Empirical Market Microstructure Joel Hasbrouck

Corrigenda and Addenda: (Typos, Thinkos, Misprints, and Enhancements)

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Special thanks to Juhani Linnainmaa, Albert Menkveld, Ting Wang and Michel van der Wel.

There are some minor typos of the sort wherein an "an" is printed as "and". I list below the more substantive typos.

Chapter 4. Page 34. The line immediately after the formula should start "where $\{\varepsilon_t\}$ is a zero-mean white noise process..."

Chapter 4. Page 36. Line immediately after the formula should be "...a power series expansion of $(1 - \phi L)^{-1}$." (AM)

Chapter 5. Page 45. Equation (5.5) should read:

$$A = E[V | Buy] = \frac{\underline{V}(1-\mu)\delta + V(1+\mu)(1-\delta)}{1+\mu(1-2\delta)}$$

Chapter 5. Page 46. Equation (5.6) should read:

$$B = E[V | Sell] = \frac{\underline{V}(1+\mu)\delta + \overline{V}(1-\mu)(1-\delta)}{1-\mu(1-2\delta)}$$

Chapter 8. Page 68. Third paragraph. Here's some more detail on the timing:

- 1. The dealer enters time *t* knowing $m_{t-1} = E\left[Value | u_{t-1}, u_{t-2}, \dots, q_{t-1}, q_{t-2}, \dots\right]$
- 2. The time-*t* public information arrives (u_t) , and $E[Value | u_t, u_{t-1}, u_{t-2}, ..., q_{t-1}, q_{t-2}, ...] = m_{t-1} + u_t$.
- 3. The time-*t* trader arrives, and submits an order of $q_t = \pm 1$:

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$$m_{t} = E\left[Value | u_{t}, u_{t-1}, u_{t-2}, \dots, q_{t}, q_{t-1}, q_{t-2}, \dots\right] = m_{t-1} + u_{t} + \lambda q_{t},$$

It is in this sense that $m_t = m_{t-1} + w_t$ where $w_t = \lambda q_t + u_t$.

If there were no non-informational costs (c = 0), then the price paid by a purchaser (the ask) would be $m_t = m_{t-1} + u_t + \lambda$; similarly, the bid would be $m_t = m_{t-1} + u_t - \lambda$. With transaction costs, the ask and bid will be set at $m_t \pm c$.

Chapter 6. Page 58. The " ε_x " in equation (6.3) should be simply " ε ".

Chapter 7. Page 63. In (7.3),

$$\mu = \frac{-\alpha\beta\Sigma_0 + \sigma_u^2 p_0}{\sigma_u^2 + \beta^2\Sigma_0}$$

Chapter 8. Page 69.

In equation (8.4), $f_t \equiv \lim_{k \to \infty} E^* [p_{t+k} | p_t, p_{t-1}, ...]$, i.e., the limit of the infinite-horizon expectation. Earlier, in the context of the basic Roll model (page 39), f_t denoted the one-period ahead forecast: $f_t \equiv E^* [p_{t+1} | p_t, p_{t-1}, ...]$. For the basic (and generalized) Roll model, $\lim_{k \to \infty} E^* [p_{t+k} | p_t, p_{t-1}, ...] = E^* [p_{t+1} | p_t, p_{t-1}, ...]$ because price differences are MA(1).

In the last line of the page, " $\beta_0 \varepsilon_1$ " should be " $\beta_0 \varepsilon_t$ ".

Chapter 8. Page 71.

7th line from the top " $\varepsilon_t + \theta \varepsilon_t$ " should be " $\varepsilon_t + \theta \varepsilon_{t-1}$ ".

In the third paragraph, " $\sigma_s^2 = \underline{\sigma}_s^2$ " should be " $\sigma_s^2 \ge \underline{\sigma}_s^2$ "

Note on equation (8.7) on page 71. This equation follows from the one in the line above it, $\underline{\sigma}_s^2 = \theta^2 \sigma_{\varepsilon}^2$. There are two ways of getting θ and σ_{ε}^2 . The first way is via direct inspection (as in the preceding paragraph). The second way is to compute the autocovariances γ_0 and γ_1 from equation (8.3), letting $\sigma_u^2 = 0$, and the go from the autocovariances to the MA parameters via (4.2).

Chapter 8. Page 76. Third paragraph. " $\sigma_w^2 = \left[\phi(1)\right]^2 \sigma_\varepsilon^2$ " should be" $\sigma_w^2 = \left[\phi(1)\right]^{-2} \sigma_\varepsilon^2$ "

Chapter 8. Page 77. "...(1-z)B(z)." should be "... $(1-z)B(z)\sigma_{\varepsilon}^{2}$."

Chapter 9, page 80. Equation (9.8) should read (in part):

 $\theta_1 = \begin{bmatrix} 0 & c(\beta - 1) \\ 0 & 0 \end{bmatrix}$

Chapter 9. Page 84. Equation 9.20 should read: "F' = ..."

Chapter 9. Page 85. 3rd line from the top. " $m_t = m_t + w_t$ " should be " $m_t = m_{t-1} + w_t$ ".

Chapter 10, page 95. Equation 10.2 should read:

$$\Gamma_0 \equiv \operatorname{Var}(\Delta p_t) = \begin{bmatrix} 2c^2 + \sigma_u^2 & 2\rho c^2 \\ 2\rho c^2 & 2c^2 + \sigma_u^2 \end{bmatrix}$$

(Thanks to Juan Cabrera)

Page 99. Equation (10.10) comes from computing $\theta(L)^{-1}(1-L)$, using $\theta(L) = 1 + \theta_1 L$ and the solution to θ_1 given in (10.8).

Page 123. Third paragraph. " $b_T < B/V$ " should read " $\beta_T < B/V$ "

Chapter 12. Figure 12-4. The numerical values on the horizontal axis are not correct. The figure should be:

