
Turnaround: Applications of the Z-Score Model in the US and China

The GTI Case

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Corporate Bankruptcy & Reorganization
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Corporate Credit Scoring Models and the Bond Rating Equivalence

Forecasting Distress With Discriminant Analysis

Linear Form

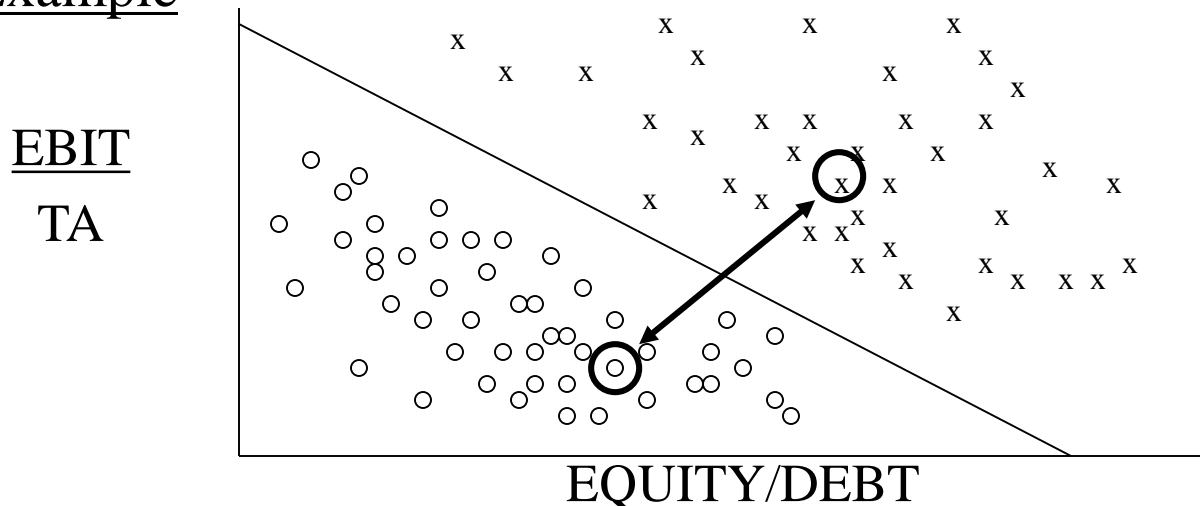
$$Z = a_1x_1 + a_2x_2 + a_3x_3 + \dots + a_nx_n$$

Z = Discriminant Score (Z Score)

$a_1 \rightarrow a_n$ = Discriminant Coefficients (Weights)

$x_1 \rightarrow x_n$ = Discriminant Variables (e.g. Ratios)

Example



"Z" Score Component Definitions

<u>Variable</u>	<u>Definition</u>	<u>Weighting Factor</u>
X_1 - - - - -	$\frac{\text{Working Capital}}{\text{Total Assets}}$	1.2
X_2 - - - - -	$\frac{\text{Retained Earnings}}{\text{Total Assets}}$	1.4
X_3 - - - - -	$\frac{\text{EBIT}}{\text{Total Assets}}$	3.3
X_4 - - - - -	$\frac{\text{Market Value of Equity}}{\text{Book Value of Total Liabilities}}$	0.6
X_5 - - - - -	$\frac{\text{Sales}}{\text{Total Assets}}$	1.0

Z Score Bankruptcy Model

$$Z = .012X_1 + .014X_2 + .033X_3 + .006X_4 + .999X_5$$

e.g. 20.0%

$$Z = 1.2X_1 + 1.4X_2 + 3.3X_3 + .6X_4 + .999X_5$$

e.g. 0.20

$$X_1 = \frac{\text{Current Assets} - \text{Current Liabilities}}{\text{Total Assets}}$$

$$X_4 = \frac{\text{Market Value of Equity}}{\text{Total Liabilities}}$$

$$X_2 = \frac{\text{Retained Earnings}}{\text{Total Assets}}$$

$$X_5 = \frac{\text{Sales}}{\text{Total Assets}} \quad (= \# \text{ of Times e.g. } 2.0x)$$

$$X_3 = \frac{\text{Earnings Before Interest and Taxes}}{\text{Total Assets}}$$

Zones of Discrimination:
Original Z - Score Model

$Z > 2.99$ - “Safe” Zone

$1.8 < Z < 2.99$ - “Grey” Zone

$Z < 1.80$ - “Distress” Zone

Average Z-Score by S&P Bond Rating S&P 500: 1992 - 2005

<u>Rating</u>	<u>2004-2005</u>	<u>1996-2001</u>	<u>1992-1995</u>
AAA	5.31	5.60	4.80
AA	4.99	4.73	4.15
A	4.22	3.74	3.87
BBB	3.37	2.81	2.75
BB	2.27	2.38	2.25
B	1.79	1.80	1.87
B-	1.34	1.31	1.38
CCC+	0.90	0.82	0.89
CCC	0.45	0.33	0.40
D	-0.19	-0.20	0.05

Estimating Probability of Default and Probability of Loss Given Defaults

- Credit scores on new issues to estimate
- Bond ratings equivalents on new issues and then,
- Utilize mortality rates to estimate annual and cumulative defaults

Marginal and Cumulative Mortality Rate Equation

$$\mathbf{MMR}_{(t)} = \frac{\text{Total value of defaulting debt in year } (t)}{\text{total value of the population at the start of the year } (t)}$$

MMR = Marginal Mortality Rate

One can measure the cumulative mortality rate (CMR) over a specific time period (1,2,..., T years) by subtracting the product of the surviving populations of each of the previous years from one (1.0), that is,

$$CMR_{(t)} = 1 - \prod_{t=1} SR_{(t)},$$

here $CMR_{(t)}$ = Cumulative Mortality Rate in (t) ,
 $SR_{(t)}$ = Survival Rate in (t) , $1 - MMR_{(t)}$

Mortality Rate Concept (Illustrative Calculation)

For BB Rated Issues

Security No.	Issued Amount	Year 1 Default	Call	SF	Year 2 Default	Call	SF
1	50	--	--	5	--	--	5
2	50	50	--	--	NE	NE	NE
3	100	--	100	--	NE	NE	NE
4	100	--	--	--	100	--	--
5	150	--	--	--	--	--	15
6	150	--	--	--	--	--	--
7	200	--	--	20	--	--	20
8	200	--	--	--	--	200	--
9	250	--	--	--	--	--	--
10	250	--	--	--	--	--	--
Total	1,500	50	100	25	100	200	40
Amount Start of Period	1,500	-	175	-	1,325	- 340	= 985
		Year 1			Year 2		
Marginal Mortality Rate		50/1,500 = 3.3%			100/1,325 = 7.5%		
Cumulative Rate		3.3%			1 - (SR1 x SR2) = CMR2 1 - (96.7% x 92.5%) = 10.55%		

NE = No longer in existence
SF = Sinking fund

Mortality Rates by Original Rating

All Rated Corporate Bonds* 1971-2015

Years After Issuance

		1	2	3	4	5	6	7	8	9	10
AAA	Marginal	0.00%	0.00%	0.00%	0.00%	0.01%	0.02%	0.01%	0.00%	0.00%	0.00%
	Cumulative	0.00%	0.00%	0.00%	0.00%	0.01%	0.03%	0.04%	0.04%	0.04%	0.04%
AA	Marginal	0.00%	0.00%	0.21%	0.07%	0.02%	0.01%	0.01%	0.01%	0.02%	0.01%
	Cumulative	0.00%	0.00%	0.21%	0.28%	0.30%	0.31%	0.32%	0.33%	0.35%	0.36%
A	Marginal	0.01%	0.03%	0.12%	0.13%	0.10%	0.06%	0.02%	0.25%	0.08%	0.05%
	Cumulative	0.01%	0.04%	0.16%	0.29%	0.39%	0.45%	0.47%	0.72%	0.80%	0.85%
BBB	Marginal	0.33%	2.36%	1.26%	1.00%	0.50%	0.22%	0.26%	0.15%	0.15%	0.34%
	Cumulative	0.33%	2.68%	3.91%	4.87%	5.34%	5.55%	5.80%	5.94%	6.08%	6.40%
BB	Marginal	0.94%	2.02%	3.88%	1.97%	2.34%	1.51%	1.45%	1.12%	1.43%	3.13%
	Cumulative	0.94%	2.94%	6.71%	8.54%	10.68%	12.03%	13.31%	14.28%	15.51%	18.15%
B	Marginal	2.85%	7.72%	7.85%	7.80%	5.70%	4.48%	3.58%	2.08%	1.76%	0.77%
	Cumulative	2.85%	10.35%	17.39%	23.83%	28.17%	31.39%	33.85%	35.22%	36.36%	36.85%
CCC	Marginal	8.13%	12.43%	17.89%	16.32%	4.85%	11.65%	5.44%	4.84%	0.66%	4.28%
	Cumulative	8.13%	19.55%	33.94%	44.72%	47.40%	53.53%	56.06%	58.19%	58.46%	60.24%

*Rated by S&P at Issuance
Based on 2,903 issues

Mortality Losses by Original Rating

All Rated Corporate Bonds*
1971-2015

Years After Issuance

		1	2	3	4	5	6	7	8	9	10
AAA	Marginal	0.00%	0.00%	0.00%	0.00%	0.01%	0.01%	0.01%	0.00%	0.00%	0.00%
	Cumulative	0.00%	0.00%	0.00%	0.00%	0.01%	0.02%	0.03%	0.03%	0.03%	0.03%
AA	Marginal	0.00%	0.00%	0.03%	0.03%	0.01%	0.01%	0.00%	0.01%	0.01%	0.01%
	Cumulative	0.00%	0.00%	0.03%	0.06%	0.07%	0.08%	0.08%	0.09%	0.10%	0.11%
A	Marginal	0.00%	0.01%	0.05%	0.06%	0.06%	0.04%	0.02%	0.03%	0.05%	0.03%
	Cumulative	0.00%	0.01%	0.06%	0.12%	0.18%	0.22%	0.24%	0.27%	0.32%	0.35%
BBB	Marginal	0.24%	1.54%	0.76%	0.59%	0.27%	0.14%	0.16%	0.09%	0.09%	0.19%
	Cumulative	0.24%	1.78%	2.52%	3.10%	3.36%	3.49%	3.65%	3.74%	3.82%	4.01%
BB	Marginal	0.56%	1.17%	2.31%	1.12%	1.34%	0.71%	0.79%	0.49%	0.74%	1.10%
	Cumulative	0.56%	1.72%	3.99%	5.07%	6.34%	7.01%	7.74%	8.19%	8.87%	9.87%
B	Marginal	1.91%	5.40%	5.33%	5.22%	3.77%	2.46%	2.33%	1.15%	0.92%	0.54%
	Cumulative	1.91%	7.21%	12.15%	16.74%	19.88%	21.85%	23.67%	24.55%	25.24%	25.64%
CCC	Marginal	5.38%	8.70%	12.52%	11.49%	3.39%	8.62%	2.34%	3.39%	0.41%	2.73%
	Cumulative	5.38%	13.61%	24.43%	33.11%	35.38%	40.95%	42.33%	44.29%	44.51%	46.03%

*Rated by S&P at Issuance
Based on 2,481 issues

Financial Distress Prediction Applications

- Lenders
- Investors
- Long/Short Investment Strategy on Stocks
- Security Analysts
- Regulators & Gov' t Agencies
- Auditors
- Legal Direction – e.g. “Deepening Insolvency”
- Credit Rating Agencies
- Sovereign Default Risk Assessment
- Advisors
- M&A
- Purchasers, Suppliers
- Accounts Receivable Management
- Researchers
- Chapter 22 Avoidance
- MANAGERS
 - Managing a Financial Turnaround

Managing a Financial Turnaround: The GTI Case

Caveats for a Successful Turnaround

Objectives

- To demonstrate that specific management tools which work are available in crisis situations
- To illustrate that predictive models can be turned “inside out” and used as internal management tools to, in effect, reverse their predictions
- To illustrate an interactive, as opposed to a passive, approach to financial decision making

Physical Facilities & Financial Situation

- 7 Manufacturing facilities (California to New York)
- 3 Offices locations (California to Germany)
- American Stock Exchange Listed Company
- Incorporated in late 1960' s
- Successful IPO through early 1970' s

Financial Changes at GTI during 1st half of 75

- Working Capital decreased by \$6 million
- Retained Earnings decreased by \$2 million
- A \$2 million loss incurred
- Net Worth decreased from \$6,207 to \$4,370
- Market Value of Equity decreased by 50%
- Sales decreased by 50%

Ethical Consideration

- Pressure led to “Corner Cutting”
- Returns not reported
- Bad inventory (and too much of it)
- Questionable Deferrals and Reserves levels

Employee Moral & Attitude

- Internally Competitive
- Angry
- Insecure

Management's Responsibility

- “PROTECT and ENHANCE
the Stockholders Investment in GTI”
(Words of the new CEO)

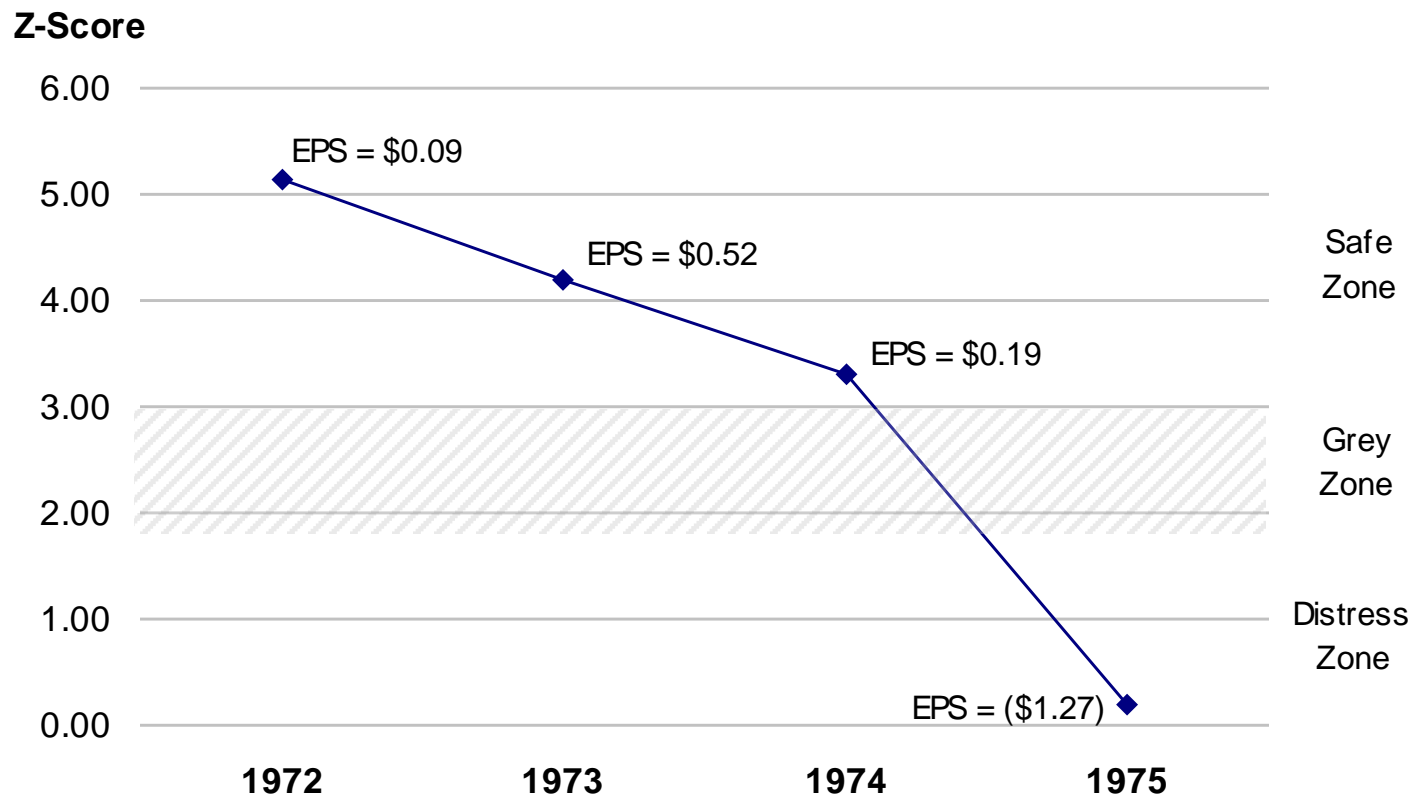
Material to be Covered

- Condition of GTI in June of 1975
- Management & Control changes
- Definition of Management's Responsibility
- Description of Management tools used
- Caveats for a successful Turnaround

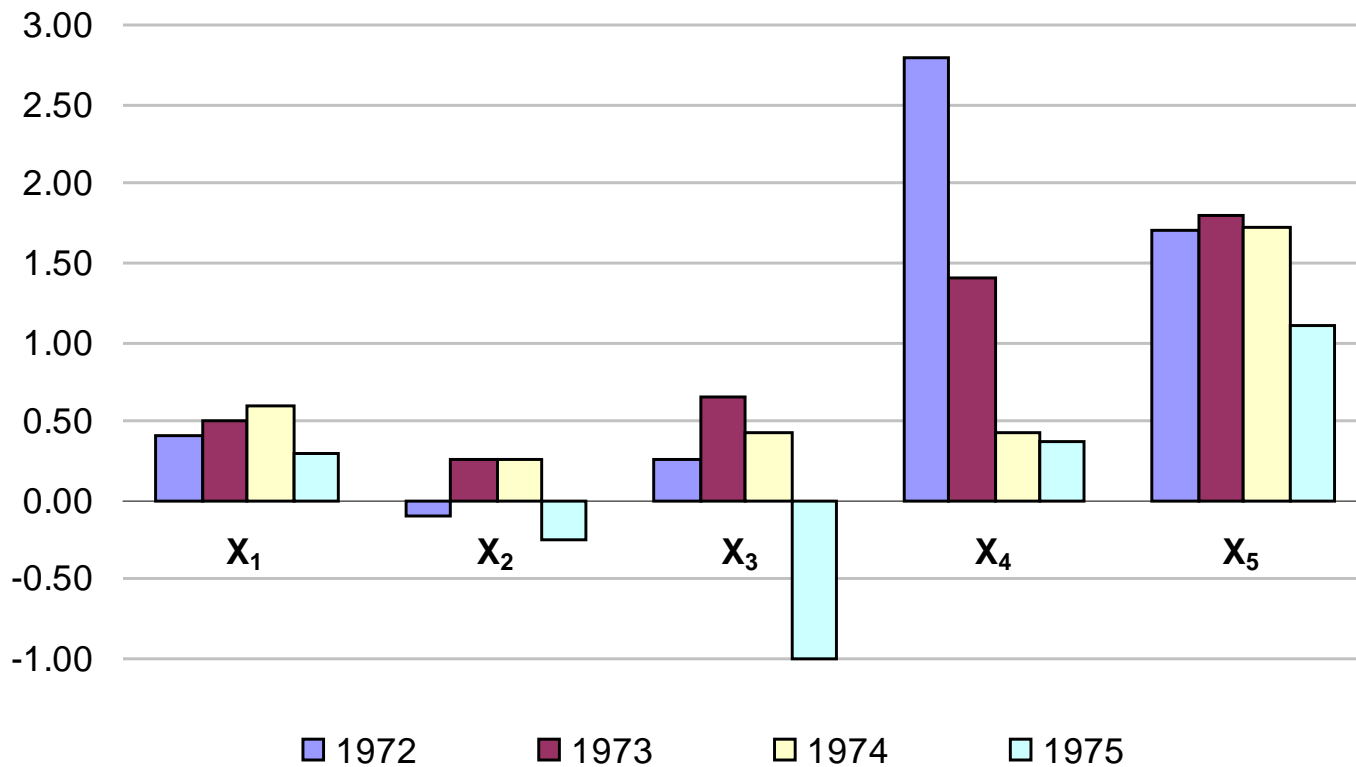
Z-Score Component Definitions

<u>Variable</u>	<u>Definition</u>	<u>Weighting Factor</u>
X_1	$\frac{\text{Working Capital}}{\text{Total Assets}}$	1.2
X_2	$\frac{\text{Retained Earnings}}{\text{Total Assets}}$	1.4
X_3	$\frac{\text{EBIT}}{\text{Total Assets}}$	3.3
X_4	$\frac{\text{Market Value of Equity}}{\text{Book Value of Total Liabilities}}$	0.6
X_5	$\frac{\text{Sales}}{\text{Total Assets}}$.999

Z-Score Distressed Firm Predictor: Application to GTI Corporation (1972 – 1975)



Components of Z-Score Distressed Firm: *Predictor as Applied to GTI Corporation*



Management Tools Used

- Altman's Distressed Firm Predictor (Z-Score)
- Function / Location Matrix
- Financial Statements
- Planning Systems
- Trend Charts

Strategy

- **Strategy #1:** Reduce Personnel & Eliminate Capital Spending
- **Reason:** Reverse Cash drain
- **Tool:** Source and Application of Funds
- **Timing:** Immediate

Strategy

- **Strategy #2:** Consolidate Locations
- **Reason:** Reduce Management Costs
- **Tool:** Function Location Matrix
- **Timing:** Short and Long Term Planning

Function / Location Matrix

	Pennsylvania	Indiana	New York	California	West Germany	
Operations	\$1	\$1	\$1	\$1	\$1	\$5
Marketing	\$1	\$1	\$1	\$1	\$1	\$5
Engineering	\$1	\$1	\$1	\$1	\$1	\$5
Finance	\$1	\$1	\$1	\$1	\$1	\$5
	\$4	\$4	\$4	\$4	\$4	\$20

Key Actions - 1975

- Immediate Reduction of Personnel
- Stop Capital Spending
- Consolidate Profitable Product Lines

Z-Score Component Definitions

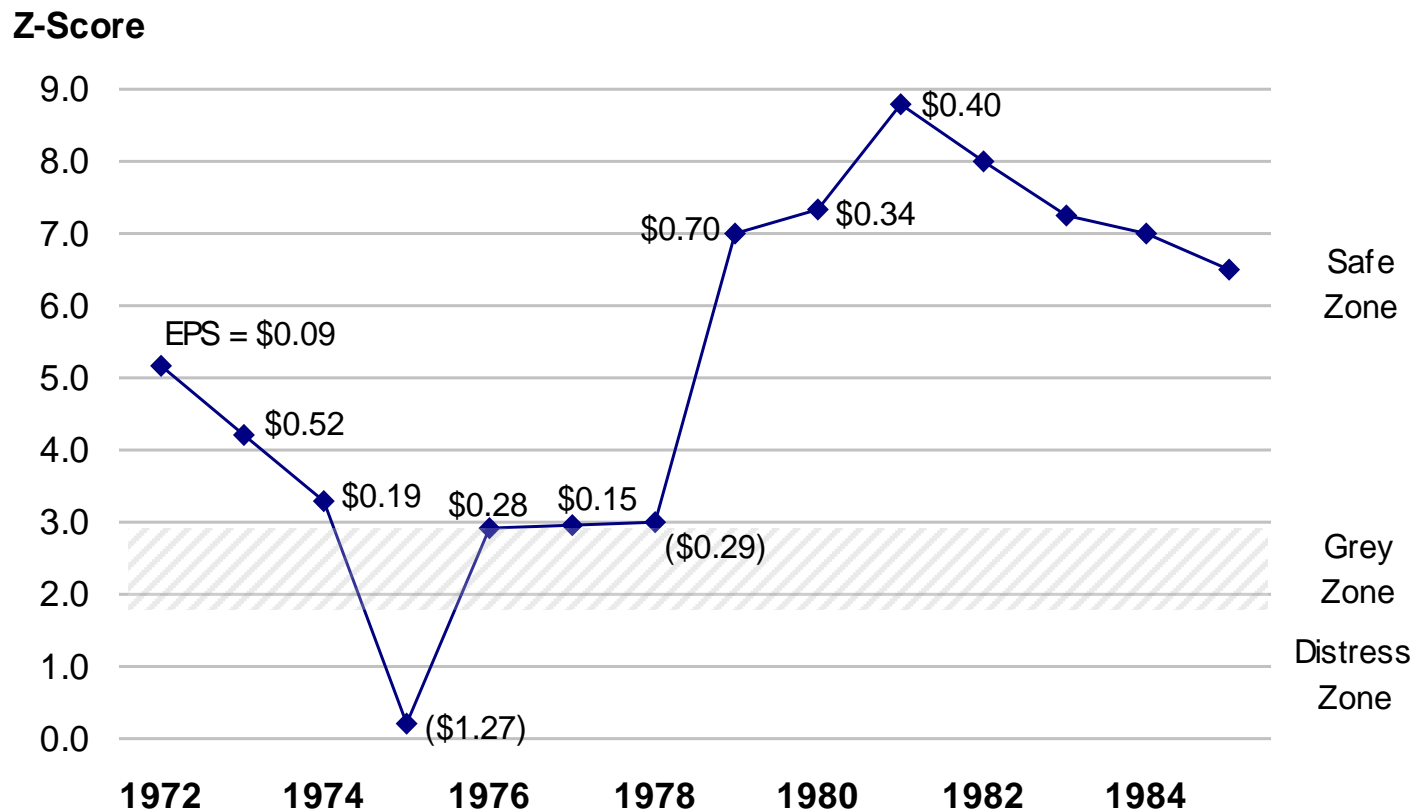
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Managerial & Financial Restructuring Actions and Impact on Z-Score

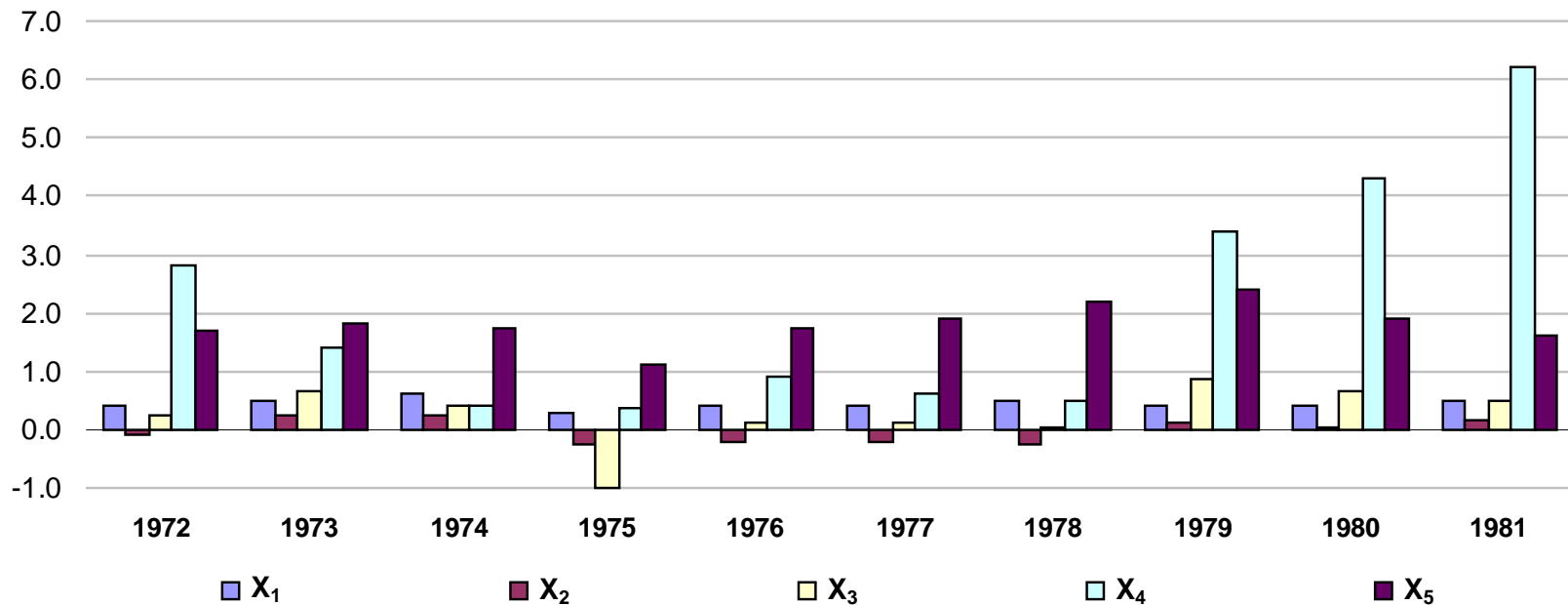
<u>Strategy</u>	<u>Reason</u>	<u>Impact</u>
Consolidated Locations	Eliminate Underutilized Assets	Z-Score
Drop Losing Product Lines	Eliminate Unprofitable Underutilized Assets	Z-Score
Reduce Debt Using Funds Received from Sale of Assets	Reduce Liabilities and Total Assets	Z-Score

Z-Score Distressed Firm Predictor

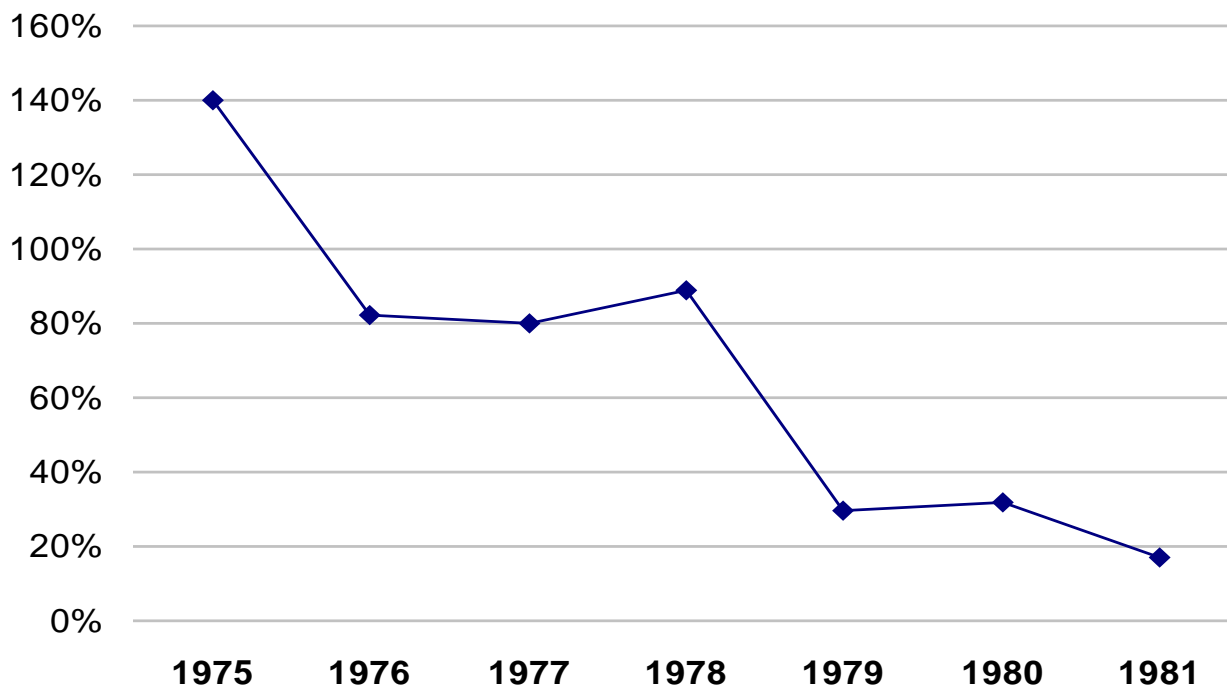
Application to GTI Corporation (1972 – 1984)



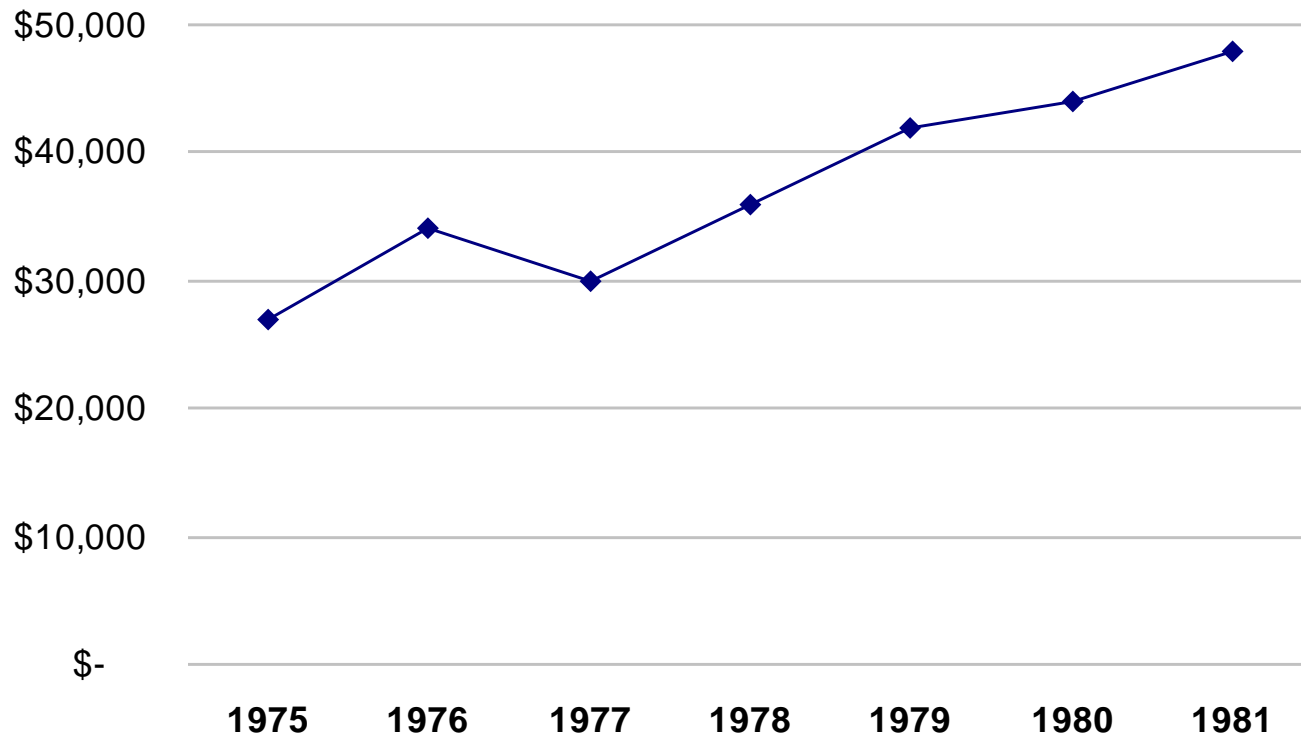
Components of Z-Score Distressed Firm: *Predictor as Applied to GTI Corporation*



Debt / Equity Ratio



Sales Dollars / Employee





Distress Prediction Model
For Chinese Companies

Z_{China} Model for Chinese Companies

Model Development and Test Results

- **Training:** **30** “ST” (Special Treatment Distressed Companies) based on
Sample two consecutive years of negative earnings or NAV below par value
 listed on Sheuzhen or Shanghai Stock Exchanges (1998,1999).
 30 “Non – ST” listed companies (Healthy)
 60

- **Holdout (Test) :** **21** “ST” Companies (1998,1999)
Sample 39 “Non – ST” Companies (Randomly Selected)
 60

- **Variable Selection:** 15 Financial Ratios from one year before “ST,” including Profitability, Solvency, Liquidity and Asset Management Measures. Based on their acceptance in China as well as from several prior distress prediction models outside of China.

Based on a study, “Corporate Financial Distress Diagnosis in China,” L. Zhang, J. Yen and E. Altman, Summer 2007.

Model for Distress Prediction in China

$$Z_c = 0.517 - 0.388 (X_1) + 1.158 (X_2) + 9.320 (X_3) - 0.460 (X_4)$$

Where:

	<u>Mean “ST”</u>	<u>Mean “Non-ST”</u>
$X_1 = \text{Working Capital} / \text{Average Total Assets (ATA)} =$	• -0.17	0.12
		(F = 5.8)
$X_2 = \text{Retained Earnings} / \text{TA} =$	• -0.33	0.22
		(F = 19.8)
$X_3 = \text{Net Profit} / \text{ATA} =$	• -0.36	0.26
		(F = 139.1)
$X_4 = \text{Total Liabilities} / \text{TA} =$	• 0.75	0.42
		(F = 42.4)

Classification Accuracy

Training Sample

<i>Actual Classification</i>		<i>Predicted Classification</i>	
		<u>Distressed</u>	<u>Non-Distressed</u>
Distressed (“ST”)	30	30 (100%)	0
Non-Distressed	0	0	30 (100%)

Accuracy Over Time

<u>Years Prior to “ST”</u>	<u>Accuracy Level</u>
1	100%
2	87%
3	70%
4	60%
5	22%

Holdout Sample Accuracy

	<u># of Firms</u>	Predictive Accuracy	
		<u>(0.5) Cutoff</u>	<u>(0.3) Cutoff</u>
Distressed	21	21 (100%)	19 (90%)
Non-Distressed	39	34 (87%)	39 (100%)

Rating Distribution of Listed Chinese Companies

Rating Level	Z _c -Score Interval	Percentage Each Year							
		1998	1999	2000	2001	2002	2003	2004	2005
AAA	≥ 1.8	6.3%	4.3	2.3	0.9	1.0	1.2	2.8	2.5
AA	1.3 – 1.8	17.5	11.0	9.2	5.9	4.2	5.8	5.4	5.7
A	0.9 – 1.3	31.6	31.3	27.6	18.5	15.3	14.8	15.1	12.4
BBB	0.5 – 0.9	24.7	29.3	37.8	40.2	39.6	36.3	34.4	31.8
BB	0.0 – 0.5	10.7	16.1	15.2	22.4	25.6	28.8	28.2	28.8
B	-1.0 – 0.0	4.9	5.0	4.6	7.3	8.1	1.5	6.8	9.4
C	-2.0 – - 1.00	2.7	1.6	1.6	2.6	2.8	1.0	2.6	3.7
D	Z _c < -2.0	1.6	1.6	1.7	2.2	3.5	10.6	4.6	5.8

Credit Ratings of "ST" Companies Announced in 2002

Rating Level	2002 (#)	2002 (%)	2001 (%)	2000 (%)	1999 (%)	1998 (%)
AAA	0	0	0	3.6	3.5	7.1
AA	0	0	0	3.6	7.1	7.1
A	0	0	0	10.7	3.6	10.7
BBB	1	3.6	0	14.3	21.4	28.6
BB	6	21.4	14.3	14.3	39.3	21.4
B	8	28.6	25.0	46.4	17.9	10.7
C	5	17.9	28.6	3.6	7.1	10.7
D	8	28.6	32.1	3.6	0.0	3.6

Total 28 Companies