Every valuation starts with a narrative, a story that you see unfolding for your company in the future.
- In developing this narrative, you will be making assessments of your company (its products, its management), the market or markets that you see it growing in, the competition it faces and will face and the macro environment in which it operates.
 - Rule 1: Keep it simple.
 - Rule 2: Keep it focused.

The Uber Narrative

In June 2014, my initial narrative for Uber was that it would be

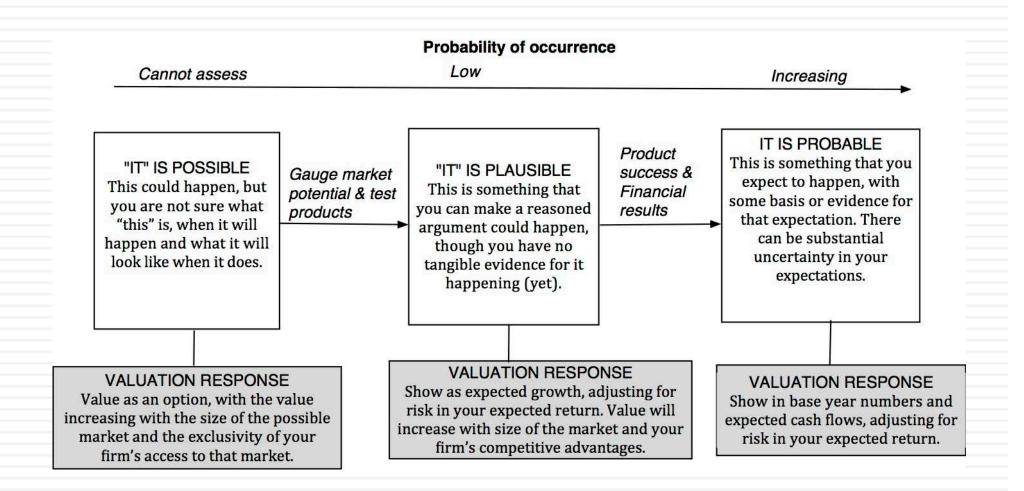
- An urban car service business: I saw Uber primarily as a force in urban areas and only in the car service business.
- 2. Which would expand the business moderately (about 40% over ten years) by bringing in new users.
- With local networking benefits: If Uber becomes large enough in any city, it will quickly become larger, but that will be of little help when it enters a new city.
- 4. Maintain its revenue sharing (20%) system due to strong competitive advantages (from being a first mover).
- 5. And its existing low-capital business model, with drivers as contractors and very little investment in infrastructure.

The Ferrari Narrative

- Ferrari will stay an exclusive auto club, deriving its allure from its scarcity and the fact that only a few own Ferraris.
- By staying exclusive, the company gets three benefits:
 - It can continue to charge nose bleed prices for its cars and sell them with little or no advertising.
 - It does not need to invest in new assembly plants, since it does not plan to ramp up production.
 - It sells only to the super rich, who are unaffected by overall economic conditions or market crises.

Step 3: Check the narrative against history, economic first principles & common sense

146



The Impossible, The Implausible and the Improbable

147

The Impossible

Bigger than the economy

Assuming Growth rate for company in perpetuity> Growth rate for economy

Bigger than the total market

Allowing a company's revenues to grow so much that it has more than a 100% market share of whatever business it is in.

Profit margin > 100%

Assuming earnings growth will exceeds revenue growth for a long enough period, and pushing margins above 100%

Depreciation without cap ex

Assuming that depreciation will exceed cap ex in perpetuity.

The Implausible

Growth without reinvestment

Assuming growth forever without reinvestment.

Profits without competition

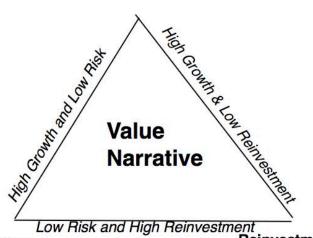
Assuming that your company will grow and earn higher profits, with no competition.

Returns without risk

Assuming that you can generate high returns in a business with no risk.

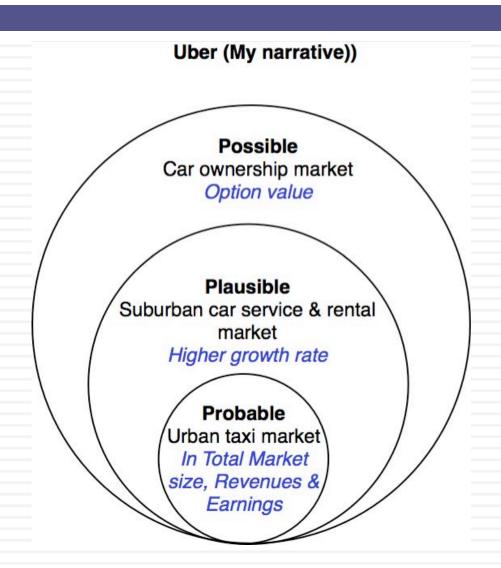
The Improbable

Growth

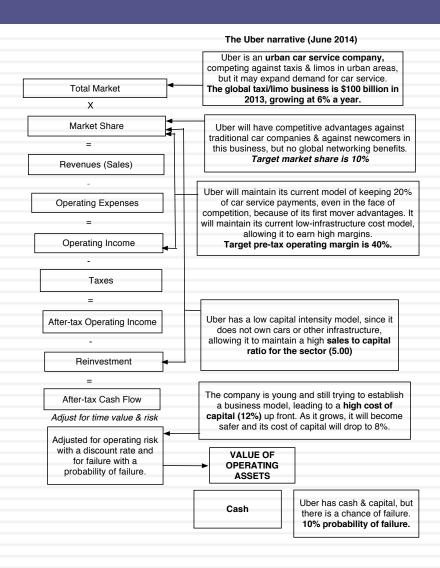


Risk Reinvestment

Uber: Possible, Plausible and Probable



Step 4: Connect your narrative to key drivers of value

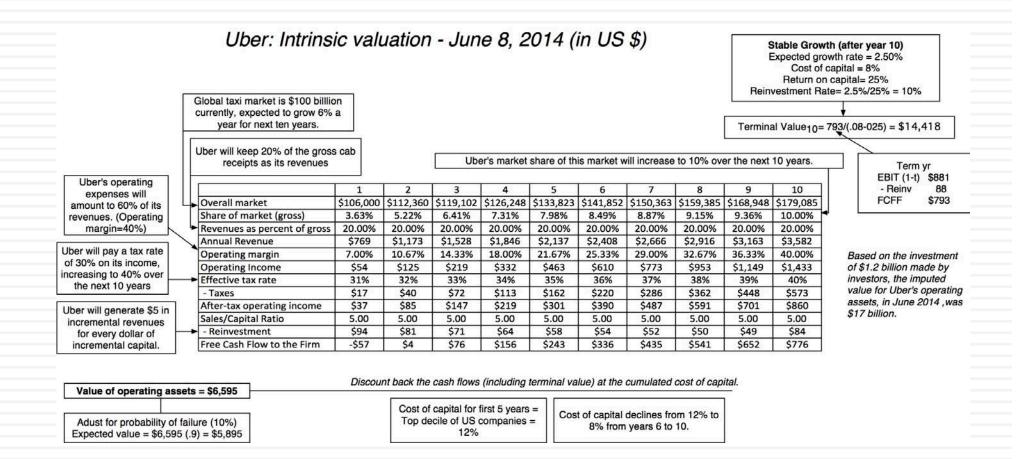


Ferrari: From story to numbers

Valuation Input	The Story	Valuation Inputs
Revenues	Keep it scarce	Revenue growth of 4% (in Euro terms) a year for next 5 years, scaling down to
Operating Margin & Taxes		0.7% in year 10. Translates into an increase in production of about 25% in next 10 years
Operating Income	And pricey	Ferrari's pre-tax operating margin stays at 18.2%, in the 95th percentile of auto business.
Reinvestment	Little need for capacity expansion	Sales/Invested Capital stays at 1.42, i.e. every euro invested generates 1.42 euros in sales
Cash Flow		
Discount Rate (Risk	Super-rich clients are recession-proof	Cost of capital of 6.96% in Euros and no chance of default.
	expansion Super-rich clients are	euros in sales Cost of capital of 6.96% in Euros

Step 5: Value the company (Uber)

151



Ferrari: The "Exclusive Club" Value

Stay Super Exclusive: Revenue growth is low

-	Ba	se year		1		2		3		4		5		6		7		8		9		10	Ter	minal year
Revenue growth rate			4.	00%	4.	00%	4.	00%	4.	00%	4.	00%	3.	34%	2.	68%	2.	02%	1.	36%	0.	70%		0.70%
Revenues	€	2,763	€	2,874	€	2,988	€ :	3,108	€	3,232	€	3,362	€	3,474	€	3,567	€	3,639	€	3,689	€	3,714	€	3,740
EBIT (Operating) margin		18.20%	18	.20%	18	.20%	18	.20%	18	.20%	18	.20%	18	.20%	18	.20%	18	.20%	18	.20%	18	.20%		18.20%
EBIT (Operating income)	€	503	€	523	€	544	€	566	€	588	€	612	€	632	€	649	€	662	€	671	€	676	€	681
Tax rate		33.54%	33	.54%	33	.54%	33	.54%	33	.54%	33	.54%	33	.54%	33	.54%	33	.54%	33	.54%	33	.54%		33.54%
EBIT(1-t)	€	334	€	348	€	361	€	376	€	391	€	407	€	420	€	431	€	440	€	446	€	449	€	452
- Reinvestment			€	78	€	81	€	84	€	87	€	91	€	79	€	66	€	51	€	35	€	18	€	22
FCFF			€	270	€	281	€	292	€	303	€	316	€	341	€	366	€	389	€	411	€	431	€	431
Cost of capital			6.	96%	6.	96%	6.	96%	6.	96%	6.	96%	6.	96%	6.	97%	6.	98%	6.	99%	7.	00%		7.00%
PV(FCFF)			€	252	€	245	€	238	€	232	€	225	€	228	€	228	€	227	€	224	€	220		
Terminal value	€	6,835																						
PV(Terminal value)	€	3,485																						
PV (CF over next 10 years)	€	2,321																						
Value of operating assets =	€	5,806																						
- Debt	€	623				-																		
- Minority interests	€	13																						
+ Cash	€	1,141																						
Value of equity	€	6,311																						

High Prices + No selling cost = Preserve current operating margin

Minimal Reinvestment due to low growth

The super rich are not sensitive to economic downturns

Step 5: Keep the feedback loop

- Not just car service company.: Uber is a car company, not just a car service company, and there may be a day when consumers will subscribe to a Uber service, rather than own their own cars. It could also expand into logistics, i.e., moving and transportation businesses.
- Not just urban: Uber can create new demands for car service in parts of the country where taxis are not used (suburbia, small towns).
- Global networking benefits: By linking with technology and credit card companies, Uber can have global networking benefits.

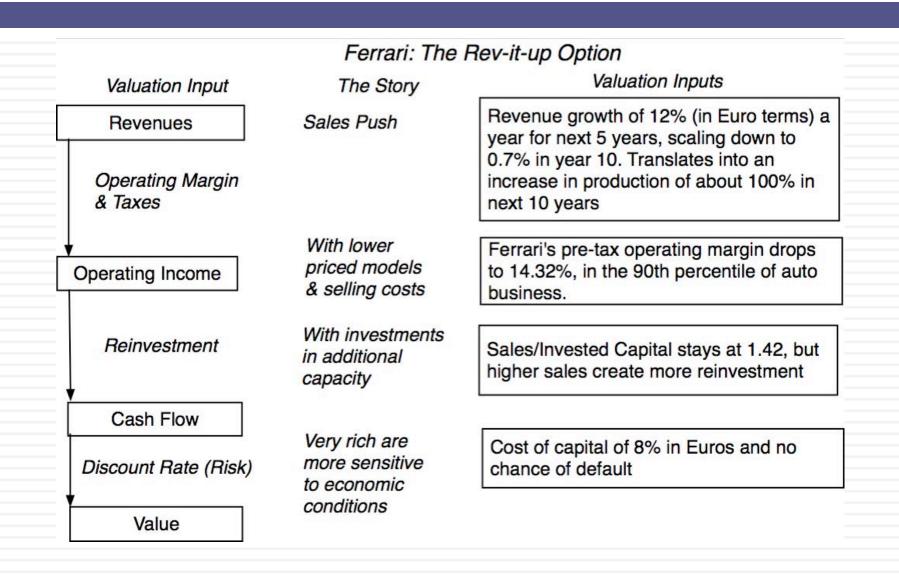
Valuing Bill Gurley's Uber narrative

	Uber (Gurley)	Uber (Gurley Mod)	Uber (Damodaran)
Narrative	Uber will expand the car service	Uber will expand the car service	Uber will expand the car service
	market substantially, bringing in	market substantially, bringing in	market moderately, primarily in
	mass transit users & non-users	mass transit users & non-users from	urban environments, and use its
	from the suburbs into the market,	the suburbs into the market, and use	competitive advantages to get a
	and use its <u>networking</u> advantage	its <u>networking advantage</u> to gain a	significant but not dominant
	to gain a dominant market share,	dominant market share, while	market share and maintain its
	while maintaining its revenue slice	cutting prices and margins (to 10%).	revenue slice at 20%.
	at 20%.		
Total	\$300 billion, growing at 3% a year	\$300 billion, growing at 3% a year	\$100 billion, growing at 6% a year
Market			
Market	40%	40%	10%
Share			
Uber's	20%	10%	20%
revenue			
slice			
Value for	\$53.4 billion + Option value of	\$28.7 billion + Option value of	\$5.9 billion + Option value of
Uber	entering car ownership market	entering car ownership market (\$6	entering car ownership market (\$2-
	(\$10 billion+)	billion+)	3 billion)

Different narratives, Different Numbers

Total Market	Growth Effect	Network Effect	Competitive Advantages	Value of Uber
A4. Mobility Services	B4. Double market size	C5. Strong global network effects	D4. Strong & Sustainable	\$90,457
A3. Logistics	B4. Double market size	C5. Strong global network effects	D4. Strong & Sustainable	\$65,158
A4. Mobility Services	B3. Increase market by 50%	C3. Strong local network effects	D3. Semi-strong	\$52,346
A2. All car service	B4. Double market size	C5. Strong global network effects	D4. Strong & Sustainable	\$47,764
A1. Urban car service	B4. Double market size	C5. Strong global network effects	D4. Strong & Sustainable	\$31,952
A3. Logistics	B3. Increase market by 50%	C3. Strong local network effects	D3. Semi-strong	\$14,321
A1. Urban car service	B3. Increase market by 50%	C3. Strong local network effects	D3. Semi-strong	\$7,127
A2. All car service	B3. Increase market by 50%	C3. Strong local network effects	D3. Semi-strong	\$4,764
A4. Mobility Services	B1. None	C1. No network effects	D1. None	\$1,888
A3. Logistics	B1. None	C1. No network effects	D1. None	\$1,417
A2. All car service	B1. None	C1. No network effects	D1. None	\$1,094
A1. Urban car service	B1. None	C1. No network effects	D1. None	\$799

The Ferrari Counter Narrative



Ferrari: The "Rev-it-up" Alternative

Get less exclusive: Double number of cars sold over next decade

	Ba	se year		1		2		3		4		5		6		7		8		9	1	10	Ter	minal year
Revenue growth rate			12	.00%	12	.00%	12	.00%	12	.00%	12.	00%	9.	74%	7.	48%	5.	22%	2.	96%	0.7	70%		0.70%
Revenues	€	2,763	€	3,095	€	3,466	€ :	3,882	€	4,348	€ 4	1,869	€	5,344	€	5,743	€	6,043	€	6,222	€	5,266	€	6,309
EBIT (Operating) margin		18.20%	17	.81%	17	.42%	17	.04%	16	.65%	16.	26%	15	.87%	15	.48%	15	.10%	14	.71%	14.	32%		14.32%
EBIT (Operating income)	€	503	€	551	€	604	€	661	€	724	€	792	₩	848	€	889	€	912	€	915	₩	897	€	904
Tax rate		33.54%	33	.54%	33	.54%	33	.54%	33	.54%	33.	54%	33	.54%	33	.54%	33	.54%	33	.54%	33.	54%	10	33.54%
EBIT(1-t)	€	334	€	366	€	401	€	439	€	481	€	526	€	564	€	591	€	606	€	608	€	596	€	600
- Reinvestment			€	233	€	261	€	293	€	328	€	367	₩	334	€	281	€	211	€	126	₩	31	€	35
FCFF			€	133	€	140	€	147	€	153	€	159	€	230	€	310	€	395	€	482	€	566	€	565
Cost of capital			8.	00%	8.	00%	8.	00%	8.	00%	8.6	00%	7.	90%	7.	80%	7.	70%	7.	60%	7.5	50%		7.50%
PV(FCFF)			€	123	€	120	€	117	€	113	€	108	€	145	€	181	€	215	€	244	€	266		
Terminal value	€	8,315																						
PV(Terminal value)	€	3,906																						
PV (CF over next 10 years)	€	1,631																						
Value of operating assets =	€	5,537																						
- Debt	€	623																						
- Minority interests	€	13																						
+ Cash	€	1,141																						
Value of equity	€	6,042																						

Lower
Prices +
Some selling
cost = Lower
operating
margin

Reinvestment reflects higher sales

The very rich are more sensitive to economic conditions

And the world is full of feedback.. My Ferrari afterthought!



Step 6: Be ready to modify narrative as events unfold

159

Narrative Break/End	Narrative Shift	Narrative Change (Expansion or Contraction)
Events, external (legal, political or economic) or internal (management, competitive, default), that can cause the narrative to break or end.	Improvement or deterioration in initial business model, changing market size, market share and/or profitability.	Unexpected entry/success in a new market or unexpected exit/failure in an existing market.
Your valuation estimates (cash flows, risk, growth & value) are no longer operative	Your valuation estimates will have to be modified to reflect the new data about the company.	Valuation estimates have to be redone with new overall market potential and characteristics.
Estimate a probability that it will occur & consequences	Monte Carlo simulations or scenario analysis	Real Options

Uber: The September 2015 Update

Input	June 2014	September 2015	Rationale
Total Market	\$100 billion; Urban car service	\$230 billion; Logistics	Market is broader, bigger & more global than I thought it would be. Uber's entry into delivery & moving businesses is now plausible, perhaps even probable.
Growth in market	Increase market size by 34%; CAGR of 6%.	Double market size; CAGR of 10.39%.	New customers being drawn to car sharing, with more diverse offerings.
Market Share	10% (Local Networking)	25% (Weak Global Networking)	Higher cost of entry will reduce competitors, but remaining competitors have access to capital & in Asia, the hometown advantage.
Slice of gross receipts	20% (Left at status quo)	15%	Increased competition will reduce car service company slice.
Operating margin	40% (Low cost model)	25% (Partial employee model)	Drivers will become partial employees, higher insurance and regulatory costs.
Cost of capital	12% (Ninth decile of US companies)	10% (75 th percentile of US companies)	Business model in place and substantial revenues.
Probability of failure	10%	0%	Enough cash on hand to find off threats to survival.
Value of equity	\$5.9 billion	\$23.4 billion	Value increased more than four fold.

Potential Market	Market size (in millions)
A1. Urban car service	\$100,000
A2. All car service	\$175,000
A3. Logistics	\$230,000
A4. Mobility Services	\$310,000

Growth Effect	CAGR (next 10 years)
B1. None	3.00%
B2. Increase market by 25%	5.32%
B3. Increase market size by 50%	7.26%
B4: Double market size	10.39%

Network Effects	Market Share
C1. No network effects	5%
C2. Weak local network effects	10%
C3. Strong local network effects	15%
C4. Weak global network effects	25%
C5. Strong global network effects	40%

ncreases overal	I market to	\$618 bi	illion in v	year 10
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G2

	Base	2016	2017	2018	2019	2020	2021	2022	2023	2024	2025	Assumptions
Overall market	\$230,000	\$253,897	\$280,277	\$309,398	\$341,544	\$377,031	\$416,204	\$459,448	\$507,184	\$559,881	\$618,052	A3 & B4
Share of market (gross)	4.71%	6.74%	8.77%	10.80%	12.83%	14.86%	16.89%	18.91%	20.94%	22.97%	25.00%	C4
Gross Billings	\$10,840	\$17,117	\$24,582	\$33,412	\$43,813	\$56,014	\$70,277	\$86,900	\$106,218	\$128,612	\$154,513	
Revenues as percent of gross	20.00%	19.50%	19.00%	18.50%	18.00%	17.50%	17.00%	16.50%	16.00%	15.50%	15.00%	D3
Annual Revenue	\$2,168	\$3,338	\$4,670	\$6,181	\$7,886	\$9,802	\$11,947	\$14,338	\$16,995	\$19,935	\$23,177	
Operating margin	-23.06%	-18.26%	-13.45%	-8.64%	-3.84%	0.97%	5.77%	10.58%	15.39%	20.19%	25.00%	E2
Operating Income	-\$500	-\$609	-\$628	-\$534	-\$303	\$95	\$690	\$1,517	\$2,615	\$4,026	\$5,794	
Effective tax rate	30.00%	31.00%	32.00%	33.00%	34.00%	35.00%	36.00%	37.00%	38.00%	39.00%	40.00%	
- Taxes	-\$150	-\$189	-\$201	-\$176	-\$103	\$33	\$248	\$561	\$994	\$1,570	\$2,318	
After-tax operating income	-\$350	-\$420	-\$427	-\$358	-\$200	\$62	\$442	\$956	\$1,621	\$2,456	\$3,477	
Sales/Capital Ratio		5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	5.00	F
- Reinvestment		\$234	\$267	\$302	\$341	\$383	\$429	\$478	\$531	\$588	\$648	
Free Cash Flow to the Firm		-\$654	-\$694	-\$660	-\$541	-\$322	\$13	\$478	\$1,090	\$1,868	\$2,828	
Terminal value											\$56,258	
Present value of FCFF		-\$595	-\$573	-\$496	-\$369	-\$200	\$7	\$248	\$520	\$822	\$1,152	
Present value of terminal value											\$22,914	
Cost of capital	10.00%	10.00%	10.00%	10.00%	10.00%	10.00%	9.60%	9.20%	8.80%	8.40%	8.00%	G1

PV of cash flows during next 10 years =	\$515
PV of terminal value =	\$22,914
Value of operating assets	\$23,429
Probability of failure	0.00%
Adjusted value of operating assets	\$23,429
Less Debt	\$0
Value of Equity	\$23,429

Expense Profile	Operating Margin		
E1: Independent contractor	40%		
E2: Partial employee	25%		
E3: Full employee	15%		

	F: Status Quo: Sales/Capital = 5					
•						

Capital Intensity

Competitive Advantages	Slice of Gross Receipts
D1. None	5%
D2. Weak	10%
D3. Semi-strong	15%
D4. Strong & Sustainable	20%

Risk Estimates

G1. Cost of capital at 75th percentile of US companies = 10% G2. Probability of failure in next 10 years= 0%

Uber Valuation: September 2015

Henkel

The Story

Henkel is a stolid (solid and conservatively run) company that has an established presence and brand name power in each of its three markets (industrial adhesives, laundry detergents and household goods) but is unlikely to stray too far (geographically, leverage-wise or business-wise) from its existing domains.

detergents and household goods) but is unlikely to stray too far (geographically, leverage-wise or business-wise) from its existing domains.							
The Assumptions							
	Base year	Years 1-5	Years 6-10	•	After year 10	Link to story	
Revenues (a)	\$ 18,074	4.20%	4.2%->2.2%		0.03%	Solid and slow growth	
Operating margin (b)	15.25%	15.25%	12.80%		12.80%	Strong presence and brand name	
Tax rate	25.00%	25.00%	25.00%		25.00%	Not a risk taker when it comes to taxes	
Reinvestment (c)		Sales to capital ratio	1.52	RIR =	0.43%	Nor with reinvestment	
Return on capital	15.26%	Marginal ROIC =	8.37%		7.00%	Global competition will wear on returns	
Cost of capital (d)		7.48%	7.00%		7.00%	Or with business & leverage risk	
			The	Cash Flows			
	Revenues	Operating Margin	EBIT	EBIT (1-t)	Reinvestment	FCFF	
1	\$ 18,833	15.00%		\$ 2,119	\$ 499	\$ 1,620	
2	\$ 19,624	14.76%	\$ 2,896	\$ 2,172	\$ 520	\$ 1,652	
3	\$ 20,448	14.51%	\$ 2,968	\$ 2,226	\$ 542	\$ 1,684	
4	\$ 21,307	14.27%	\$ 3,040	\$ 2,280	\$ 565	\$ 1,715	
5	\$ 22,202	14.02%	,	\$ 2,335	-	\$ 1,746	
6	\$ 22,949	13.78%	7 -7	\$ 2,372	\$ 492	\$ 1,880	
7	\$ 23,530	13.53%	, , , , , , , , , , , , , , , , , , , ,	\$ 2,389	\$ 382	\$ 2,006	
8	\$ 23,930	13.29%	,	\$ 2,385		\$ 2,122	
9	\$ 24,137	13.04%	\$ 3,149			\$ 2,225	
10	\$ 24,144		7 -/	\$ 2,318	-	\$ 2,313	
Terminal year	\$ 24,151	12.80%	\$ 3,091	\$ 2,319	\$ 10	\$ 2,309	
				he Value			
Terminal value			\$ 33,122				
PV(Terminal value)			\$ 16,316				
PV (CF over next 10 year	rs)		\$ 12,741				
Value of operating asset	's =		\$ 29,057				
Adjustment for distress		\$ -		Probability of failure =	0.00%		
- Debt & Mnority Interests \$, , , , , , , , , , , , , , , , , , , ,				
+ Cash & Other Non-operating assets			\$ 2,305				
		\$ 29,176					
- Value of equity option	s		\$ -				
Number of shares			399.83				
Value per share			\$ 72.97		Stock was trading at =	\$118.22	

Aswath Damodaran

RELATIVE VALUATION (PRICING)

Aswath Damodaran

Relative valuation is pervasive...

- Most asset valuations are relative.
- Most equity valuations on Wall Street are relative valuations.
 - Almost 85% of equity research reports are based upon a multiple and comparables.
 - More than 50% of all acquisition valuations are based upon multiples
 - Rules of thumb based on multiples are not only common but are often the basis for final valuation judgments.
- While there are more discounted cashflow valuations in consulting and corporate finance, they are often relative valuations masquerading as discounted cash flow valuations.
 - The objective in many discounted cashflow valuations is to back into a number that has been obtained by using a multiple.
 - The terminal value in a significant number of discounted cashflow valuations is estimated using a multiple.

The Reasons for the allure...

"If you think I'm crazy, you should see the guy who lives across the hall"

Jerry Seinfeld talking about Kramer in a Seinfeld episode

" A little inaccuracy sometimes saves tons of explanation"

H.H. Munro

" If you are going to screw up, make sure that you have lots of company"

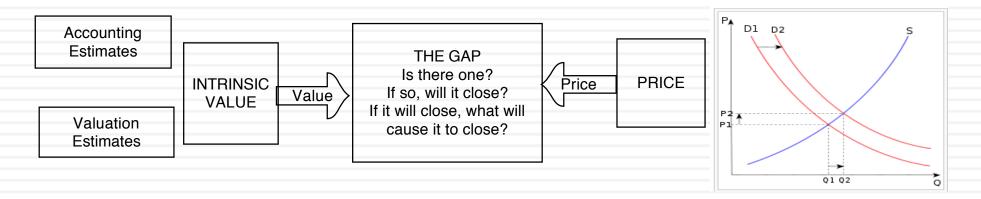
Ex-portfolio manager

Drivers of intrinsic value

- Cashflows from existing assets
- Growth in cash flows
- Quality of Growth

Drivers of price

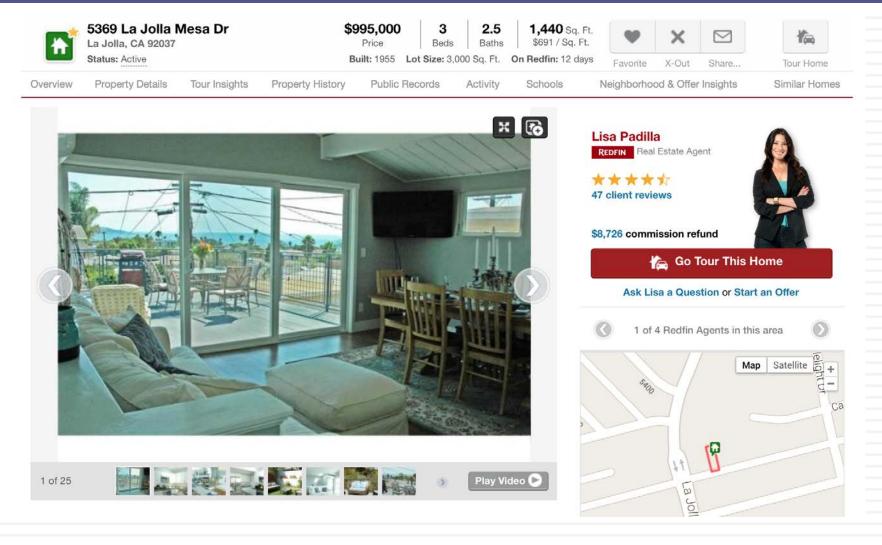
- Market moods & momentum
- Surface stories about fundamentals



Aswath Damodaran

Test 1: Are you pricing or valuing?

167



Test 2: Are you pricing or valuing?

168

Europe

Switzerland

Biotechnology

Biotechnology

Reuters BION.S Bloomberg BION SW Exchange Ticker SWX BION Price at 12 Aug 2013 (CHF) 124.00

Price Target (CHF) 164.50

52-week range (CHF) 128.40 - 84.90

Strong sector and stock-picking continue

Impressive performance

Over the past two years, BB Biotech shares have roughly tripled, which could tempt investors to take profits. However, this performance has been well backed by a deserved revival of the biotech industry, encouraging fundamental news, M&A, and increased money flow into health care stocks. In addition, BBB returned to index outperformance by modifying its stock-picking approach. Hence, despite excellent performance, the shares still trade at a 23% discount to the net asset value of the portfolio. Hence, the shares are an attractive value vehicle to capture growth opportunities in an attractive sector.

Biotech industry remains attractive

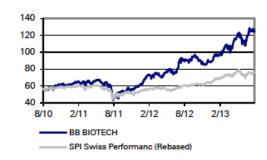
With the re-rating of the pharma sector, investors have also showed increased interest in biotech stocks. Established biotech stocks have delivered encouraging financial results and approvals, while there has also been substantial industry consolidation, which is not surprising in times of "cheap" money and high liquidity. BB Biotech remains an attractive vehicle to capture the future potential of the biotech sector. In addition, investors benefit from a 23% discount to NAV and attractive cash distribution policy of 5% yield p.a. Hence, we reiterate our Ruy on RR Riotech shares

Key changes Target Price 106.50 to 164.50 ↑

54.5%

Price/price relative

Source: Deutsche Bank



Performance (%)	1m	3m	12m
Absolute	-1.4	5.4	37.4

Test 3: Are you pricing or valuing?

\$200.00

\$1,132.81

4	60	
I	09	

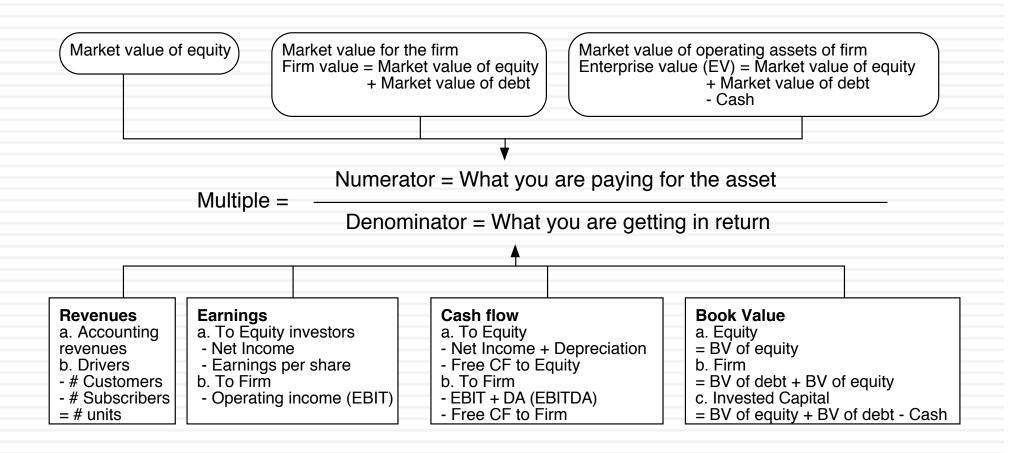
	1	2	3	4	5
EBITDA	\$100.00	\$120.00	\$144.00	\$172.80	\$207.36
- Depreciation	\$20.00	\$24.00	\$28.80	\$34.56	\$41.47
EBIT	\$80.00	\$96.00	\$115.20	\$138.24	\$165.89
- Taxes	\$24.00	\$28.80	\$34.56	\$41.47	\$49.77
EBIT (1-t)	\$56.00	\$67.20	\$80.64	\$96.77	\$116.12
+ Depreciation	\$20.00	\$24.00	\$28.80	\$34.56	\$41.47
- Cap Ex	\$50.00	\$60.00	\$72.00	\$86.40	\$103.68
- Chg in WC	\$10.00	\$12.00	\$14.40	\$17.28	\$20.74
FCFF	\$16.00	\$19.20	\$23.04	\$27.65	\$33.18
Terminal Value					\$1,658.88
Cost of capital	8.25%	8.25%	8.25%	8.25%	8.25%
Present Value	\$14.78	\$16.38	\$18.16	\$20.14	\$1,138.35
Value of operating assets today	\$1,207.81				
+ Cash	\$125.00				

Aswath Damodaran

- Debt

Value of equity

The tool for pricing: A multiple



The Four Steps to Deconstructing Multiples

Define the multiple

In use, the same multiple can be defined in different ways by different users. When comparing and using multiples, estimated by someone else, it is critical that we understand how the multiples have been estimated

Describe the multiple

Too many people who use a multiple have no idea what its cross sectional distribution is. If you do not know what the cross sectional distribution of a multiple is, it is difficult to look at a number and pass judgment on whether it is too high or low.

Analyze the multiple

It is critical that we understand the fundamentals that drive each multiple, and the nature of the relationship between the multiple and each variable.

Apply the multiple

Defining the comparable universe and controlling for differences is far more difficult in practice than it is in theory.

Definitional Tests

- □ Is the multiple consistently defined?
 - Proposition 1: Both the value (the numerator) and the standardizing variable (the denominator) should be to the same claimholders in the firm. In other words, the value of equity should be divided by equity earnings or equity book value, and firm value should be divided by firm earnings or book value.
- Is the multiple uniformly estimated?
 - The variables used in defining the multiple should be estimated uniformly across assets in the "comparable firm" list.
 - If earnings-based multiples are used, the accounting rules to measure earnings should be applied consistently across assets. The same rule applies with book-value based multiples.

Example 1: Price Earnings Ratio: Definition

PE = Market Price per Share / Earnings per Share

There are a number of variants on the basic PE ratio in use. They are based upon how the price and the earnings are defined.

Price: is usually the current price is sometimes the average price for the year

EPS: EPS in most recent financial year
EPS in trailing 12 months (Trailing PE)
Forecasted EPSnnext year (Forward PE)
Forecasted EPS in future year

Example 2: Enterprise Value / EBITDA Multiple

 The enterprise value to EBITDA multiple is obtained by netting cash out against debt to arrive at enterprise value and dividing by EBITDA.

```
Enterprise Value 
EBITDA = Market Value of Equity + Market Value of Debt - Cash

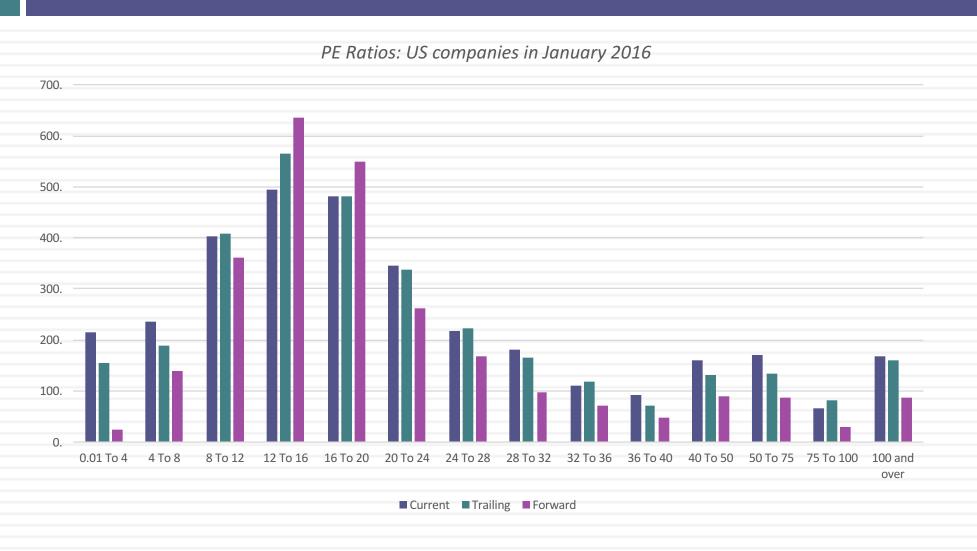
Earnings before Interest, Taxes and Depreciation
```

- Why do we net out cash from firm value?
- What happens if a firm has cross holdings which are categorized as:
 - Minority interests?
 - Majority active interests?

Descriptive Tests

- What is the average and standard deviation for this multiple, across the universe (market)?
- What is the median for this multiple?
 - The median for this multiple is often a more reliable comparison point.
- How large are the outliers to the distribution, and how do we deal with the outliers?
 - Throwing out the outliers may seem like an obvious solution, but if the outliers all lie on one side of the distribution (they usually are large positive numbers), this can lead to a biased estimate.
- Are there cases where the multiple cannot be estimated? Will ignoring these cases lead to a biased estimate of the multiple?
- How has this multiple changed over time?

1. Multiples have skewed distributions...



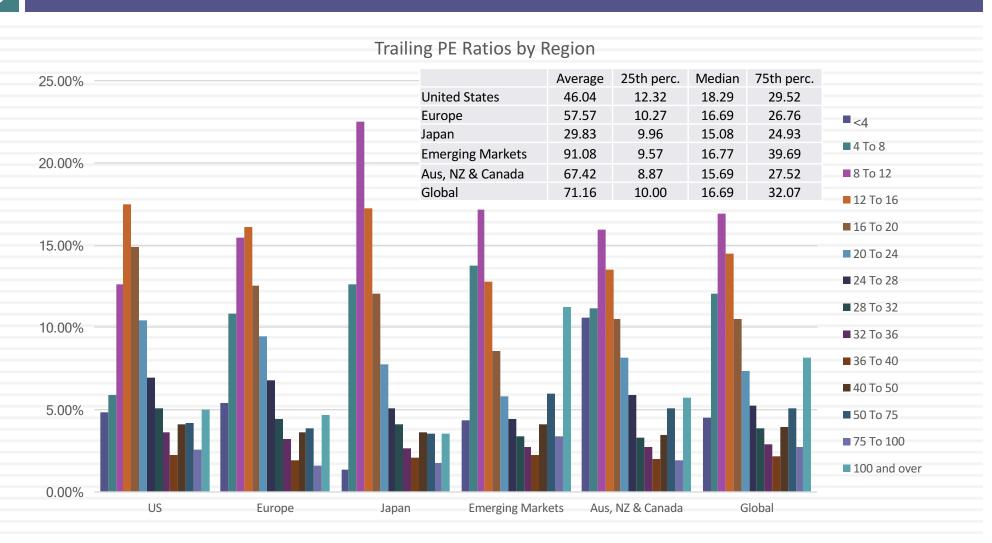
2. Making statistics "dicey"

	Current PE	Trailing PE	Forward PE
Number of firms	7480	7480	7480
Number with PE	3,344.	3,223.	2,647.
Average	59.42	46.04	29.63
Median	18.53	18.29	16.98
Minimum	0.11	0.28	0.15
Maximum	32,269.00	6,900.00	2,748.00
Standard deviation	777.02	256.06	81.27
Standard error	13.44	4.51	1.58
Skewness	37.27	19.9	18.74
25th percentile	11.88	12.32	13.1
75th percentile	30.25	29.52	24.28

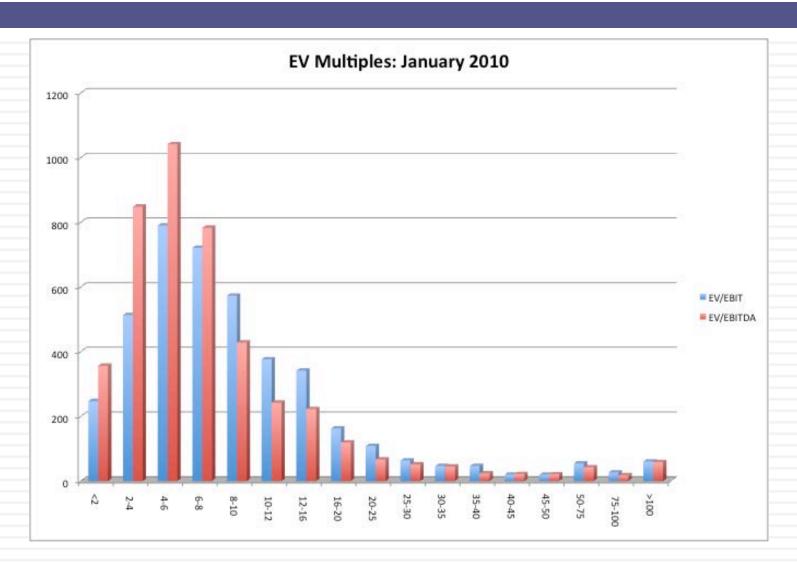
US firms in January 2016

3. Markets have a lot in common: Comparing Global PEs



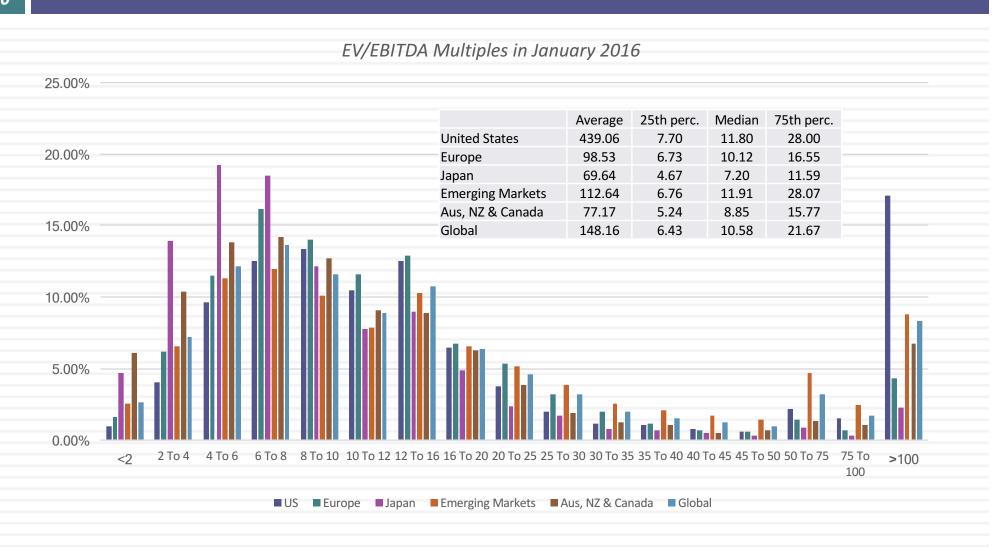


4. Simplistic rules almost always break down...6 times EBITDA may not be cheap...



But it may be in 2016, unless you are in Japan, Australia or Canada

180



Analytical Tests

- What are the fundamentals that determine and drive these multiples?
 - Proposition 2: Embedded in every multiple are all of the variables that drive every discounted cash flow valuation - growth, risk and cash flow patterns.
 - In fact, using a simple discounted cash flow model and basic algebra should yield the fundamentals that drive a multiple
- How do changes in these fundamentals change the multiple?
 - The relationship between a fundamental (like growth) and a multiple (such as PE) is seldom linear. For example, if firm A has twice the growth rate of firm B, it will generally not trade at twice its PE ratio
 - Proposition 3: It is impossible to properly compare firms on a multiple, if we do not know the nature of the relationship between fundamentals and the multiple.

PE Ratio: Understanding the Fundamentals

- To understand the fundamentals, start with a basic equity discounted cash flow model.
- With the dividend discount model,

$$P_0 = \frac{DPS_1}{r - g_n}$$

Dividing both sides by the current earnings per share,

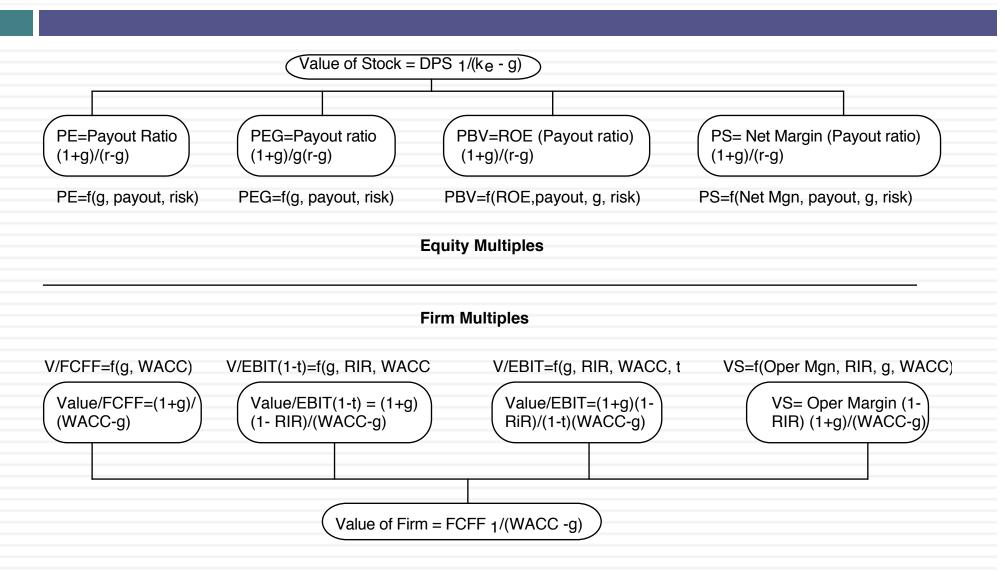
$$\frac{P_0}{EPS_0} = PE = \frac{Payout Ratio * (1 + g_n)}{r - g_n}$$

If this had been a FCFE Model,

$$P_0 = \frac{FCFE_1}{r - g_n}$$

$$\frac{P_0}{EPS_0} = PE = \frac{(FCFE/Earnings)*(1+g_n)}{r-g_n}$$

The Determinants of Multiples...



Application Tests

- Given the firm that you are valuing, what is a "comparable" firm?
 - While traditional analysis is built on the premise that firms in the same sector are comparable firms, valuation theory would suggest that a comparable firm is one which is similar to the one being analyzed in terms of fundamentals.
 - Proposition 4: There is no reason why a firm cannot be compared with another firm in a very different business, if the two firms have the same risk, growth and cash flow characteristics.
- Given the comparable firms, how do you adjust for differences across firms on the fundamentals?
 - Proposition 5: It is impossible to find an exactly identical firm to the one you are valuing.

An Example: Comparing PE Ratios across a Sector: PE

Company Name	PE	Growth
PT Indosat ADR	7.8	0.06
Telebras ADR	8.9	0.075
Telecom Corporation of New Zealand ADR	11.2	0.11
Telecom Argentina Stet - France Telecom SA ADR B	12.5	0.08
Hellenic Telecommunication Organization SA ADR	12.8	0.12
Telecomunicaciones de Chile ADR	16.6	0.08
Swisscom AG ADR	18.3	0.11
Asia Satellite Telecom Holdings ADR	19.6	0.16
Portugal Telecom SA ADR	20.8	0.13
Telefonos de Mexico ADR L	21.1	0.14
Matav RT ADR	21.5	0.22
Telstra ADR	21.7	0.12
Gilat Communications	22.7	0.31
Deutsche Telekom AG ADR	24.6	0.11
British Telecommunications PLC ADR	25.7	0.07
Tele Danmark AS ADR	27	0.09
Telekomunikasi Indonesia ADR	28.4	0.32
Cable & Wireless PLC ADR	29.8	0.14
APT Satellite Holdings ADR	31	0.33
Telefonica SA ADR	32.5	0.18
Royal KPN NV ADR	35.7	0.13
Telecom Italia SPA ADR	42.2	0.14
Nippon Telegraph & Telephone ADR	44.3	0.2
France Telecom SA ADR	45.2	0.19
Korea Telecom ADR	71.3	0.44

PE, Growth and Risk

- Dependent variable is: PE
- \square R squared = 66.2% R squared (adjusted) = 63.1%

Variable	Coefficient	SE	t-ratio	Probability
Constant	13.1151	3.471	3.78	0.0010
Growth rate	121.223	19.27	6.29	≤ 0.0001
Emerging Market	-13.853	3.606	-3.84	0.0009

Emerging Market is a dummy:

1 if emerging market

0 if not

□ Is Indosat cheap?

At 7.8 times earnings, Indosat is over valued.

Henkel: A Relative Valuation

	Exchange:Ticke					EV/ Invested
Company Name	<u>r</u>	<u>PE</u>	<u>PBV</u>	EV/Sales	EV/EBITDA	<u>Capital</u>
The Procter & Gamble Company	NYSE:PG	21.14	3.81	3.73	13.96	3.20
Colgate-Palmolive Co.	NYSE:CL	45.20	NA	4.45	15.89	NA
Reckitt Benckiser Group plc	LSE:RB.	29.87	6.47	5.31	18.21	5.38
Henkel AG & Co. KGaA	DB:HEN3	22.88	3.38	2.54	13.66	3.46
Kimberly-Clark Corporation	NYSE:KMB	20.46	136.45	2.63	11.53	6.72
Svenska Cellulosa Aktiebolaget SCA	OM:SCA B	31.56	2.52	1.79	10.88	2.04
The Clorox Company	NYSE:CLX	23.73	51.77	3.00	14.42	7.80
Church & Dwight Co. Inc.	NYSE:CHD	26.85	6.06	3.77	15.96	4.53
Spectrum Brands Holdings, Inc.	NYSE:SPB	27.37	4.58	2.33	13.54	2.15
HRG Group, Inc.	NYSE:HRG	FALSE	5.48	1.87	9.01	1.60
Energizer Holdings, Inc.	NYSE:ENR	23.42	NA	2.16	11.83	NA
PZ Cussons Plc	LSE:PZC	18.03	2.42	1.68	10.88	2.13
WD-40 Company	NasdaqGS:WDF C	28.86	10.81	4.02	19.68	9.95
Central Garden & Pet Company	NasdaqGS:CEN	26.86	2.21	0.88	9.63	1.74
McBride plc	LSE:MCB	18.93	4.70	0.60	7.70	2.55
Orchids Paper Products Company	AMEX:TIS	16.66	2.01	2.10	10.52	1.59
Oil-Dri Corp. of America	NYSE:ODC	17.80	2.09	0.87	8.29	2.24
Suominen Oyj	HLSE:SUY1V	11.69	1.43	0.52	4.78	1.32
Accrol Group Holdings Plc	AIM:ACRL	17.74	NA	1.28	9.29	NA
Median		23.15	4.20	2.16	11.53	2.39
Henkel versus Median (Under or Over))	-1.16%	-19.54%	17.57%	18.45%	44.70%

Aswath Damodaran

Henkel: Controlling for differences

	Operating				<u>Net</u> Debt/Market	Expected Crowth in	Revenue
Company Name	Operating Margin	Net Margin	ROIC	ROE	Cap	Growth in EPS	CAGR (Last 5 vears)
The Procter & Gamble Company	22.00%	16.27%	14.23%	18.02%	7.60%	6.30%	-4.57%
Colgate-Palmolive Co.	25.17%	9.04%	53.52%	NA	8.40%	6.93%	-4.57 % -0.75%
Reckitt Benckiser Group plc	27.45%	17.17%	21.34%	21.67%	3.79%	11.00%	0.17%
Henkel AG & Co. KGaA	16.11%	11.15%	16.66%	14.75%	-0.91%	8.96%	3.17%
Kimberly-Clark Corporation		10.96%	33.53%	666.89%	16.74%	7.20%	-2.59%
Svenska Cellulosa Aktiebolaget SCA	18.92%						
The Clorox Company	11.20%	4.62%	7.49%	8.00% 218.18%	20.54%	8.04%	10.80%
Church & Dwight Co. Inc.	18.23%	11.25%	31.23%		12.48%	7.05%	1.95%
Spectrum Brands Holdings, Inc.	20.64%	13.12%	16.21%	22.57%	7.15%	9.41%	5.64%
HRG Group, Inc.	13.58%	5.78%	9.72%	16.74%	46.63%	12.20%	10.10%
	16.19%	-6.49%	9.37%	-60.24%	179.41%	0.00%	13.00%
Energizer Holdings, Inc.	15.97%	8.07%	45.82%	NA	14.16%	5.77%	NA
PZ Cussons Plc	12.82%	8.24%	13.49%	13.44%	12.05%	0.00%	0.01%
WD-40 Company	18.73%	13.82%	33.50%	37.46%	0.89%	10.00%	2.50%
Central Garden & Pet Company	6.80%	2.54%	8.73%	8.24%	28.87%	11.00%	2.42%
McBride plc	5.03%	2.50%	14.15%	24.81%	28.23%	0.00%	-3.47%
Orchids Paper Products Company	12.85%	9.32%	6.48%	12.09%	35.53%	14.30%	13.60%
Oil-Dri Corp. of America	5.87%	5.18%	14.29%	11.76%	-5.53%	0.00%	2.96%
Suominen Oyj	6.71%	3.69%	11.07%	12.19%	21.64%	-0.20%	19.80%
Accrol Group Holdings Plc	10.52%	4.83%	NA	NA	NA	0.00%	NA
Median	15.97%	8.24%	14.26%	15.75%	13.32%	7.05%	2.50%
Henkel versus Median (Under or Over)	0.84%	35.37%	16.81%	-6.32%	-106.83%	27.09%	26.80%

Comparisons to the entire market: Why not?

- In contrast to the 'comparable firm' approach, the information in the entire cross-section of firms can be used to predict PE ratios.
- The simplest way of summarizing this information is with a multiple regression, with the PE ratio as the dependent variable, and proxies for risk, growth and payout forming the independent variables.

100

PEG Ratio Regression - US stocks January 2016

Model Summary^{a,c,d}

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.717 ^b	.514	.513	133.686530

- a. Broad Group = United States
- b. Predictors: (Constant), In (Expected Growth in EPS), Payout ratio, Beta
- c. Dependent Variable: PEG
- d Wainbrad Lance Courses Danvarrian Wainbrad by Marko

Coefficients a,b,c

		Unstandardize	d Coefficients	Standardized Coefficients		
Model		В	Std. Error	Beta	t	Sig.
1	(Constant)	580	.265		-2.187	.029
	Payout ratio	1.848	.109	.420	16.980	.000
l	Beta	675	.106	159	-6.361	.000
	In (Expected Growth in EPS)	-1.248	.087	348	-14.427	.000

- a. Broad Group = United States
- b. Dependent Variable: PEG
- c. Weighted Least Squares Regression Weighted by Market Cap (in US \$)

PE ratio regressions across markets – January 2016

191

Region	Regression – January 2016	\mathbb{R}^2
US	$PE = 8.76 + 75.24 g_{EPS} + 19.73 Payout - 4.08 Beta$	40.5%
Europe	$PE = 13.43 + 54.46 g_{EPS} + 17.63 Payout - 4.16 Beta$	24.7%
Japan	$PE = 20.10 + 26.46 g_{EPS} + 24.87 Payout - 7.60 Beta$	28.4%
Emerging Markets	$PE = 15.13 + 40.99 g_{EPS} + 9.03 Payout - 2.14 Beta$	11.5%
Australia, NZ, Canada	$PE = 7.31 + 73.42 g_{EPS} + 13.94 Payout - 3.73 Beta$	26.8%
Global	$PE = 12.51 + 87.48 g_{EPS} + 11.48 Payout - 3.96 Beta$	27.5%

<u>g_{EPS}=Expected Growth</u>: Expected growth in EPS or Net Income: Next 5 years

Beta: Regression or Bottom up Beta

 $\underline{\textit{Payout ratio:}} \ \textit{Dividends/Net income from most recent year. Set to zero, if net income} < 0$

Choosing Between the Multiples

- As presented in this section, there are dozens of multiples that can be potentially used to value an individual firm.
- In addition, relative valuation can be relative to a sector (or comparable firms) or to the entire market (using the regressions, for instance)
- Since there can be only one final estimate of value, there are three choices at this stage:
 - Use a simple average of the valuations obtained using a number of different multiples
 - Use a weighted average of the valuations obtained using a nmber of different multiples
 - Choose one of the multiples and base your valuation on that multiple

Picking one Multiple

- This is usually the best way to approach this issue. While a range of values can be obtained from a number of multiples, the "best estimate" value is obtained using one multiple.
- The multiple that is used can be chosen in one of two ways:
 - Use the multiple that best fits your objective. Thus, if you want the company to be undervalued, you pick the multiple that yields the highest value.
 - Use the multiple that has the highest R-squared in the sector when regressed against fundamentals. Thus, if you have tried PE, PBV, PS, etc. and run regressions of these multiples against fundamentals, use the multiple that works best at explaining differences across firms in that sector.
 - Use the multiple that seems to make the most sense for that sector, given how value is measured and created.

Conventional usage...

Sector	Multiple Used	Rationale
Cyclical Manufacturing	PE, Relative PE	Often with normalized earnings
Growth firms	PEG ratio	Big differences in growth rates
Young growth firms w/ losses	Revenue Multiples	What choice do you have?
Infrastructure	EV/EBITDA	Early losses, big DA
REIT	P/CFE (where CFE = Net income + Depreciation)	Big depreciation charges on real estate
Financial Services	Price/ Book equity	Marked to market?
Retailing	Revenue multiples	Margins equalize sooner or later

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A closing thought...

