

Exercise Set 1
September 6, 2006
(due September 13)

1. A monopolist has a short-run cost function,
$$C(q) = f + cq^2,$$
where q is the quantity produced per month, and f and c are strictly positive constants. The demand for the product, per month, is
$$D(p) = \max\{a - bp, 0\},$$
where p is the price, and a and b are strictly positive constants.
 - (a) Derive a formula for the monopolist's optimal price and quantity, as a function of the parameters of the problem. Make explicit any further assumptions you use to complete your model.
 - (b) Qualitatively, how do the optimal price and quantity depend on c ? Draw corresponding schematic graphs to illustrate your conclusions. How do the optimal price and quantity depend on f ?
2. In an extension of the model of (Tyagi, 1999), derive formulas for the retailer pass-through corresponding to equation (3) and condition (4), in the case in which the retailer's cost of marketing a quantity q per unit time is
$$C(q) = f + cq + wq,$$
where f and c are strictly positive constants, and w is the wholesale price. Discuss your results. [Hint: this question can be answered without any detailed mathematical calculations.]